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CONF - 860616 - - 1

TITLE HIGH EXPLOSIVE MODELING IN 2D EULER CODE FOR SHAPED CHARGE PROBLEMS

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SUBMITTED TO International Symposium on Intense Dynamic Loading and Its Effects. Beijing, China, June 3-7, 1986

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## High-Explosive Modeling in 2D Euler Code for Shaped Charge Problems

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### Abstract

The object of this study is to incorporate a programmed burn model of high explosive into a two-dimensional, smeared shock Eulerian hydrodynamic code. Huygen's principle and Chapman-Jouguet theory are used in defining the detonation velocity and the location where the high-explosive energy is released. Precalculated burn information such as burn times, burn distances, burn intervals, and burn fractions are implemented into the code before the hydrodynamic actions take place. Two shaped charge problems are tested using the present code and the results are compared with the experimental data, as well as those from other codes.

### I. Introduction

Computer simulations for the detonation of high explosive have drawn more attention recently both in industrial applications and laboratory analysis. There are two approaches, namely programmed burn and reactive burn, used in modeling the high-explosive energy release. Programmed burn is easy and stable when it is incorporated with hydrodynamic calculations while the reactive burn model may be more accurate, but more expensive and unstable.

Most of the 2D codes for general engineering design purpose are still using the programmed burn. For example, the 2D Lagrangian codes, HEMP[1], DYNA2D[2], EPIC2[3], MAGEE[4], and the 2D Eulerian codes, HELP[5], HULL[6], and SOIL[7]. Those codes produce good computed results compared with the experimental data although the programmed burn is the only tool for adding the high explosive released energy to the systems.

The present work uses the improved particle-in-cell (PIC) numerical scheme which is second-order accurate in time and space. The PIC method can be interpreted as a Lagrangian calculation (Phase I) followed by an Eulerian remapping (Phase II) back to the original cell locations. The high explosive deposits its energy to the system in Phase I only. Finally, two examples of high-explosive driven metal formation (shaped charge) are shown to demonstrate accuracy of the model.

### II. The Operator Splitting and PIC Method

The present work uses operator splitting and particle-in-cell methods to solve the dependent variables such as density, velocity, and internal energy. For a cylindrical coordinate, the governing equations are split into two parts and solved in radial ( $r$ ) and axial ( $z$ ) directions separately. In order to maintain a better accuracy, the calculations are alternated in directions for each computational cycle, e.g.,  $r$ - $z$ - $z$ - $r$  or  $z$ - $r$ - $r$ - $z$ . The computational procedures can be briefly described in two phases: In phase I, known as the

Lagrangian phase, the Lagrangian quantities at the (n+1)th time step are computed based on previous known quantities, i.e., the (n)th time step. In phase 2, known as remap or particle transport phase, the particles are transported according to a "tilde" velocity. The new cell mass (at n+1 time step) is the sum of the masses of the particles in that cell after transport. The new velocity is the final momentum in the cell divided by the new cell mass. The new cell specific internal energy is the final total internal energy divided by the new cell mass.

The partial differential equations for the compressible flow are given below for r and z directions separately.

For the r direction, we have

$$\rho_t = -\bar{u} \rho_r - \frac{P}{r} (ru)_r \quad (\text{mass}) \quad (1)$$

$$u_t = -\bar{u} u_r - \frac{1}{\rho} P_r \quad (\text{r momentum}), \quad (2)$$

$$v_t = -\bar{u} v_r \quad (\text{z momentum}), \quad (3)$$

and

$$e_t = -\bar{u} e_r - \frac{P}{\rho r} (ru)_r + S \quad (\text{energy}). \quad (4)$$

