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*Thermal Equilibrium Population
of the First Few Nuclear Excited States
(Ac, Th, Pa, U, Np, Pu, Am, Cm,
Bk, and Cf Isotopes)*

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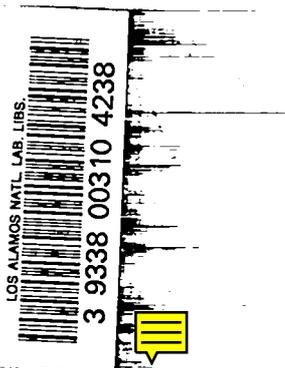
LA-10111-MS

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**Thermal Equilibrium Population
of the First Few Nuclear Excited States
(Ac, Th, Pa, U, Np, Pu, Am, Cm,
Bk, and Cf Isotopes)**

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**THERMAL EQUILIBRIUM POPULATION OF THE
FIRST FEW NUCLEAR EXCITED STATES
(Ac, Th, Pa, U, Np, Pu, Am, Cm, Bk, and Cf ISOTOPES)**

by

G. D. Doolen, H. H. Hsu, and C. L. Doolen

ABSTRACT

The Boltzmann distributions of nuclear excited states are plotted for most actinide isotopes for temperatures from 0 to 60 keV.

When working with nuclear excited states, it is often useful to refer to plots of thermal equilibrium populations as a function of material temperature. These Boltzmann distribution plots are easily generated, and they are useful for understanding nuclear behavior in high-temperature environments. Such plots for the actinides form the main content of this report. Two subsequent reports are planned: one on the lanthanides and the other on the remaining detector isotopes.

The plots contain the Boltzmann thermal equilibrium nuclear excited state populations. The fraction excited in state i , with excitation energy, E_i , equals

$$(2J_i + 1) \exp(-E_i/kT) / \sum_n (2J_n + 1) \exp(-E_n/kT) ,$$

where k is the Boltzmann constant, T is the temperature, and J_i is the nuclear spin of the i^{th} state. The sum over n goes over those states included in each plot label. Generally, states with excitation energies below 200 keV are included. The spins and energy levels are from the most recent data available from the *Nuclear Data Sheets*¹ or from the *Table of Isotopes*.²

Each of the 81 plots contains, as a function of temperature, the thermal equilibrium total excited state fraction of an actinide isotope. The population of each excited state is also plotted. The actinide isotopes plotted are shown in Fig. 1. A few isotopes are included for which unknown spins were estimated from systematics. These spins are followed by a ? in the plots.

ACKNOWLEDGMENTS

Special thanks go to Dave Madland and Ed Arthur for constructive advice and for encouraging the compilation of these plots and to Richard Hoff for providing spins and energy levels for ²⁵⁰Bk.

REFERENCES

1. M. J. Martin and J. K. Tuli, Eds., *Nuclear Data Sheets* (Academic Press, New York, 1980-1982), Vols. 31-37.
2. C. Michael Lederer and Virginia S. Shirley, Eds., *Table of Isotopes*, 7th Ed., (John Wiley and Sons, New York, 1978).

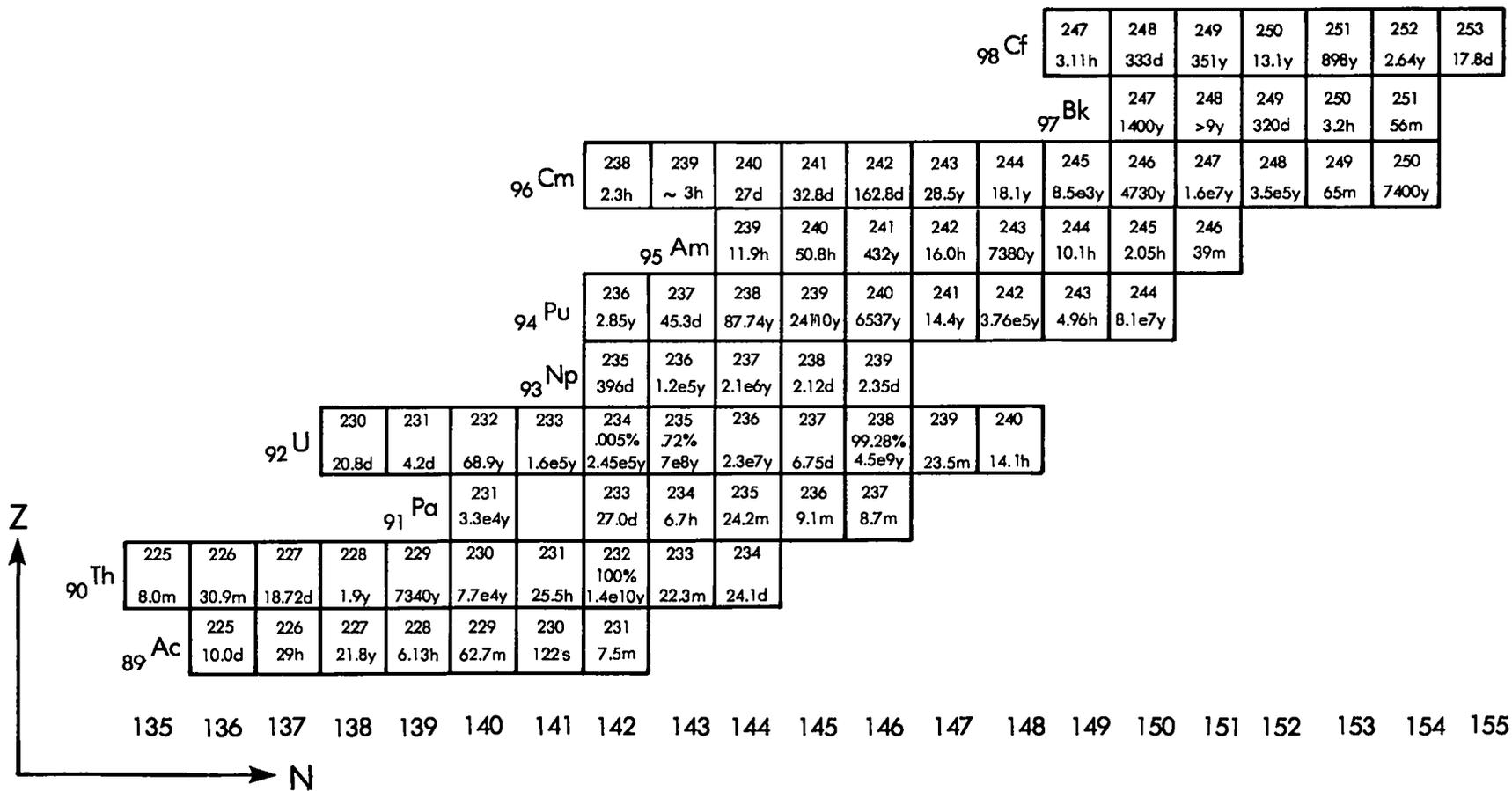
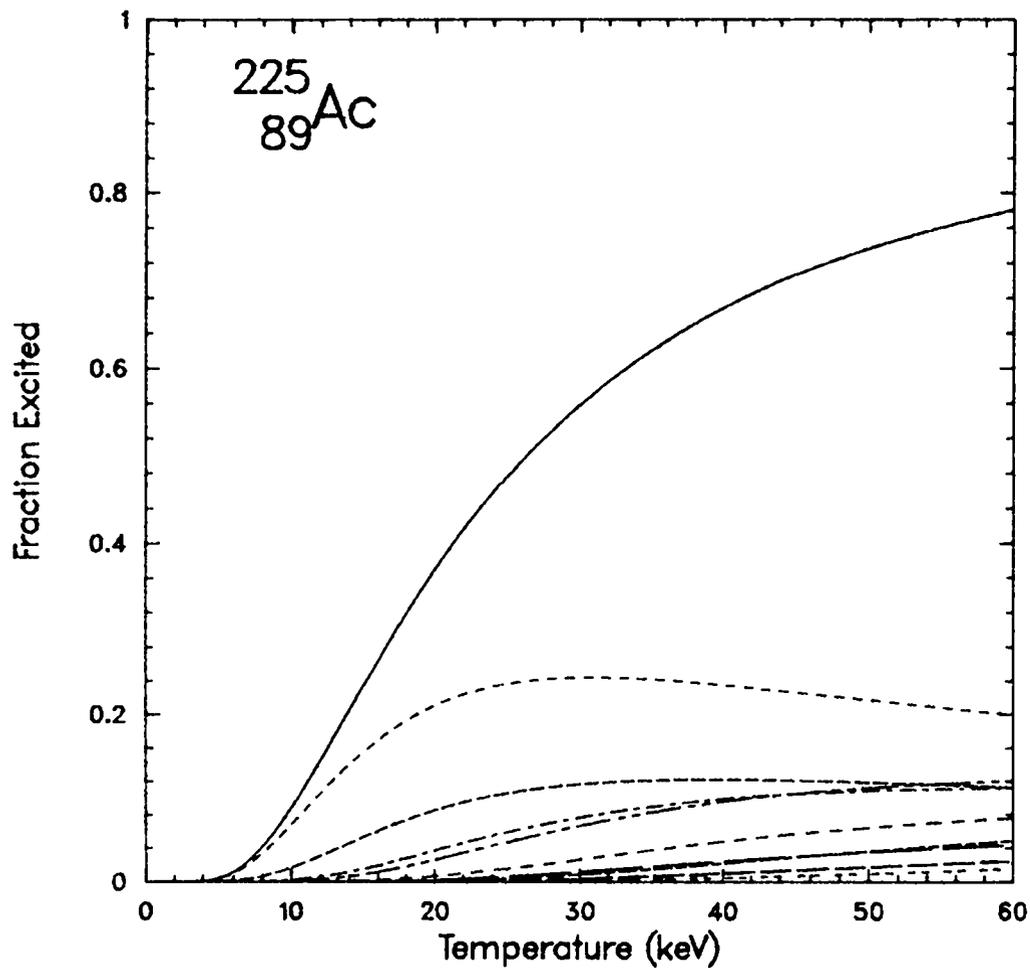
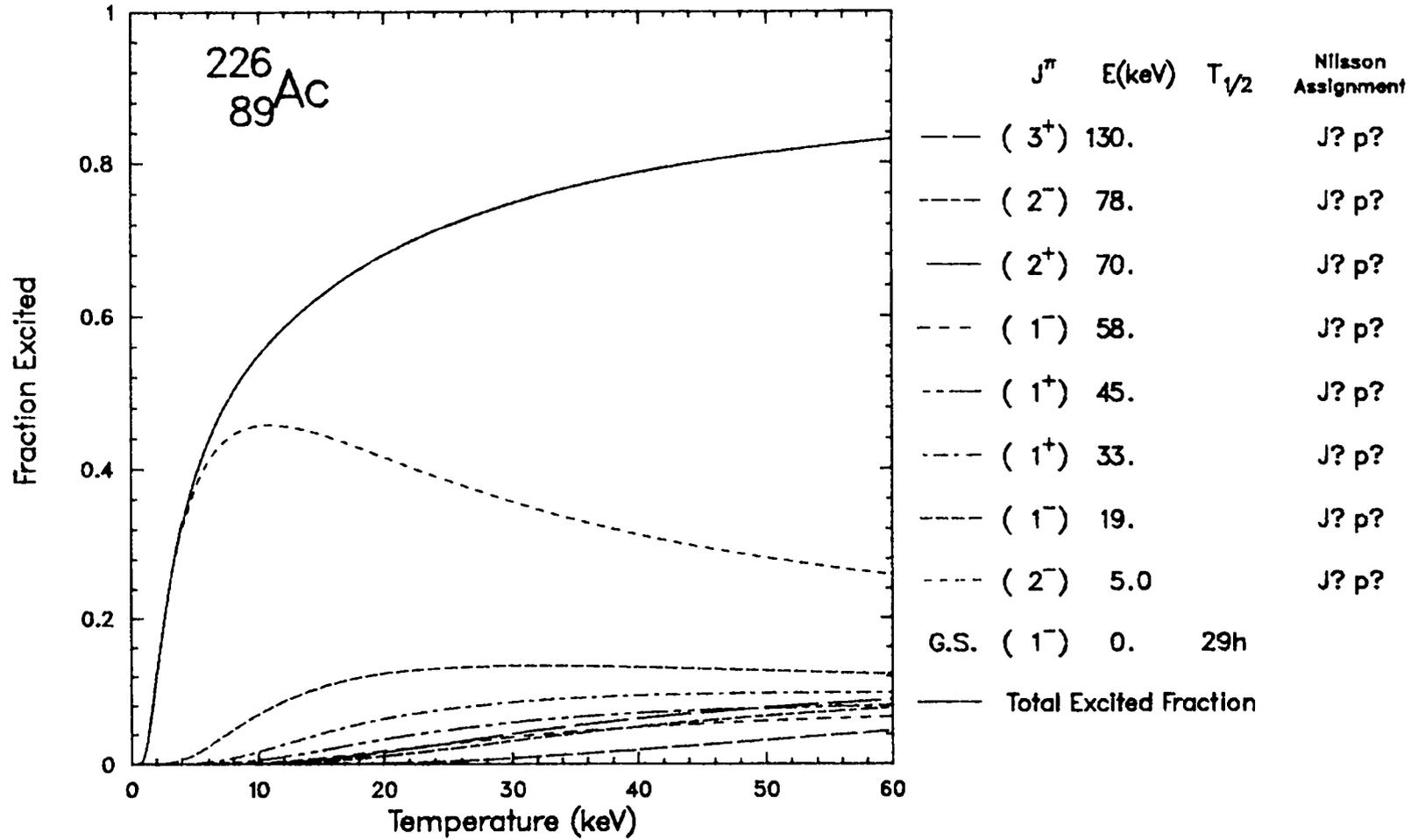
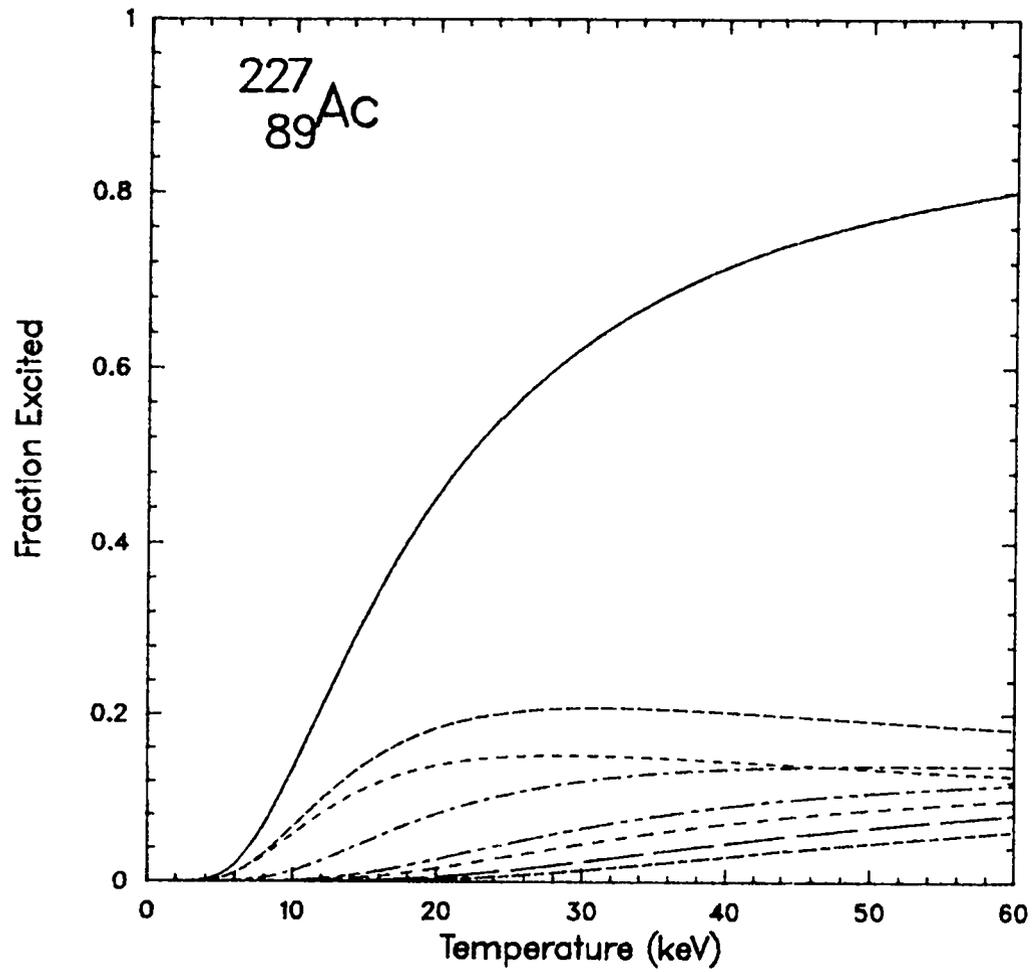


Fig. 1. Actinides.