For the z direction, we have

$$\rho_t = -\bar{v} \rho_z - \rho v_z \quad (\text{mass}), \quad (5)$$

$$u_t = -\bar{v} u_z \quad (\text{r momentum}), \quad (6)$$

$$v_t = -\bar{v} v_z - \frac{1}{\rho} P_z \quad (\text{z momentum}), \quad (7)$$

and

$$e_t = -\bar{v} e_z - \frac{P}{\rho} v_z + S \quad (\text{energy}). \quad (8)$$

In Eqs. (1) through (8),  $\rho$  is the density,  $t$  the time,  $\bar{u}$  and  $\bar{v}$  the cell edge time average velocities in r and z directions,  $P$  the pressure,  $u$  and  $v$  the velocities in r and z directions,  $S$  the energy source due to high explosive, and the subscripts  $t$ ,  $r$ , and  $z$  represent the first derivative, i.e.,  $\frac{\partial}{\partial t}$ ,  $\frac{\partial}{\partial r}$ , and  $\frac{\partial}{\partial z}$ .

In high-explosive programmed burn, the basic assumption is that the detonation wave front travels in all directions at the Chapman-Jouguet detonation velocity. Information concerning the energy released from high explosive such as burn time (BT) and burn interval (BI), are precalculated and stored in the code at time  $t = 0$ . During the run, when the problem time  $T^n$ , at cycle  $n$ , becomes greater than the BT value of a high-explosive cell, but less than  $(BT + BI)$ , a fraction of the specific energy for the particular HE is deposited in the cell. This fraction is given by  $(T^n - BT)/BI$ . On the next cycle, at  $T^{n+1}$ , if  $T^{n+1}$  is still less than  $(BT + BI)$ , another fraction

$(T^{n+1} - T^n)/BI$  of specific energy is deposited in the cell. This continues until the cell is completely burned.

The burn calculations depend on the Huygen's construction for the burn distance. In Fig. 1, if A is the detonation point, then the burn distances to points 1 and 2 are the line-of-sight distances from the detonation point, i.e., lines A1 and A2. However, the calculation of the burn distance to point 3 is more complex because point 3 is located in the shadow region from point A. In this case, the burn distance is obtained from the shortest distance of the high-explosive wave paths including a new spherical wave centered at point B. One possible solution of the burn distance for point 3 is the total distances of line AB, chord BC, and line C3.

### III. Test Problems and the Results

In modeling the test problems, a 2D Lagrangian code was used to initialize the setup and do short time calculation so that the liner will become thicker, which will allow the Eulerian code to have more zones in the liner.

The first test problem is a confined, hemispherical, copper-lined, shaped charge with PBX-W-113 as high explosive. The computational simulation of the charge and the initial conditions are shown in Fig. 2, with the thickness of the aluminum case 0.635 cm and the copper liner 0.47498 cm. The explosive charge was simultaneously initiated at all points along the AB plane which is a circular disc. The surfaces along HE, EF and GF are treated as continuous flow boundary conditions, while the z-axis as a nonflow, reflective boundary.

The equation of state for the high explosive is the Jones-Wilkins-Lee (JWL) set, which can describe the pressure-volume-energy relation of the detonation products very accurately in involving metal acceleration. The JWL-EOS for the pressure is:

$$P = A \left(1 - \frac{\omega}{R_1 V}\right) e^{-R_1 V} + B \left(1 - \frac{\omega}{R_2 V}\right) e^{-R_2 V} + (L - c_1) \frac{\omega}{V} \quad (9)$$

where  $A = 9.50448$  MBar,  $B = 0.10915$  MBar,  $R_1 = 5.0$ ,  $R_2 = 1.4$ ,  $\omega = 0.40$ ,  $c_1 =$  undetonated HE and  $c$  the detonation energy. In computing the detonation energy released, we also need the following C-J parameters:  $\rho_0 = 1.672$  g/cm<sup>3</sup>,  $D = 0.8311$  cm/ $\mu$ sec,  $c_0 = 0.087$  MBar  $\cdot$  cm<sup>3</sup>/cm<sup>3</sup> and  $c_{\text{chemical}} = c_0 + c_1 = 0.742686$  MBar  $\cdot$  cm<sup>3</sup>/cm<sup>3</sup>. The geometry of the collapsing copper liner and the jet formations is given in Figs. 3 through 5. The jet starts to collapse at about 40  $\mu$ sec after the charge initiation as shown in Fig. 3. At time = 70  $\mu$ sec, the wings of the jet were bent toward the jet tip direction as a result of the aluminum case. Fig. 5 shows a jet of 34-cm long and with the maximum width of 4-cm near the slug region. The cumulative mass versus velocity plot at time = 100  $\mu$ sec is shown in Fig. 6 with the tip velocity of 0.50 cm/ $\mu$ sec. The experimental data shows that the tip velocity at time = 100  $\mu$ sec, is 0.496 cm/ $\mu$ sec. This suggests that the numerical simulation is off by 0.8%.