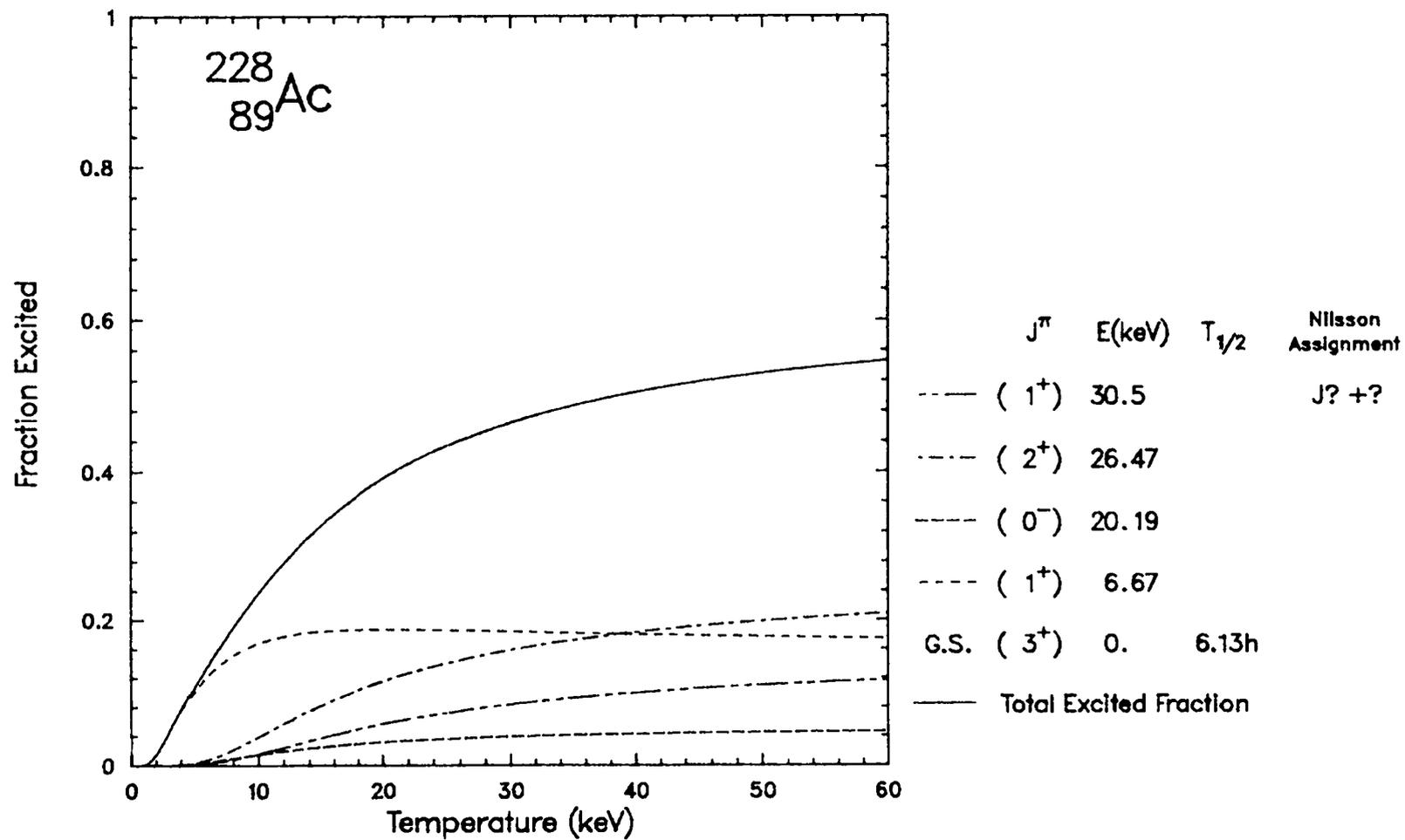


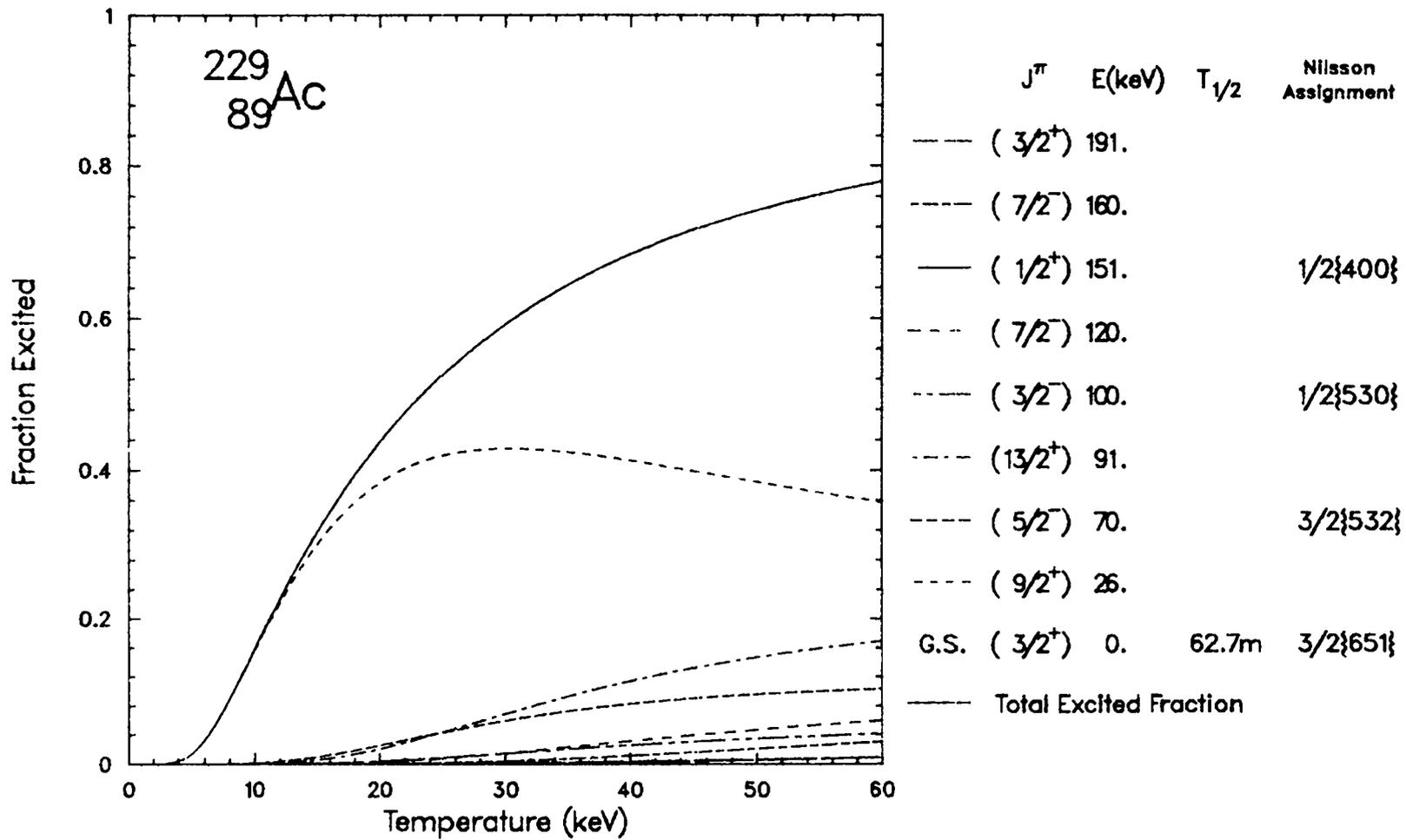
J^π	E(keV)	$T_{1/2}$	Nilsson Assignment
(7/2 ⁺)	199.9		
(7/2 ⁻)	170.6		
(5/2 ⁺)	155.5		5/2{642}
(9/2 ⁺)	145.		J?
(5/2 ⁻)	120.8		5/2{523}
(7/2 ⁺)	105.1		J?
(7/2 ⁻)	77.5		
(5/2 ⁺)	64.7		J? +?
(3/2 ⁺)	40.		3/2{651}
(5/2 ⁻)	30.		
G.S. (3/2 ⁻)	0.	10.0d	3/2{532}
Total Excited Fraction			

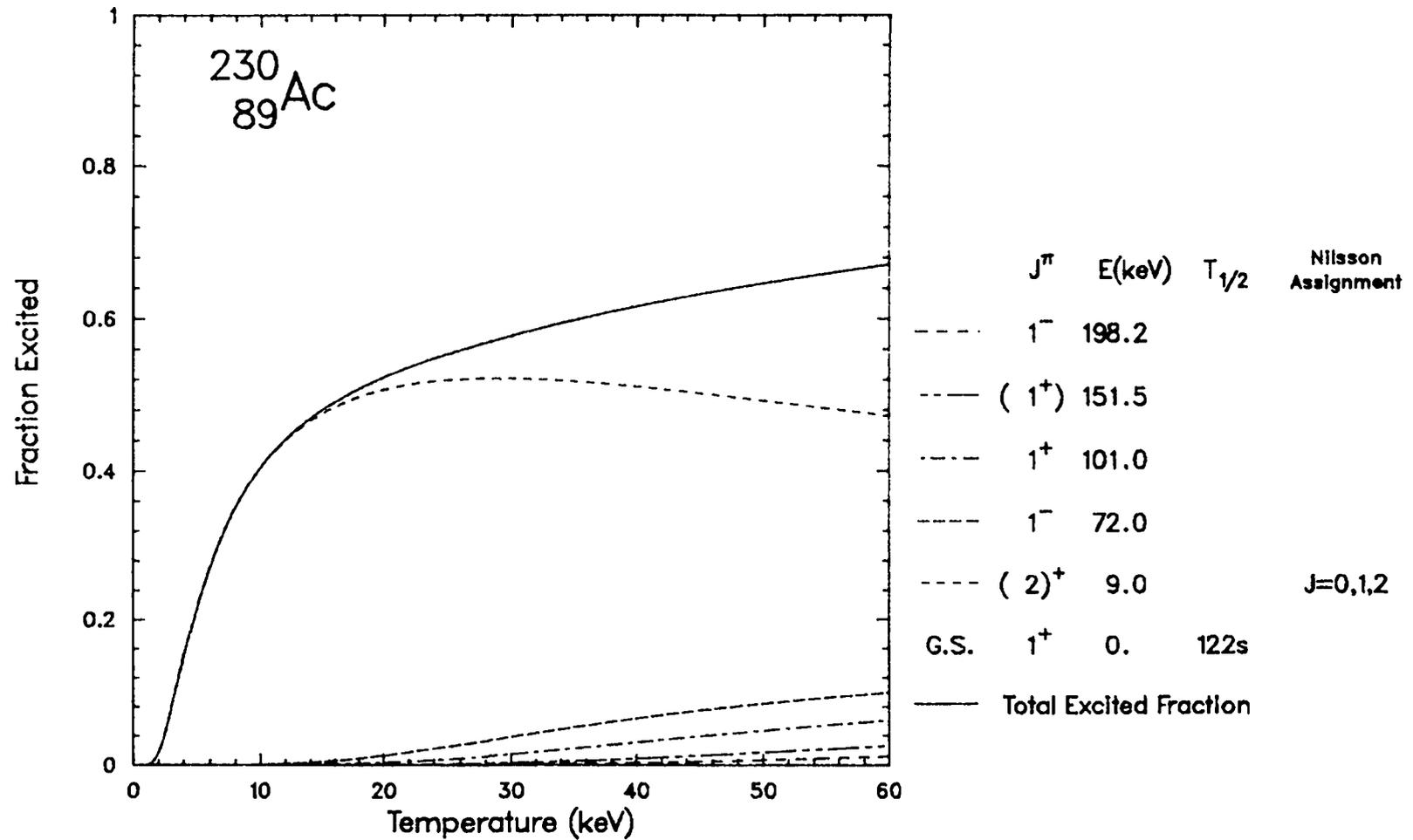


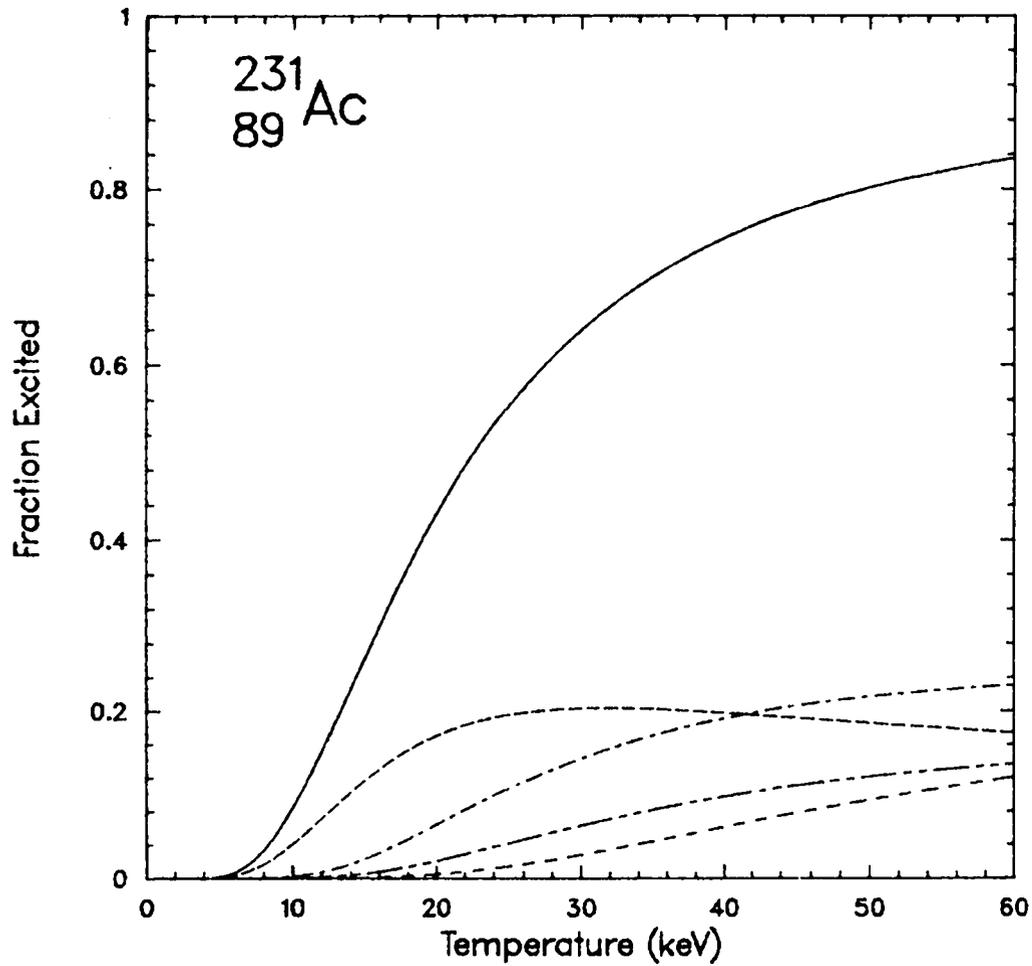


	J^π	E(keV)	$T_{1/2}$	Nilsson Assignment
---	$9/2^-$	126.84		
---	$9/2^+$	110.00		
---	$7/2^+$	84.55		
---	$7/2^-$	74.13		
---	$5/2^+$	46.35		
---	$5/2^-$	29.94		
---	$3/2^+$	27.36		$3/2\{651\}$
G.S.	$3/2^-$	0.	21.8y	$3/2\{532\}$
---	Total Excited Fraction			

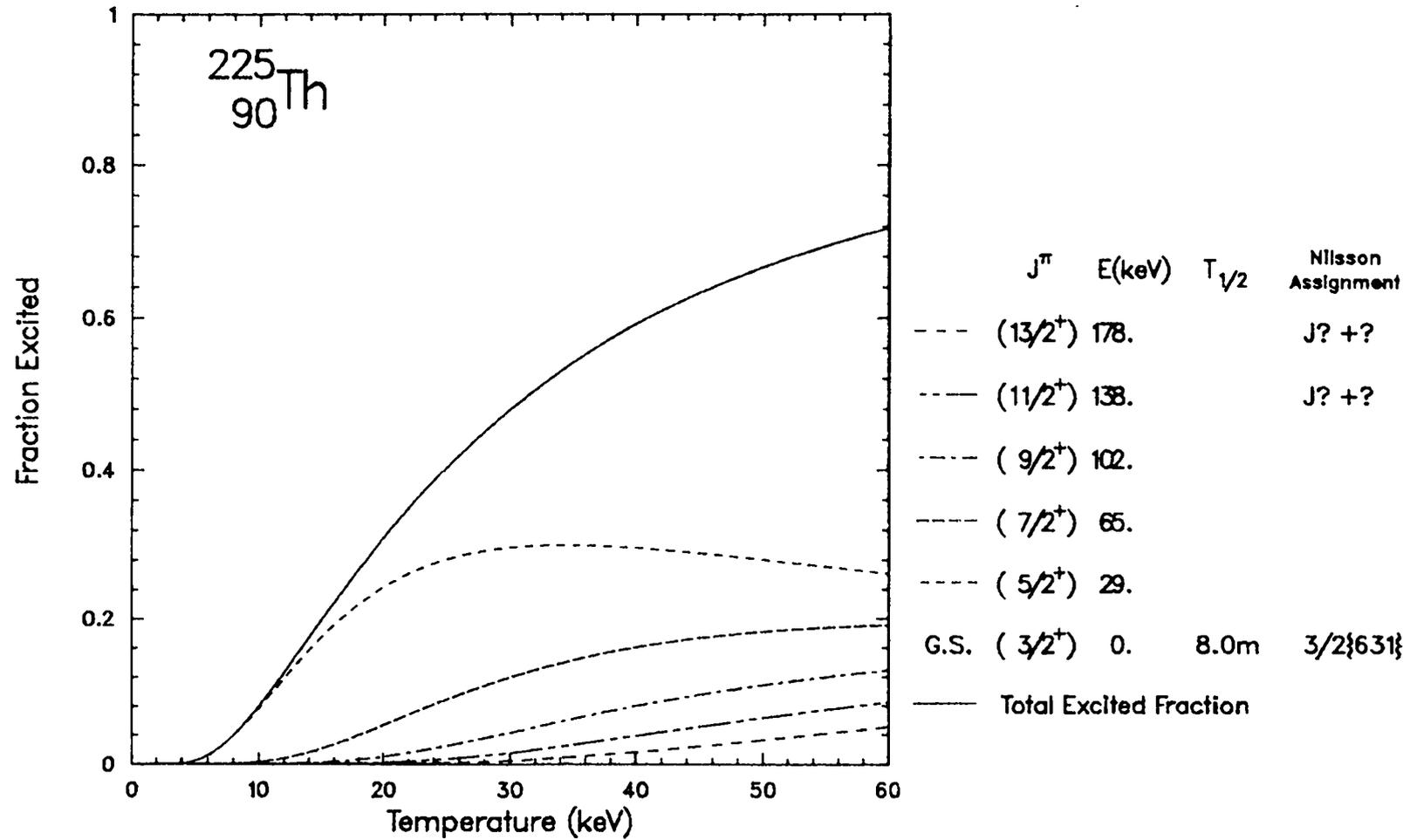


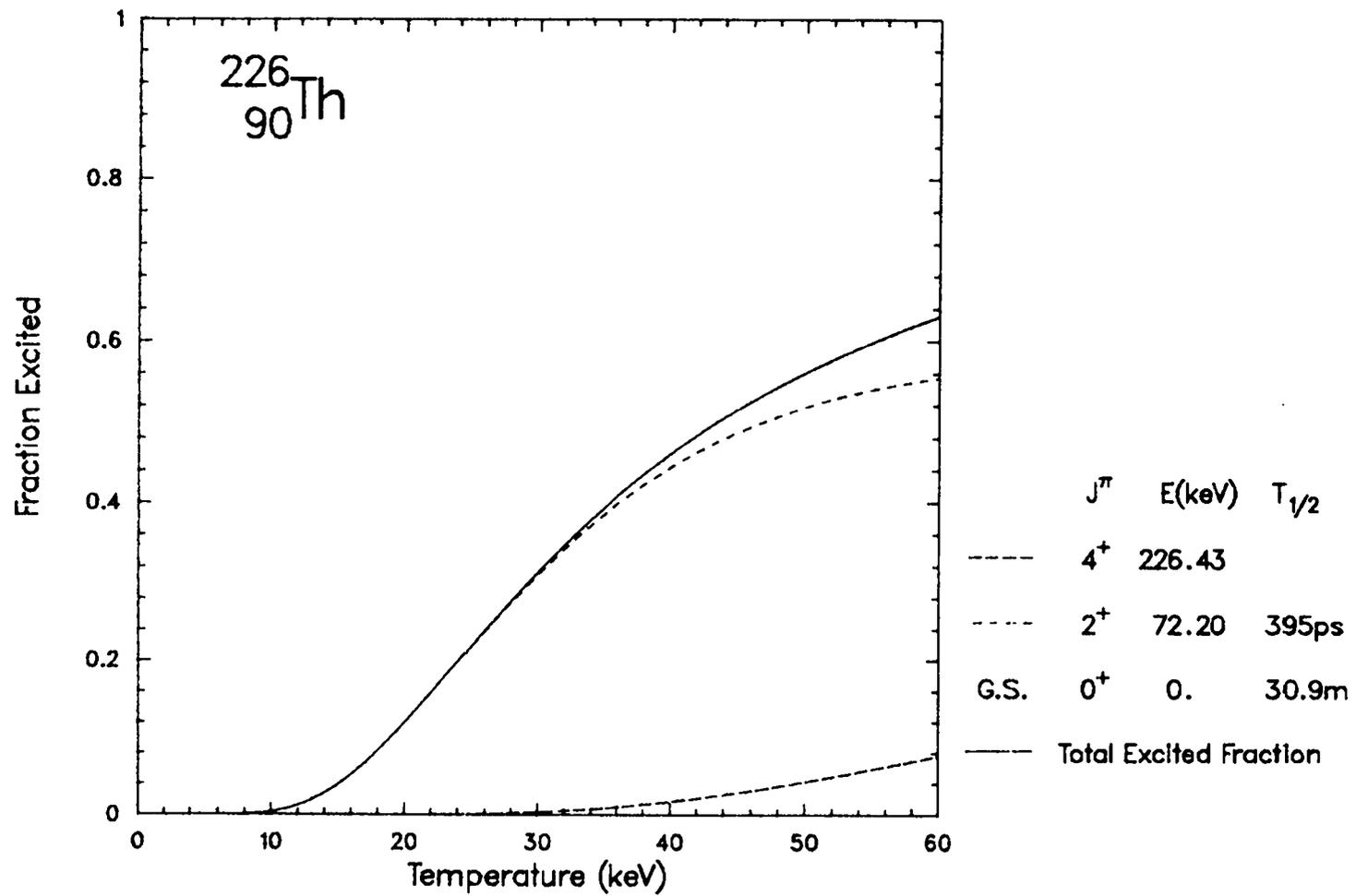


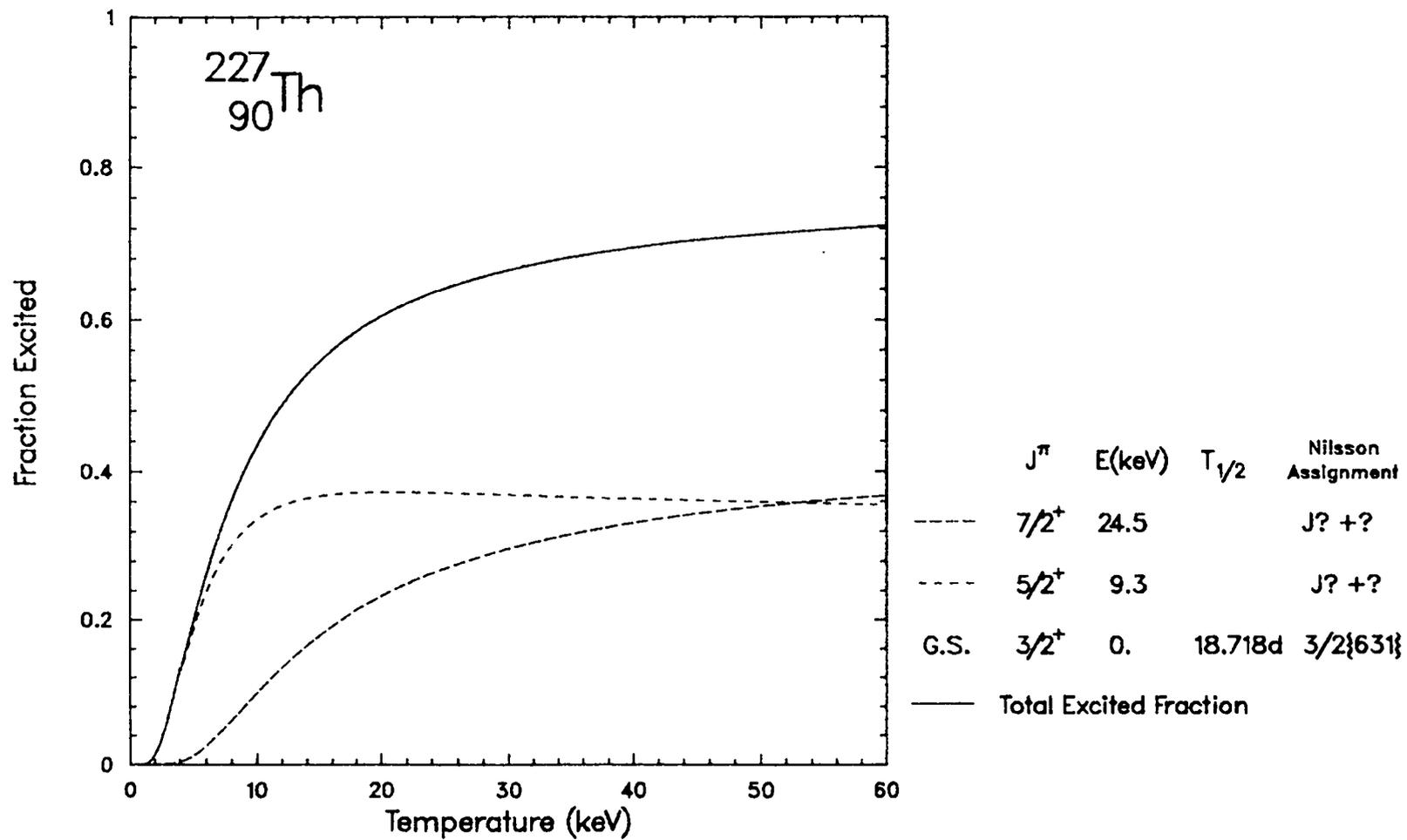


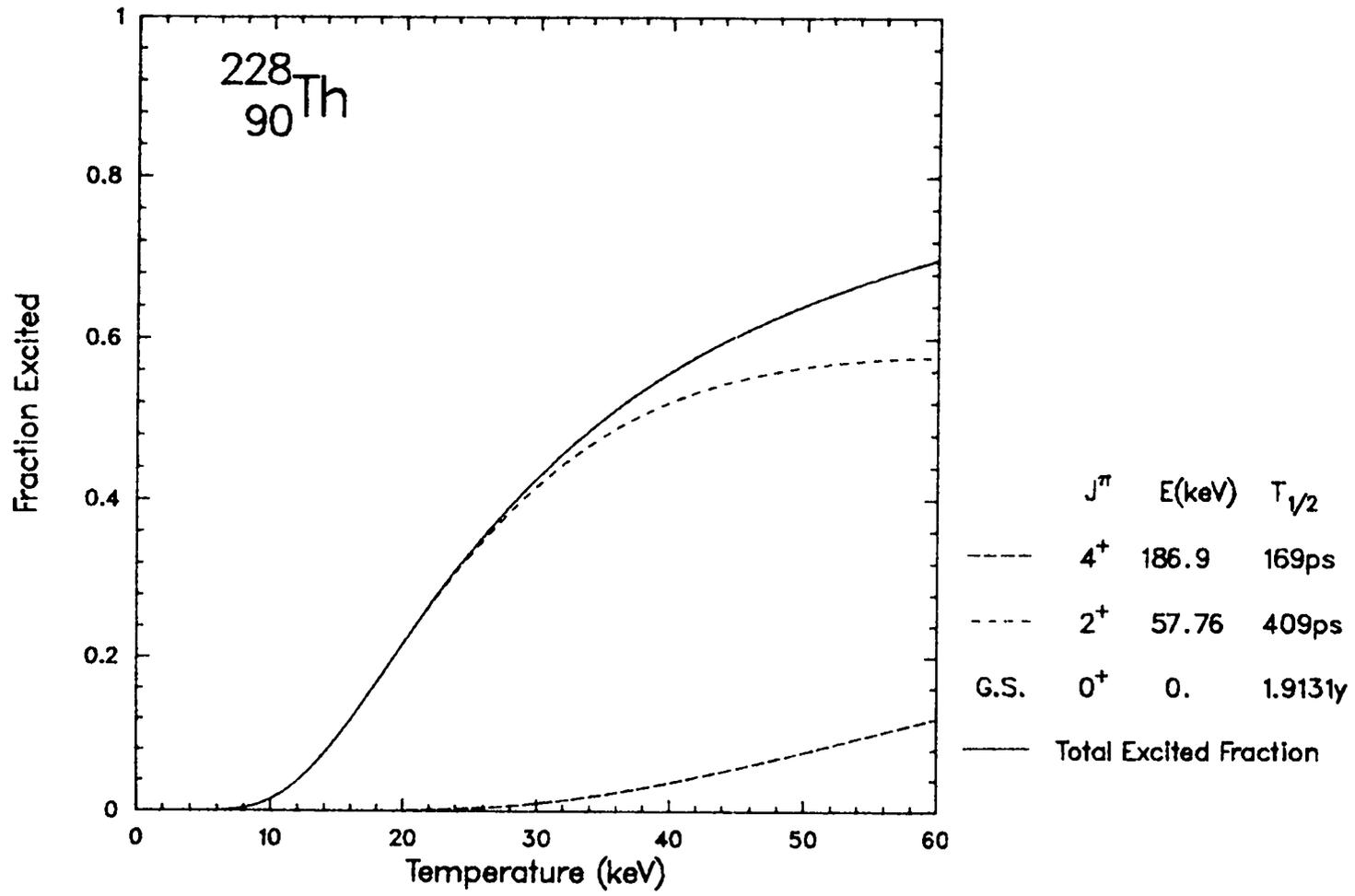


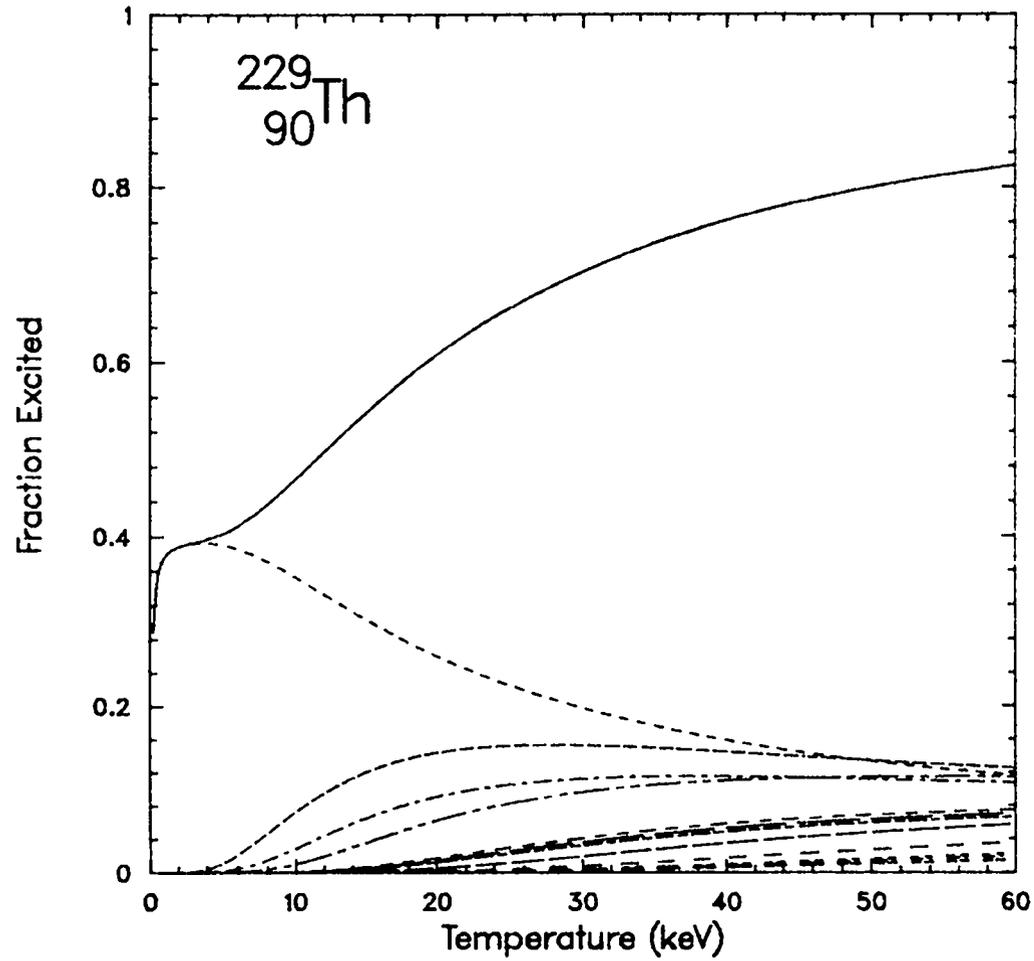
	J^π	E(keV)	$T_{1/2}$	Nilsen Assignment
---	$(13/2^+)$	135.		
---	$(7/2^-)$	94.		
---	$(9/2^+)$	76.		$3/2\{651\}$
---	$(3/2^-)$	38.		$1/2\{530\}$
---	$(3/2^+)$	38.		
---	G.S. $(1/2^+)$	0.	7.5m	$1/2\{400\}$
—	Total Excited Fraction			