The second charge studied had a conical, 42° copper liner, 2-mm thick and was loaded with Comp. B. Both experimental and computational charges were confined with aluminum bodies and had cone diameters of 81.3 mm as shown in Fig. 7. The explosive region was detonated by single point initiated at point A for the modeling calculations. Again, we use the JWL EOS, i.e., Eq. (8), with the constants,  $A = 5.242$  MBar,  $B = 0.07678$  MBar,  $R_1 = 4.2$ ,  $R_2 = 1.1$ ,  $\omega = 0.34$ , and  $c_1 = 0.2644163$  MBar  $\cdot$  cm<sup>3</sup>/cm<sup>3</sup>. The C-J parameters are  $\rho_0 = 1.717$

$\text{g/cm}^3$ ,  $D = 0.798 \text{ cm}/\mu\text{sec}$ ,  $\epsilon_0 = 0.085 \text{ MBar} - \text{cm}^3/\text{cm}^3$ , and  $\epsilon_{\text{chemical}} = 0.3494165 \text{ MBar} - \text{cm}^3/\text{cm}^3$ . The experimental measurements recorded were the collapse angles along the inside and outside surfaces of the liner wall,  $\beta^{\text{in}}$  and  $\beta^{\text{out}}$  respectively, and the distance,  $L$ , from the stagnation point to the rear of the slug. The radiographs of the collapse process were taken at delay time of 25, 31, and 37  $\mu\text{sec}$  after the initiation of the charge. Due to the detonator/booster assembly in the experiment, there is a difference of 9.5  $\mu\text{sec}$  between the data and calculations. Table I shows the comparisons among the data, HEMP and present codes calculations. The HEMP code calculations and the detail geometry of the shaped charge are reported in Reference 9. The cumulative mass versus jet velocity is plotted in Fig. 8 with tip velocity of 0.73  $\text{cm}/\mu\text{sec}$  (experimental data is 0.77  $\text{cm}/\mu\text{sec}$ ). The present code simulation shows that the jet starts to break at 106  $\mu\text{sec}$  (Fig. 9) as compared to the data of 106.4  $\mu\text{sec}$  [9].

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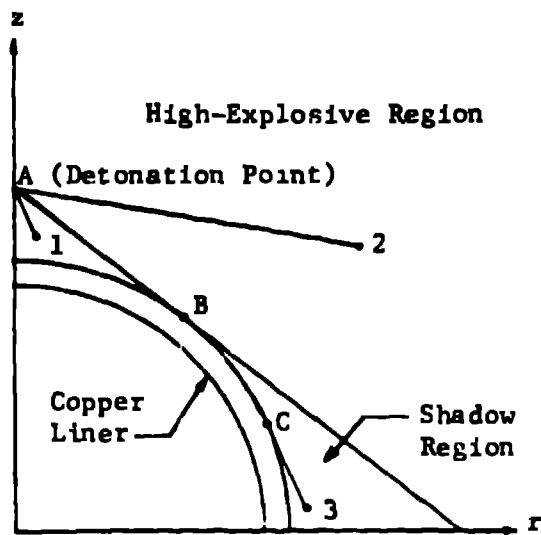