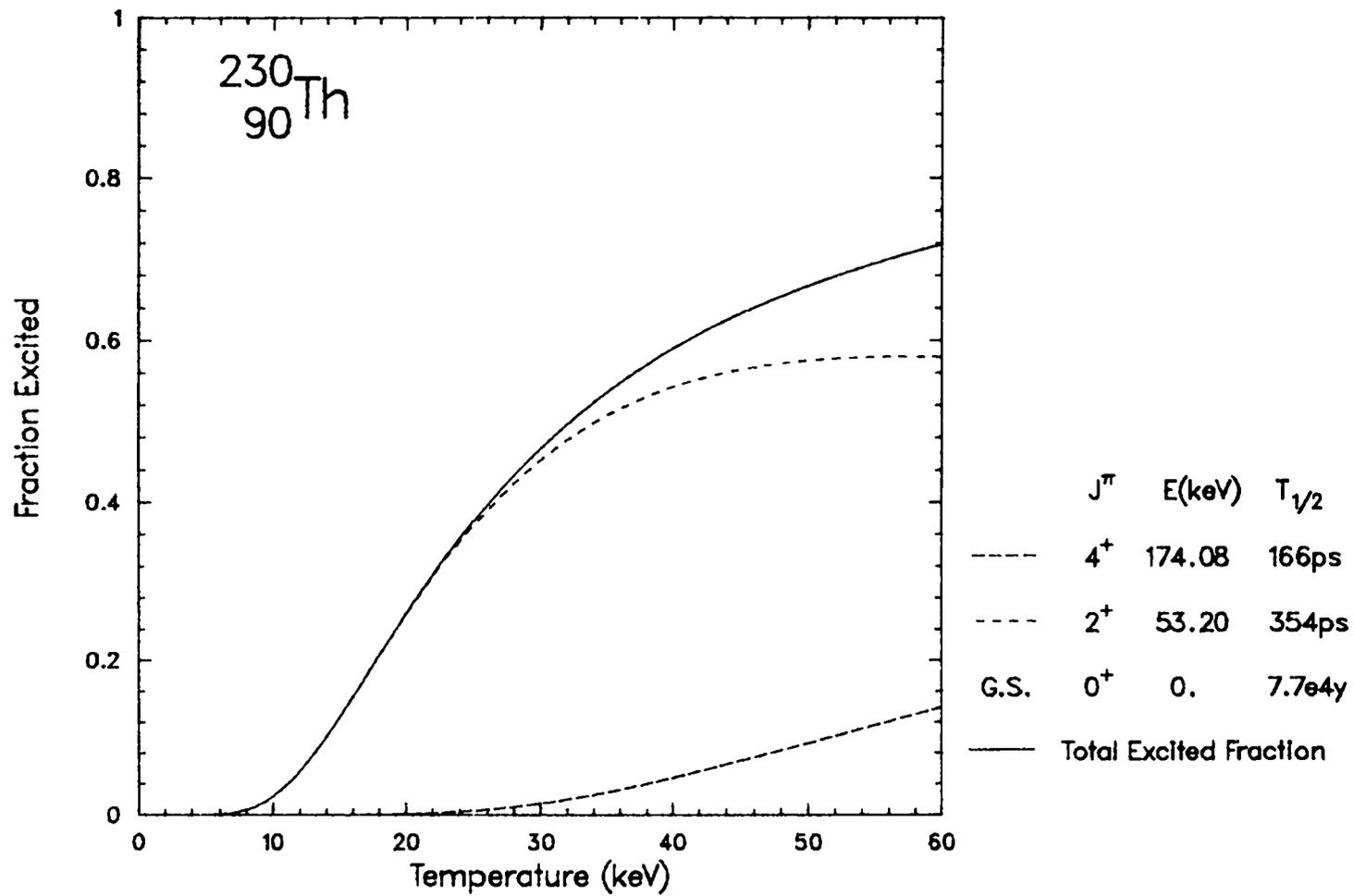


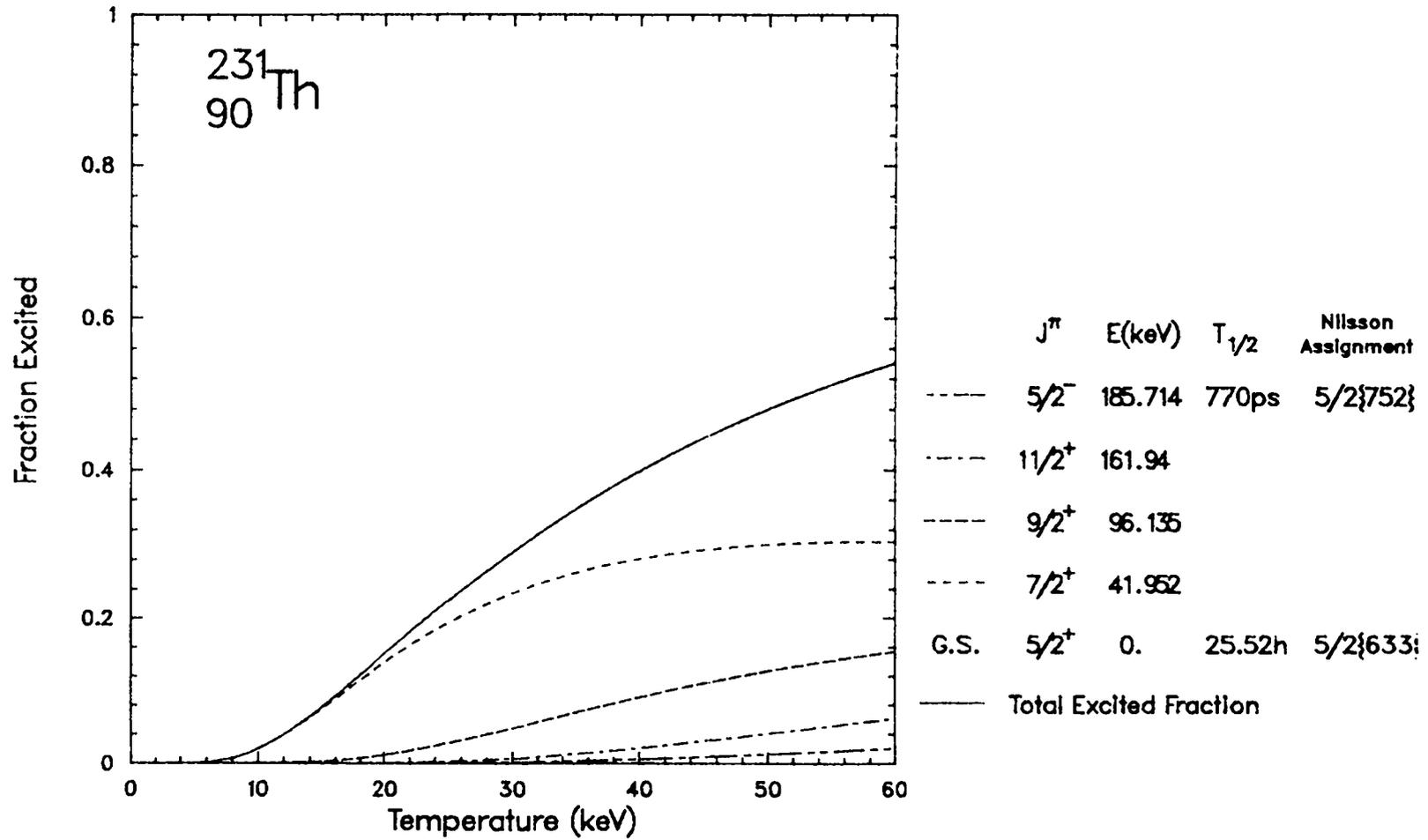


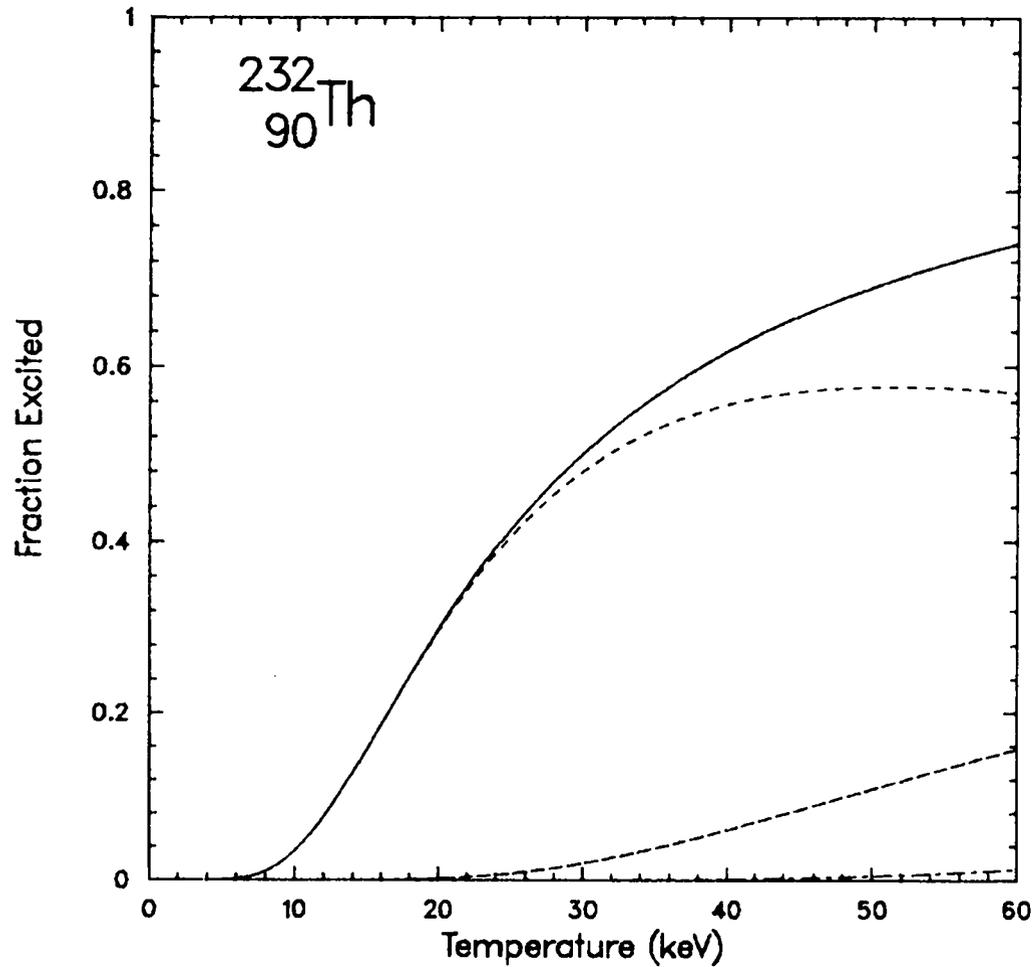




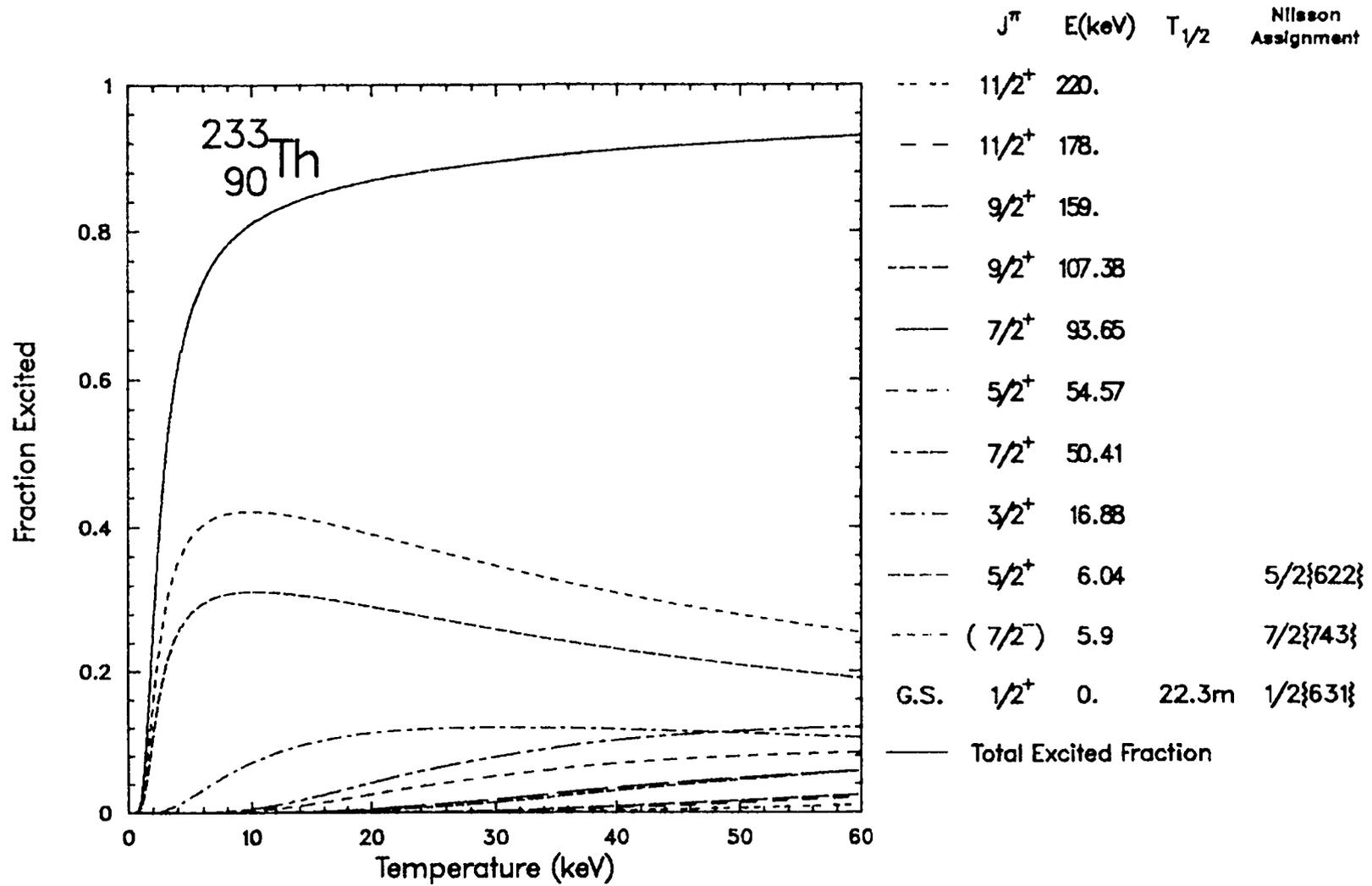
J^π	E(keV)	$T_{1/2}$	Nilsson Assignment
(7/2 ⁻)	148.16		
(5/2 ⁻)	146.36		5/2{752}
(7/2 ⁺)	140.		J? +?
(9/2 ⁺)	125.4		
9/2 ⁺	97.13	147ps	
(7/2 ⁺)	75.		
(7/2 ⁺)	71.82		
7/2 ⁻	68.		J? +?
7/2 ⁺	42.44	172ps	
(5/2 ⁺)	29.2		
5/2 ⁻	20.		J? +?
(3/2 ⁺)	.1		3/2{631}
G.S.	5/2 ⁺	0.	7340y 5/2{633}
Total Excited Fraction			

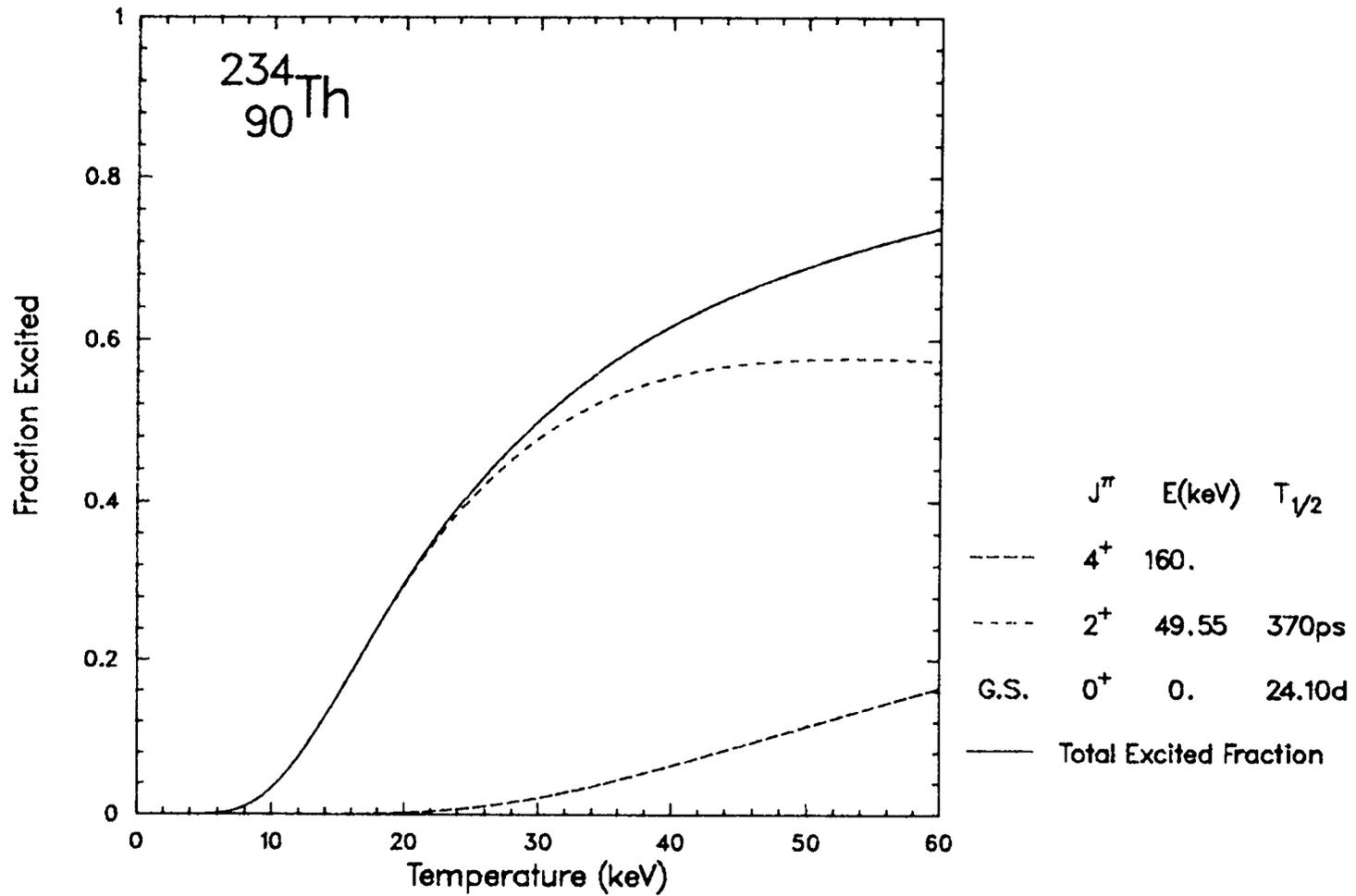


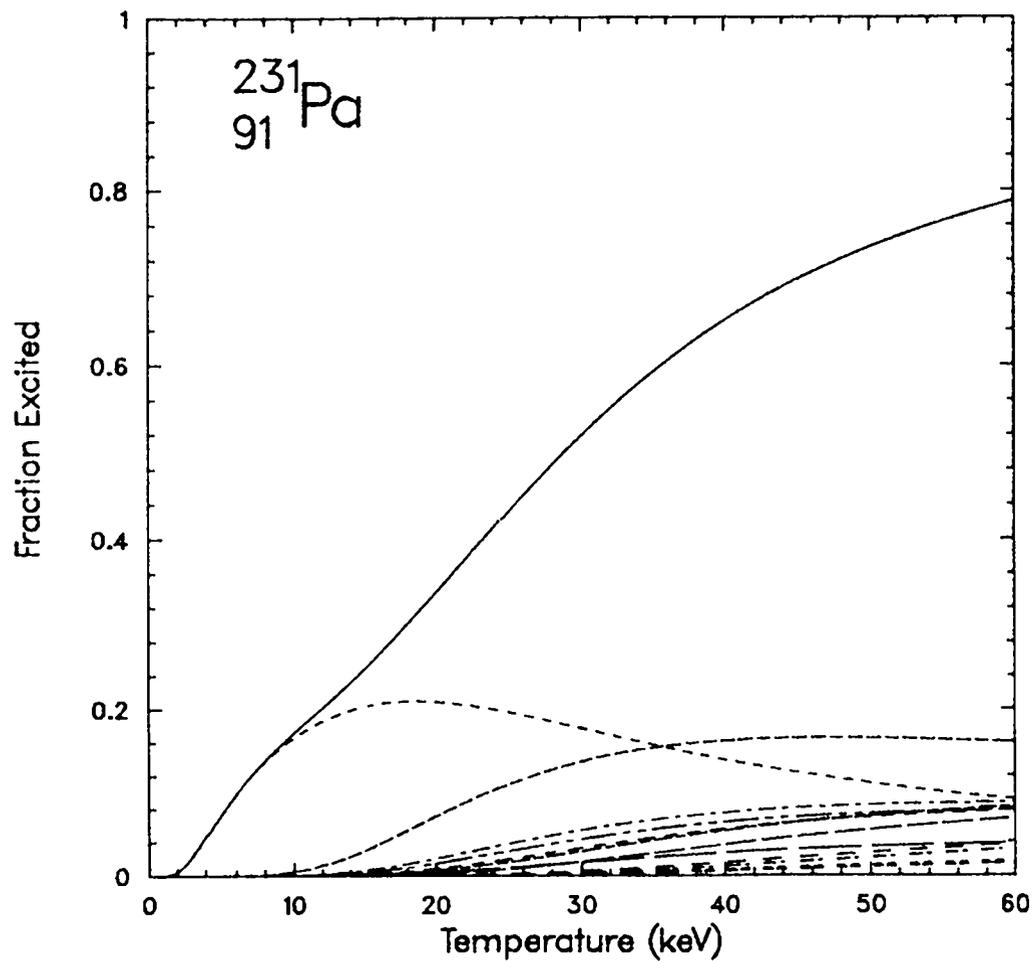




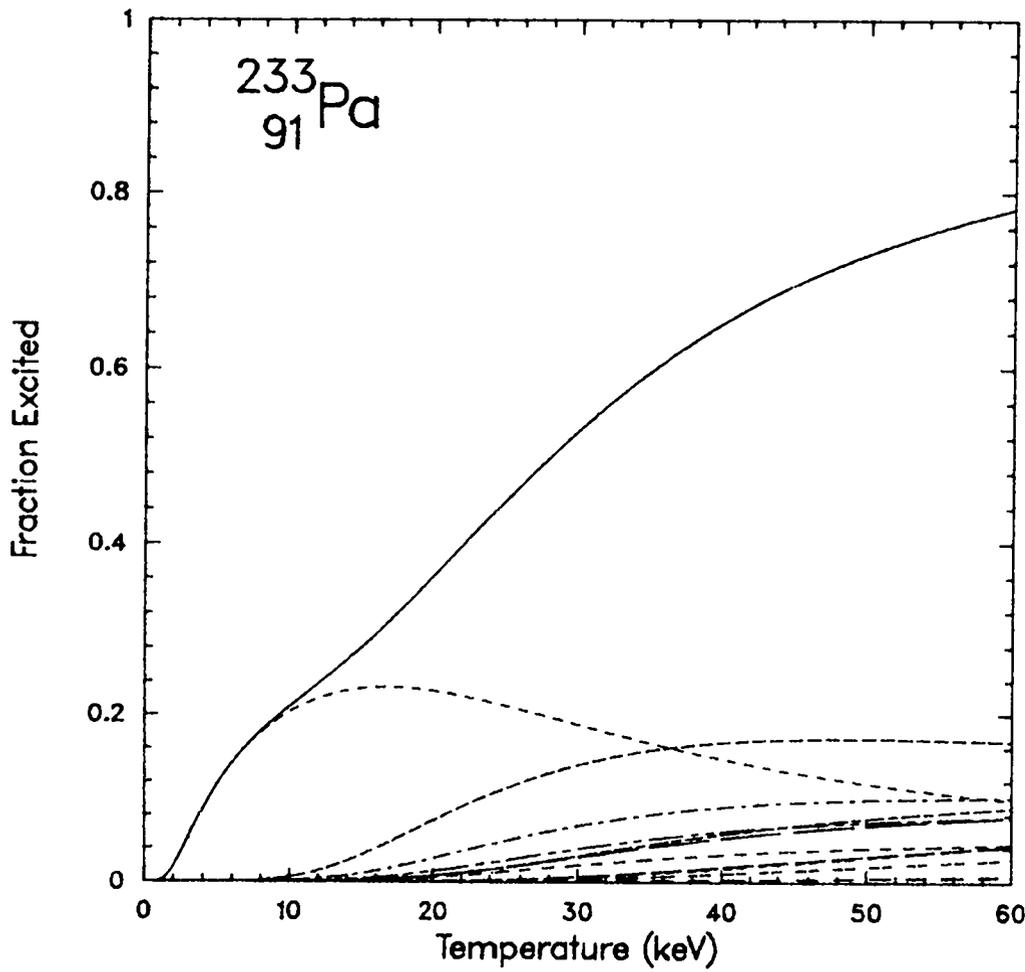
Natural Abundance = 100. %



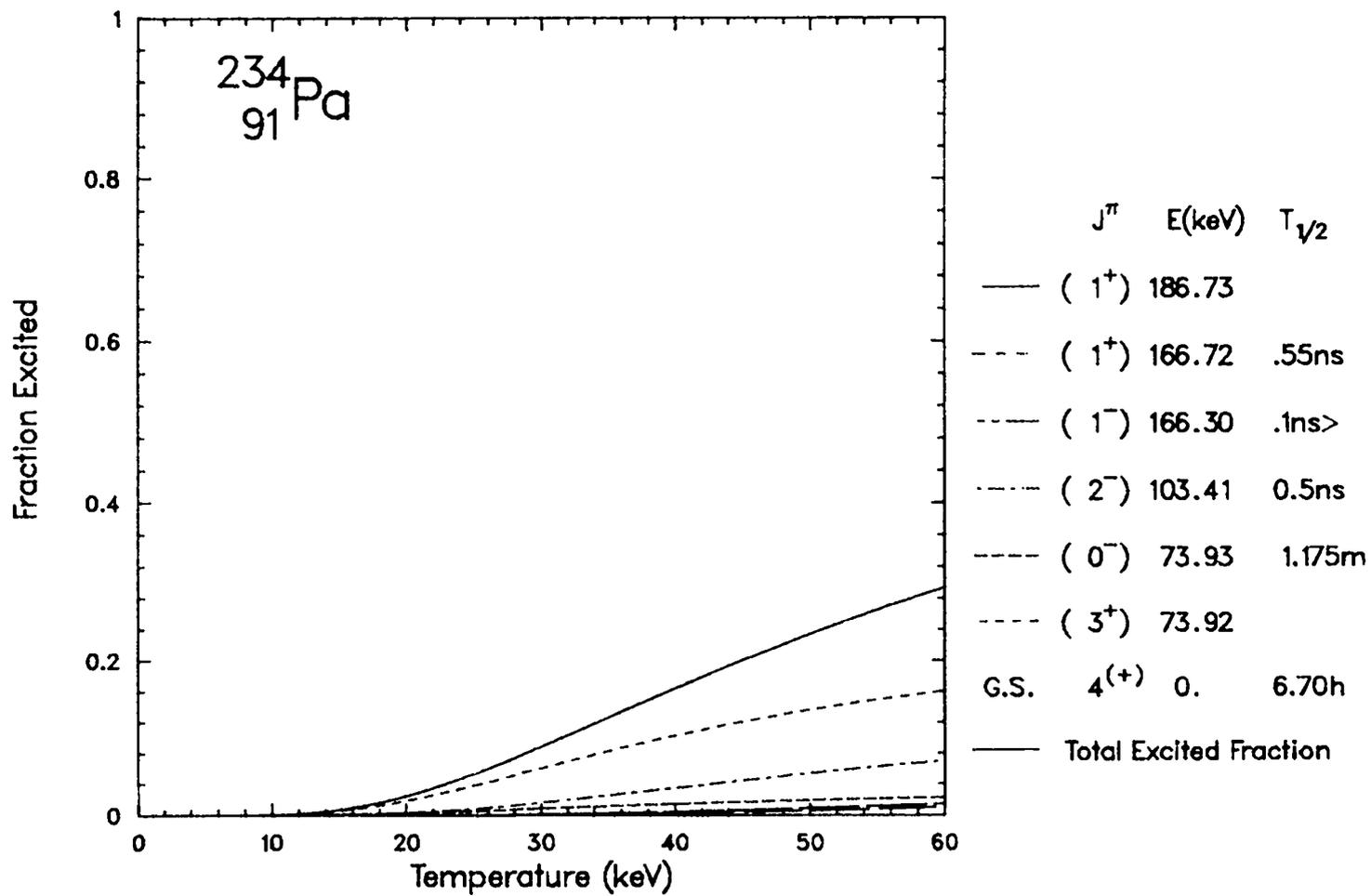


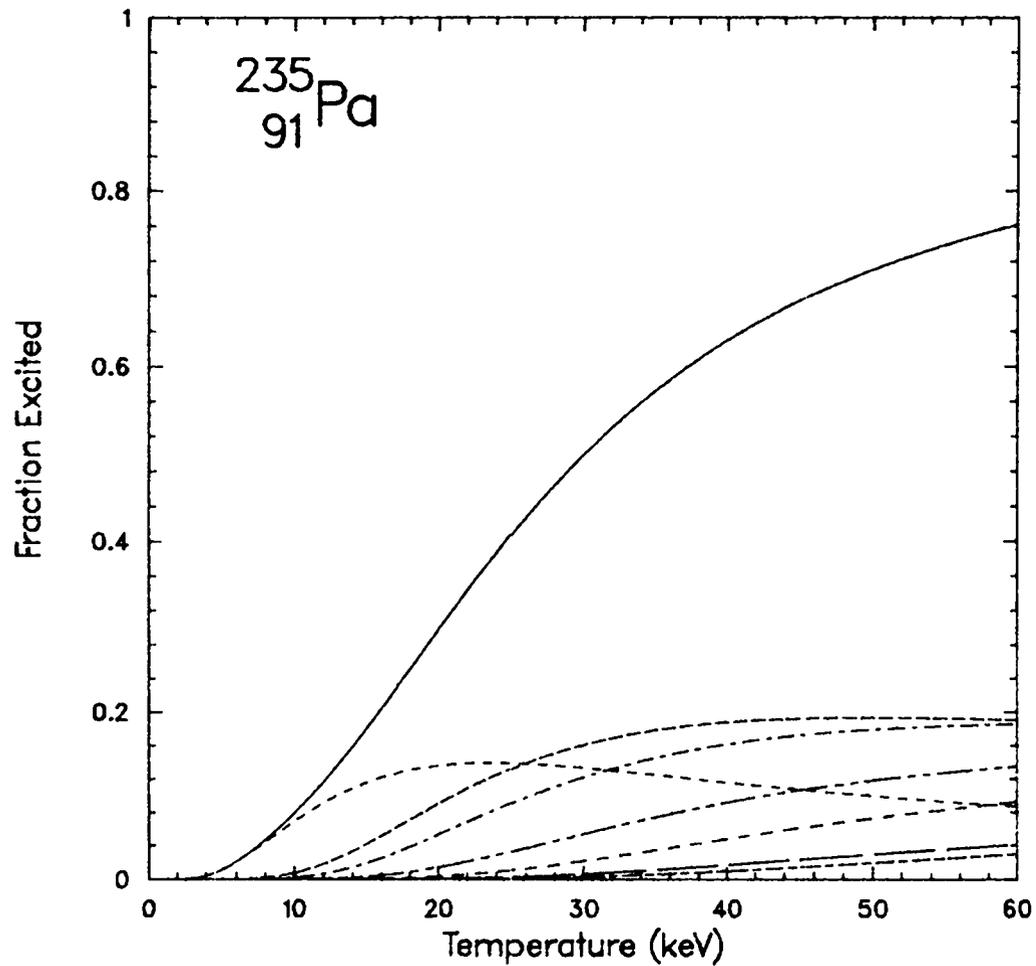


	J^π	E(keV)	$T_{1/2}$	Nilsson Assignment
--- --	$(13/2^+)$	189.		
-- --	$5/2^+$	183.494		$5/2\{642\}$
--- --	$5/2^-$	174.166		$5/2\{523\}$
-- --	$(11/2^-)$	169.3		
--- --	$(11/2^+)$	134.		
--- --	$(9/2^+)$	111.64		
--- --	$3/2^+$	102.259		
--- --	$7/2^+$	101.393		
--- --	$5/2^+$	84.208	45.1ns	$3/2\{651\}$
--- --	$5/2^-$	77.69		