Fig. 1. Huygen's Construction for Burn Distances

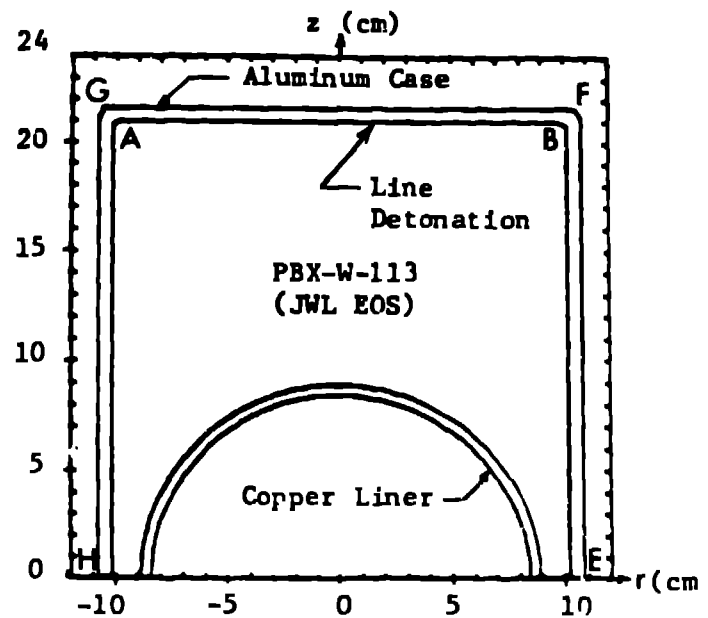


Fig. 2. Initial Geometry of First Test Problem

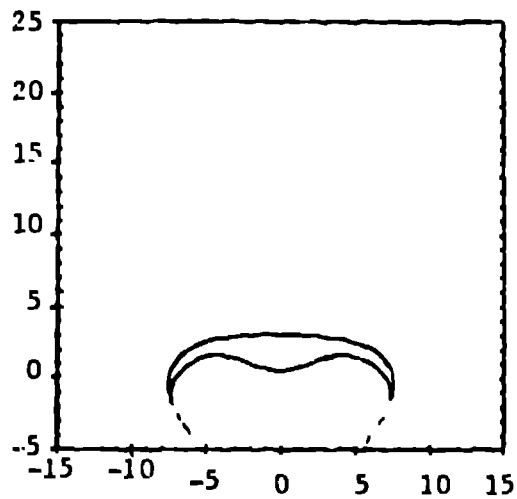


Fig. 3. Jet Shape at time = 40  $\mu$ sec

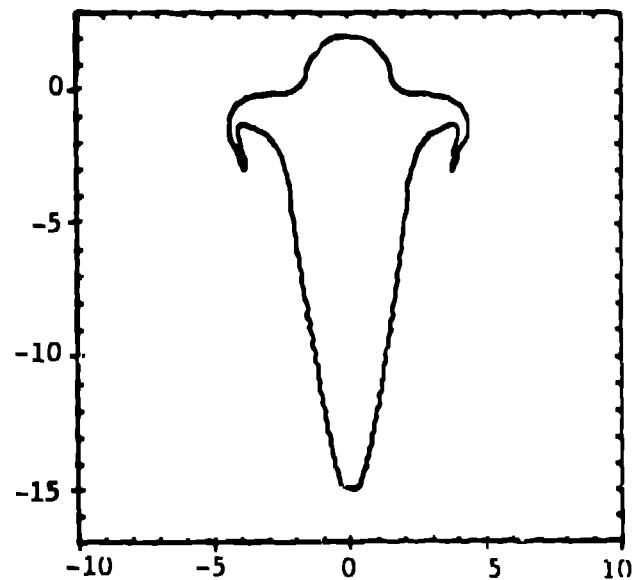


Fig. 4. Jet Shape at time = 70  $\mu$ sec

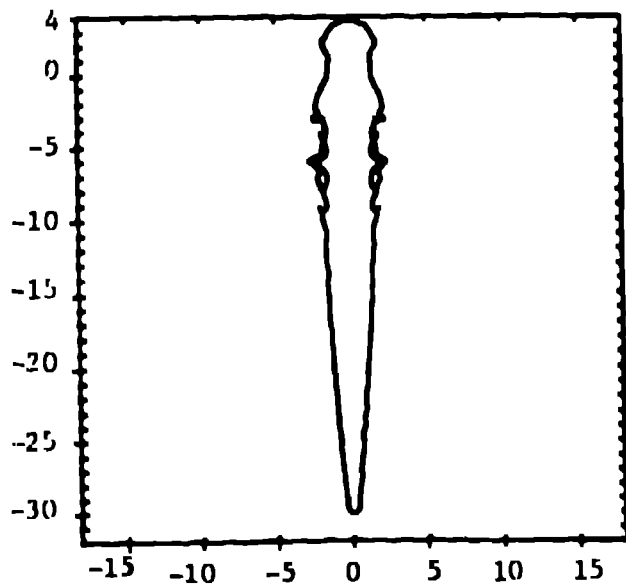


Fig. 5. Jet Shape at time = 100  $\mu$ sec

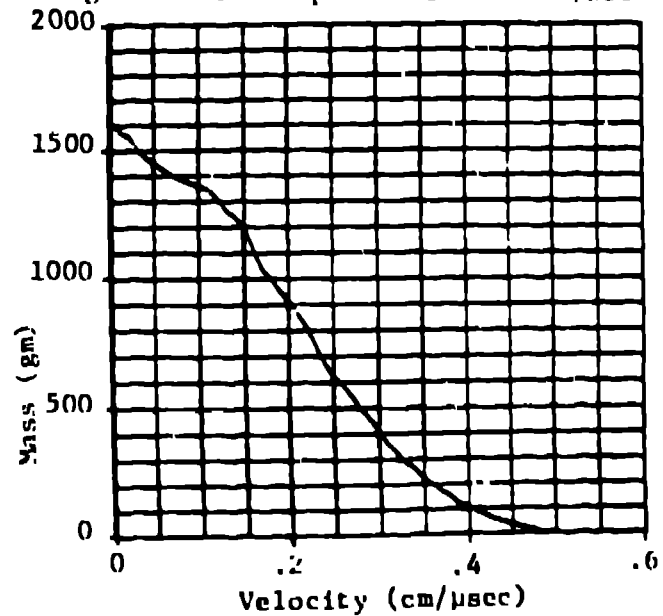


Fig. 6. Cumulative Mass versus Velocity at time = 100  $\mu$ sec

Fig. 7. Sketch of 81.3 mm BRL Precision Charge

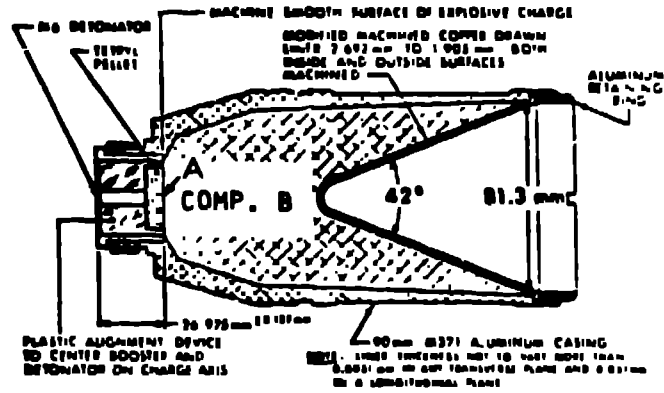