--- --	$7/2^-$	58.564	274ps	
--- --	$1/2^-$	9.20		
G.S.	$3/2^-$	0.	$3.28e4y$	$1/2\{530\}$
---	Total Excited Fraction			

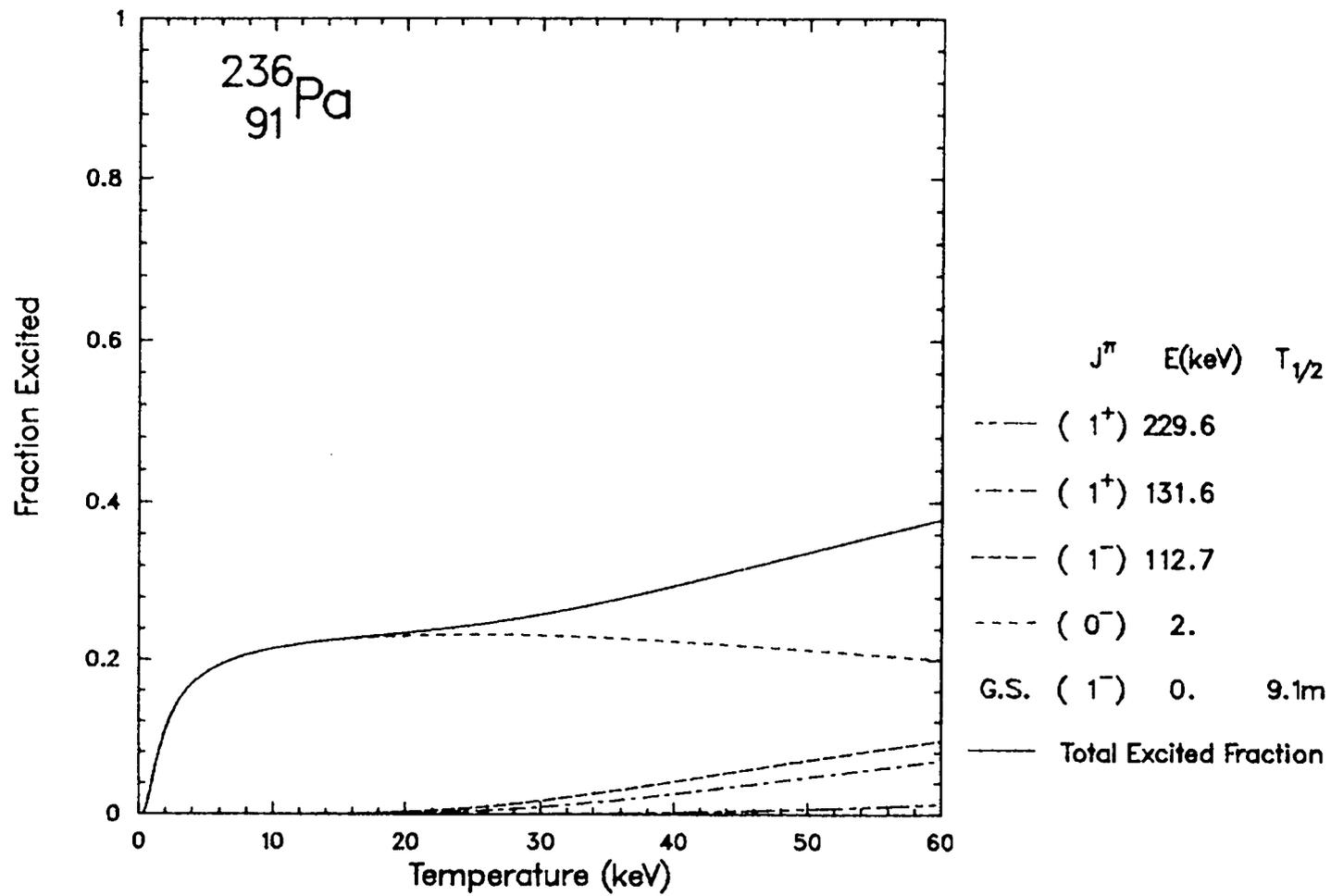


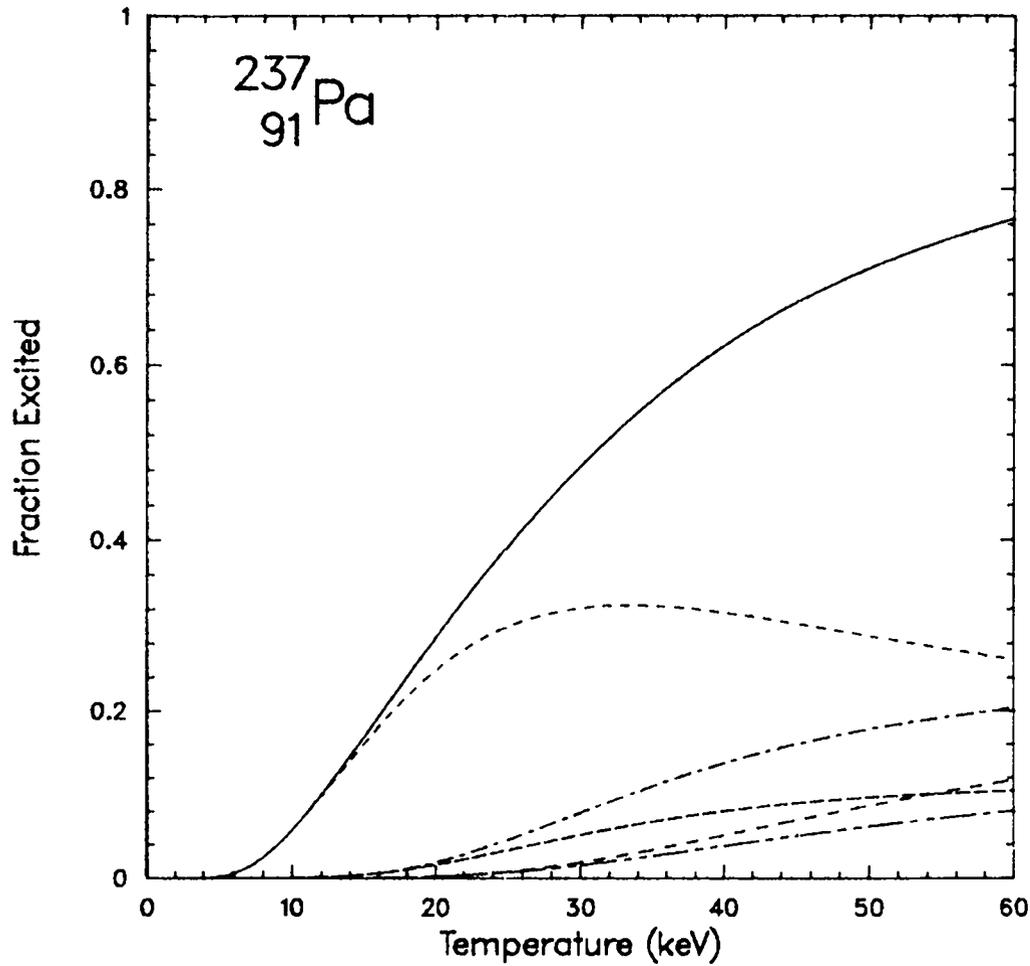
	J^π	E(keV)	$T_{1/2}$	Nilsson Assignment
---	$3/2^+$	201.7		
---	$9/2^-$	179.4		
---	$(13/2^+)$	173.		
---	$(1/2^+)$	169.15		$1/2\{400\}$
---	$(11/2^-)$	163.27		
---	$9/2^+$	109.10		
---	$7/2^+$	103.8		
---	$3/2^+$	94.7		
---	$5/2^+$	86.5	35.7ns	$3/2\{651\}$
---	$5/2^-$	70.6		
---	$7/2^-$	57.15		
---	$1/2^-$	6.65		
G.S.	$3/2^-$	0.	27.0d	$1/2\{530\}$
---	Total Excited Fraction			



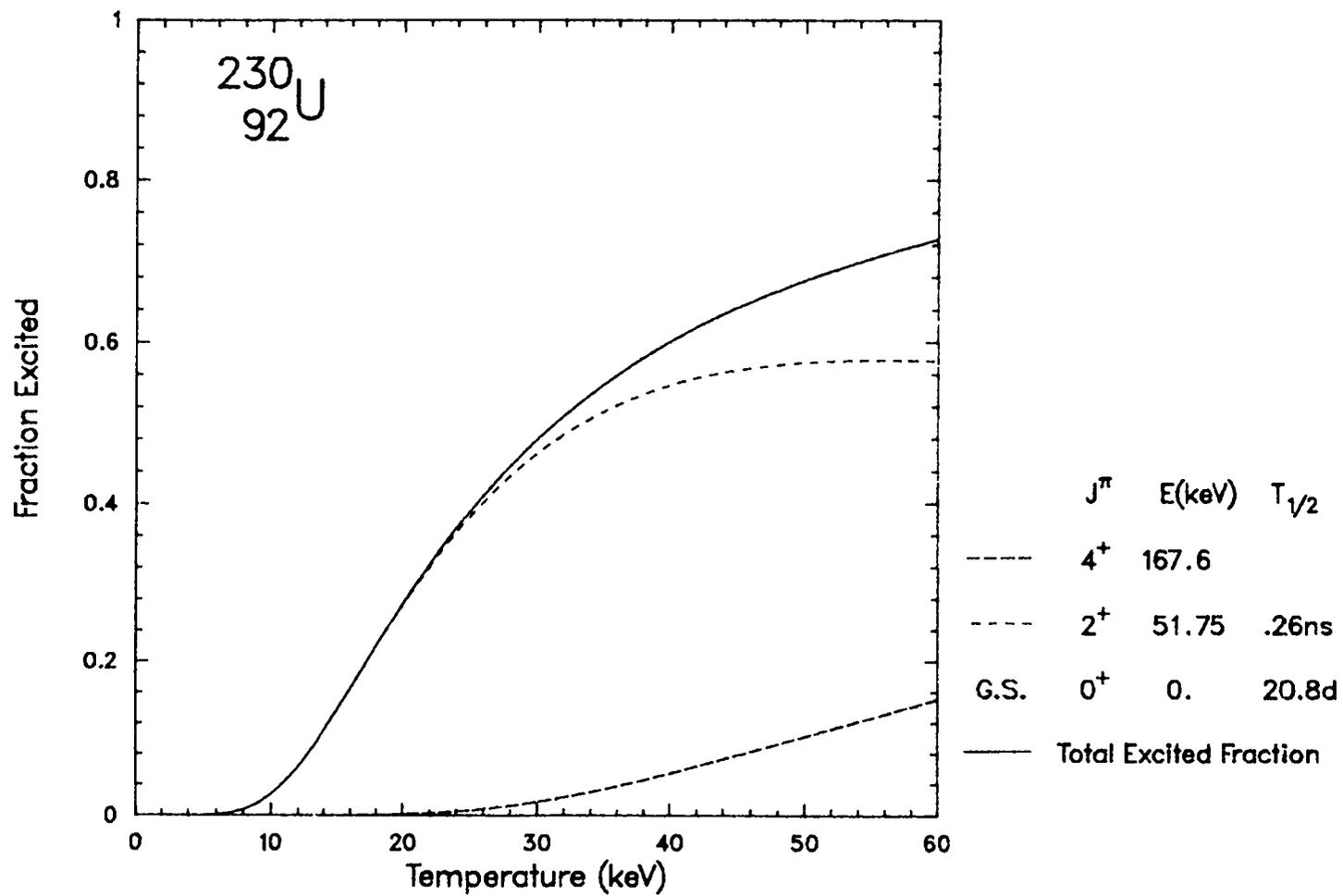


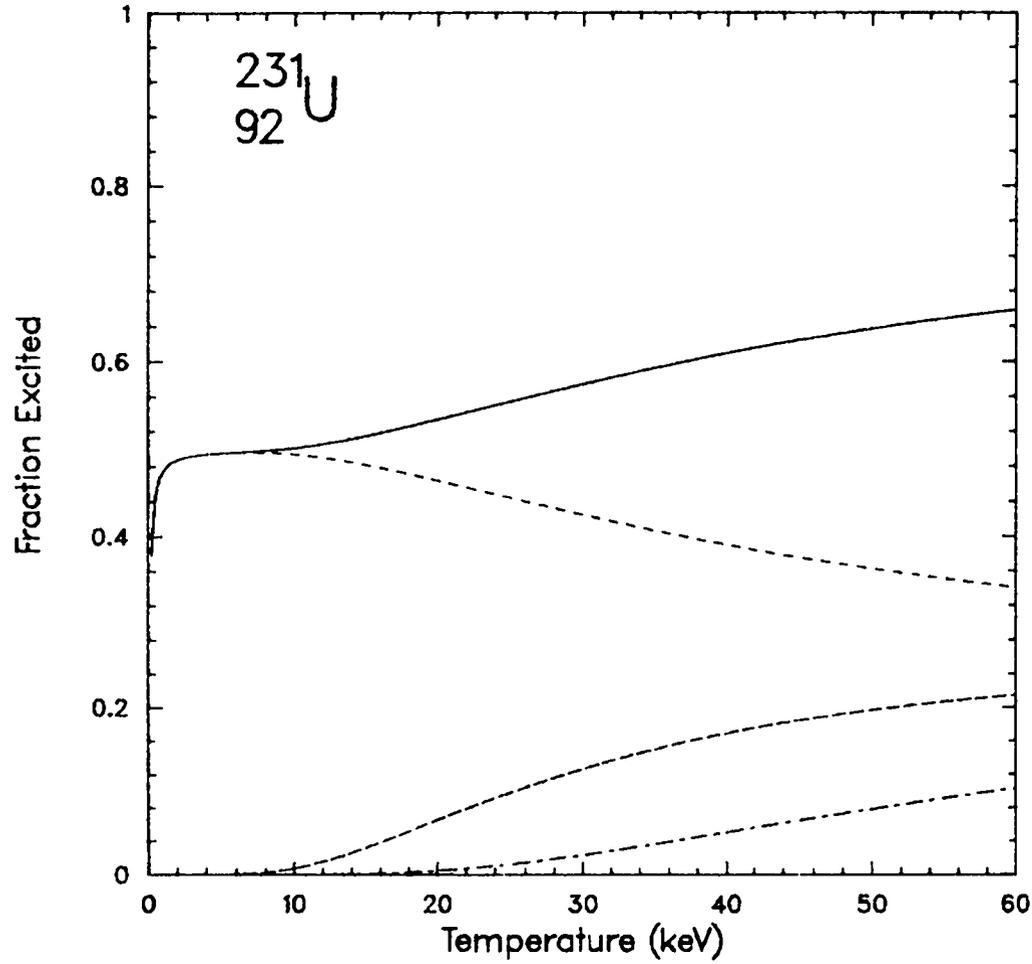
J^π	E(keV)	$T_{1/2}$	Nilsson Assignment
(11/2 ⁻)	190.		J? +?
(9/2 ⁻)	160.		J? +?
(13/2 ⁺)	132.		J? +?
(11/2 ⁺)	100.		J? +?
(9/2 ⁺)	70.		3/2{651}
(7/2 ⁻)	55.		
(1/2 ⁺)	19.		1/2{400}
G.S. (3/2 ⁻)	0.	24.2m	1/2{530}
— Total Excited Fraction			