TABLE 1.  
COLLAPSE SEQUENCE FOR A 42° COMP. B CHARGE -  
X-RAY OBSERVATIONS VS. CODE CALCULATIONS

	Elapsed Time	Collapse Angle		L *
1) X-Rays	25.0 $\mu$ s	$\beta_{in} = 33^\circ$	$\beta_{out} = 32^\circ$	20mm
HEMP	15.5 $\mu$ s	$\beta_{in} = 33^\circ$	$\beta_{out} = 32^\circ$	26mm
PRESENT STUDY	15.5 $\mu$ s	$\beta_{in} = 35^\circ$	$\beta_{out} = 32^\circ$	21mm
2) X-Rays	31.0 $\mu$ s	$\beta_{in} = 42^\circ$	$\beta_{out} = 39^\circ$	44mm
HEMP	21.5 $\mu$ s	$\beta_{in} = 42^\circ$	$\beta_{out} = 36^\circ$	50mm
PRESENT STUDY	21.5 $\mu$ s	$\beta_{in} = 42^\circ$	$\beta_{out} = 39^\circ$	45mm
3) X-Rays	37.0 $\mu$ s	$\beta_{in} = 53^\circ$	$\beta_{out} = 49^\circ$	58mm
HEMP	27.5 $\mu$ s	$\beta_{in} = 54^\circ$	$\beta_{out} = 47^\circ$	76mm
PRESENT STUDY	27.5 $\mu$ s	$\beta_{in} = 53^\circ$	$\beta_{out} = 49^\circ$	68mm

$\Delta t = 0.5\mu s$

\* L is the distance from the stagnation point to the rear of the slug.

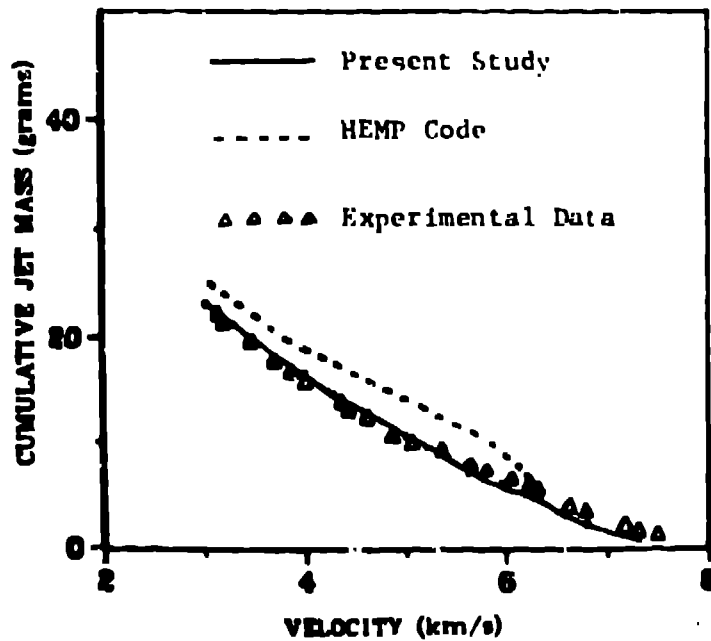


Fig. 8. Mass vs. Velocity Plot for Present Study, HEMP and Data

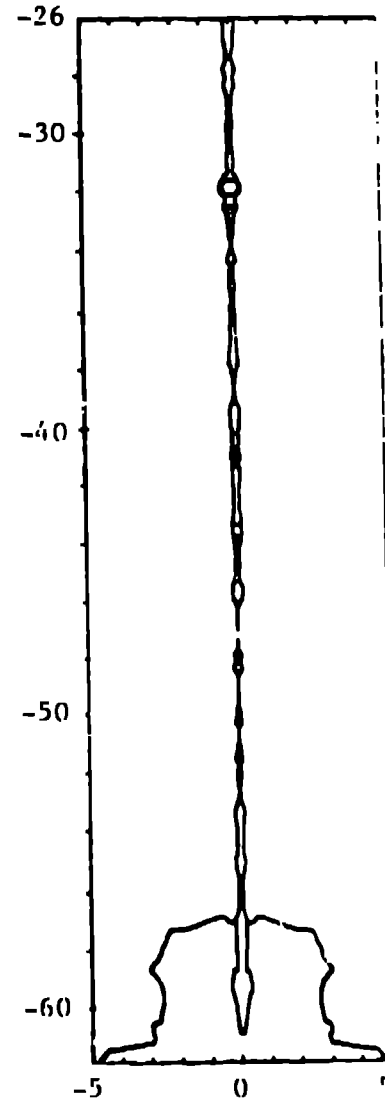


Fig. 9. The Jet Starts to Break at time = 106  $\mu$ s (only 24.2 gm of Jet are shown).