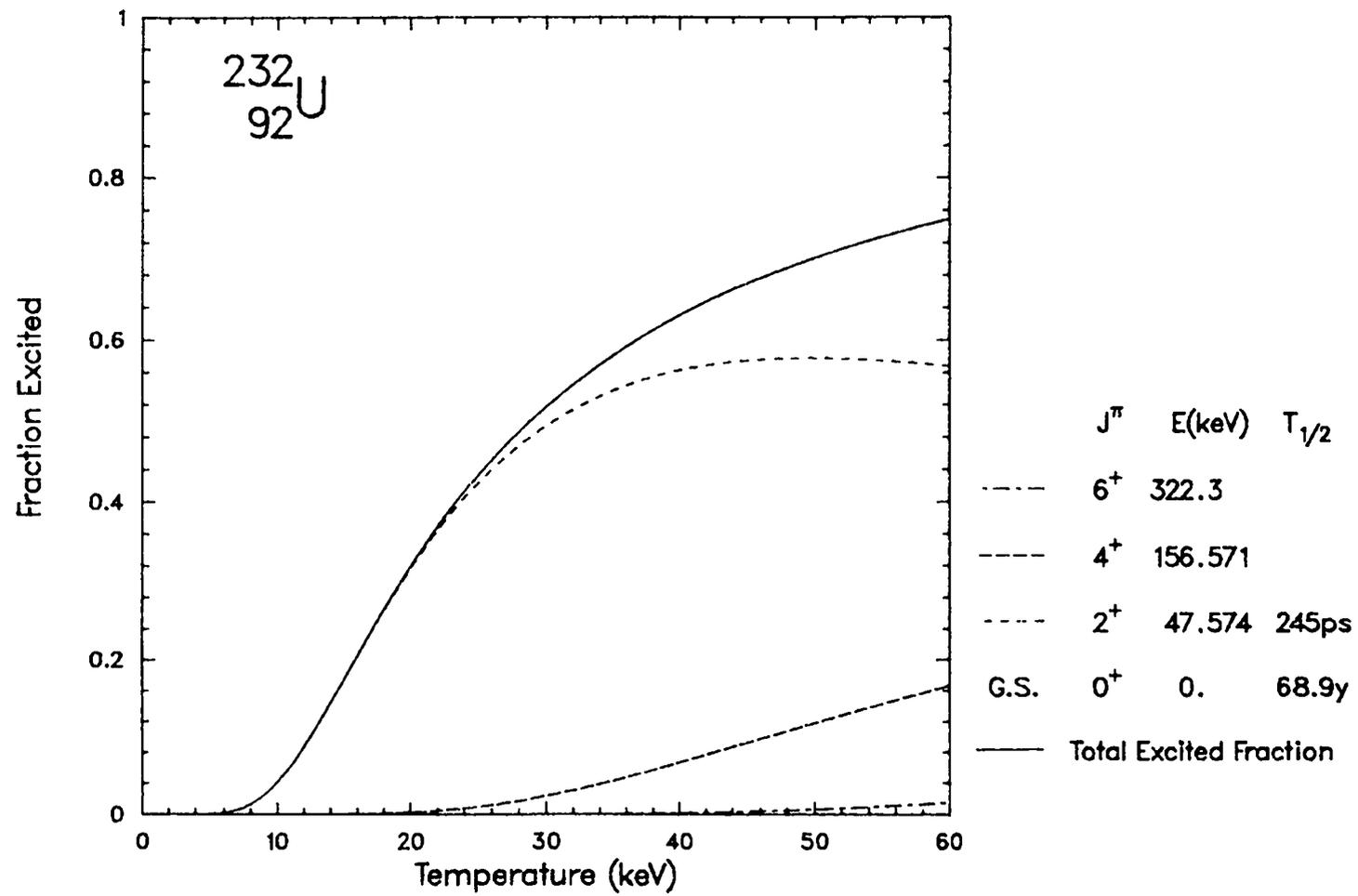


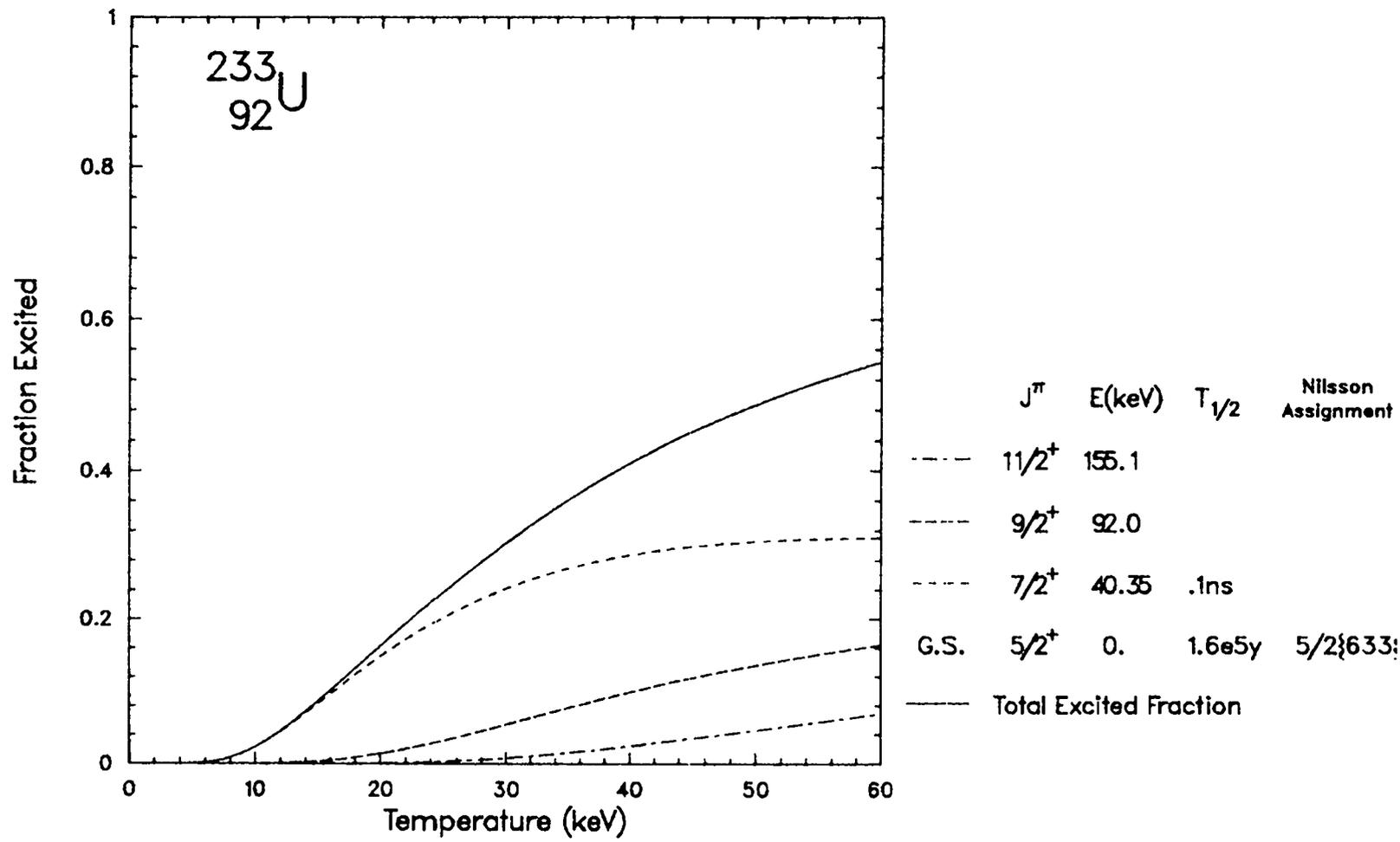


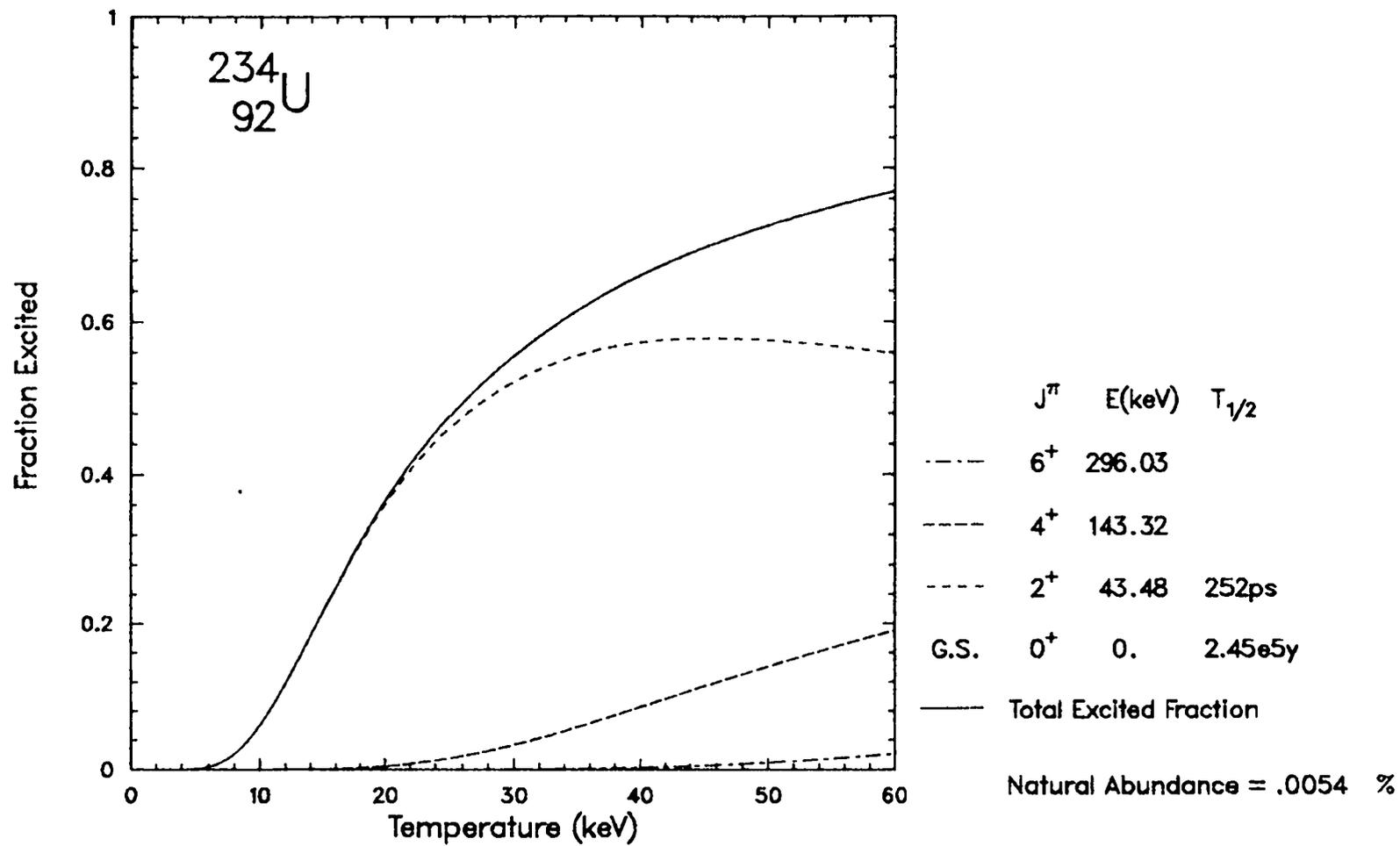
	J^π	E(keV)	$T_{1/2}$	Nilsson Assignment
---	$(13/2^+)$	158.		
---	$(7/2^-)$	147.		
---	$(9/2^+)$	105.		$3/2\{651\}$
---	$(3/2^-)$	90.		$1/2\{530\}$
---	$(3/2^+)$	35.		
G.S.	$(1/2^+)$	0.	8.7m	$1/2\{400\}$
—	Total Excited Fraction			

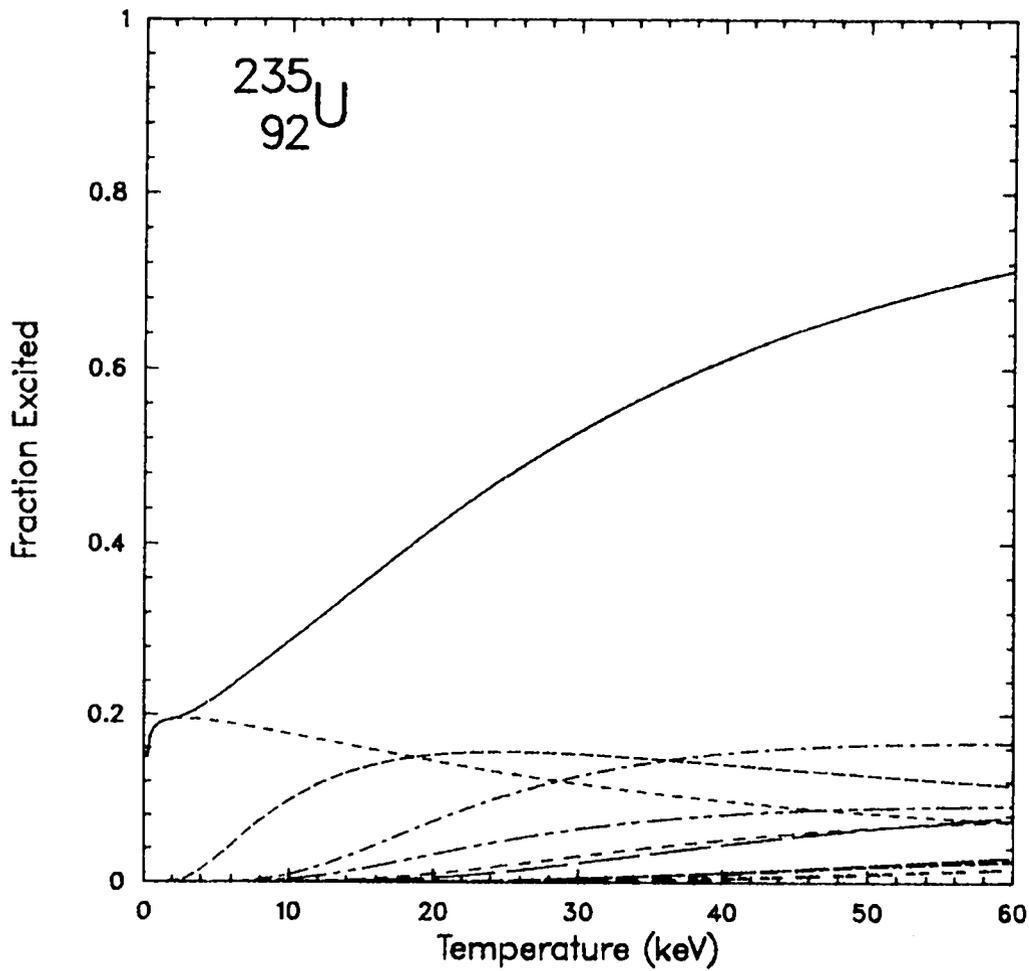






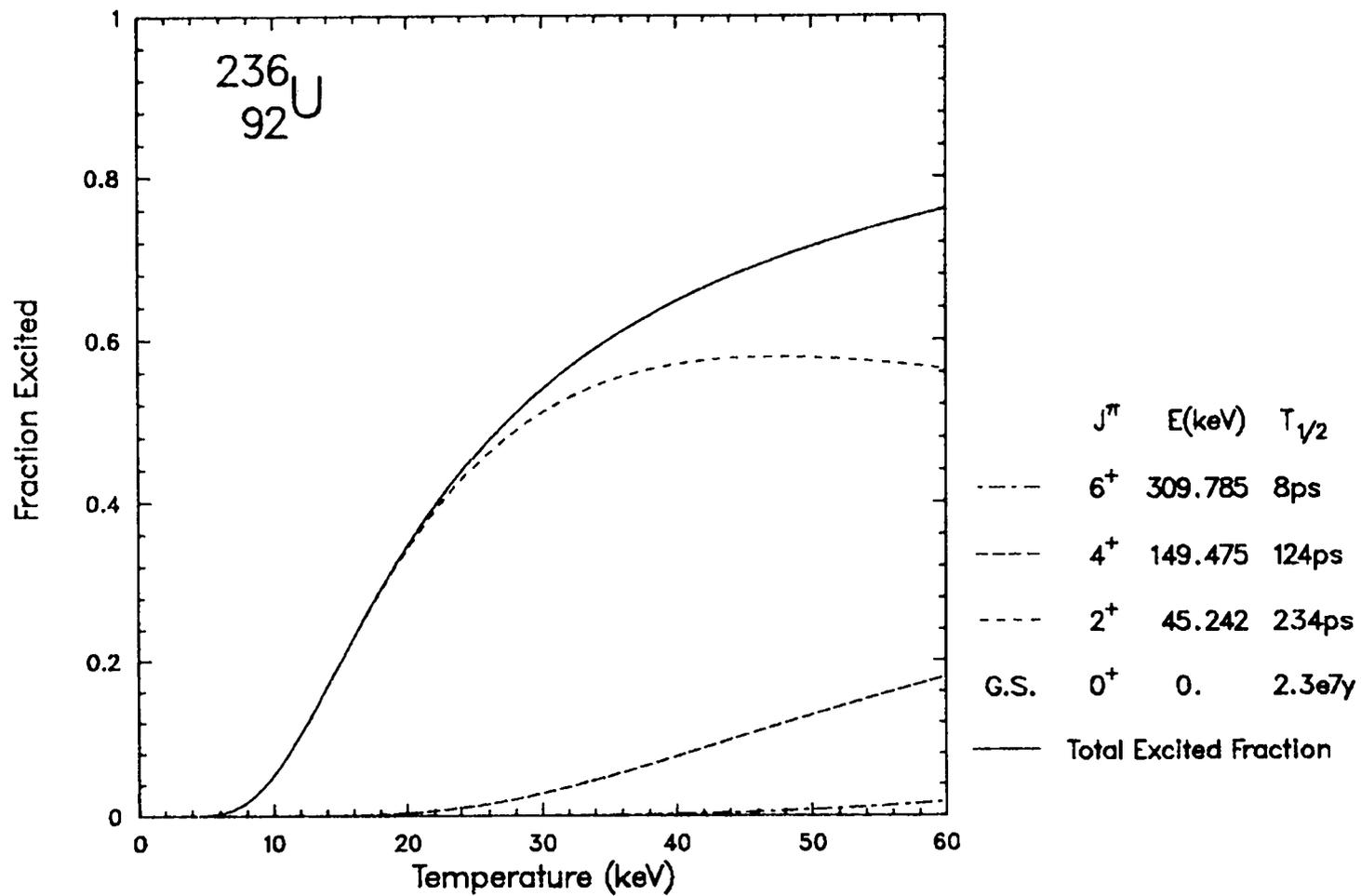


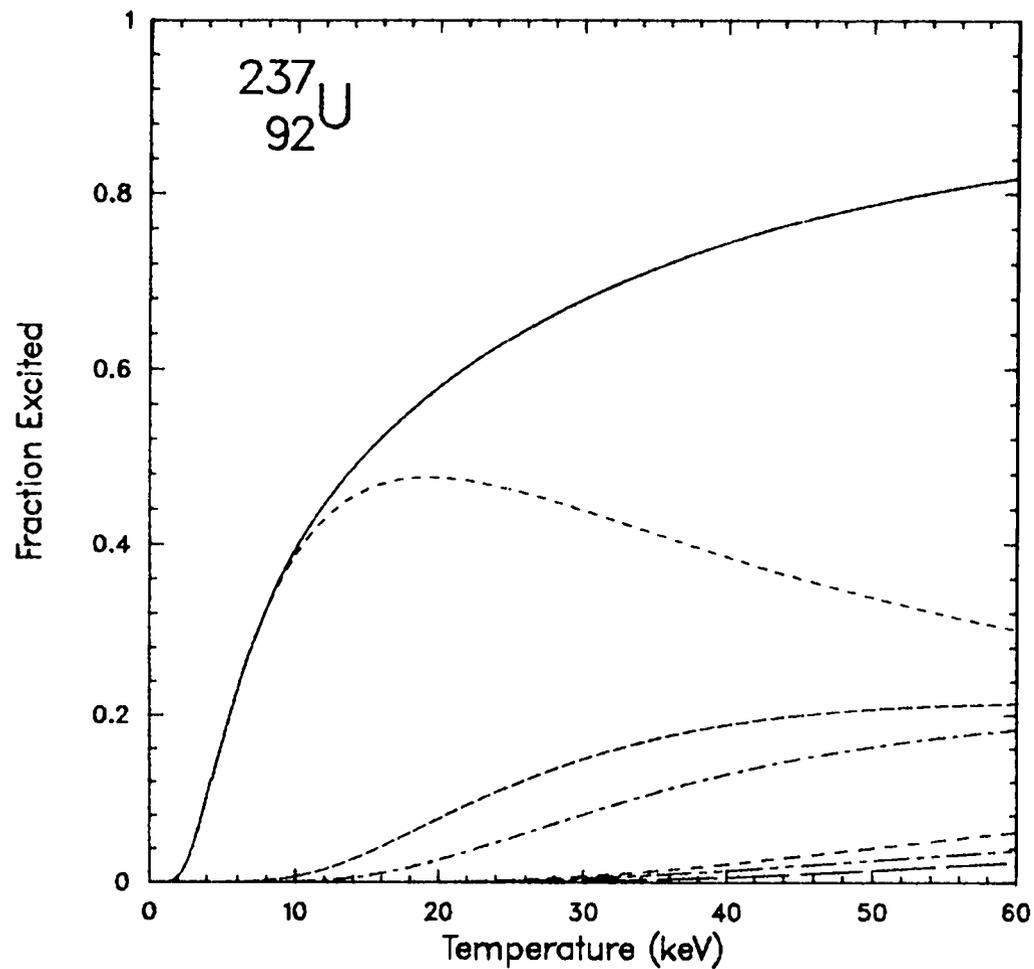


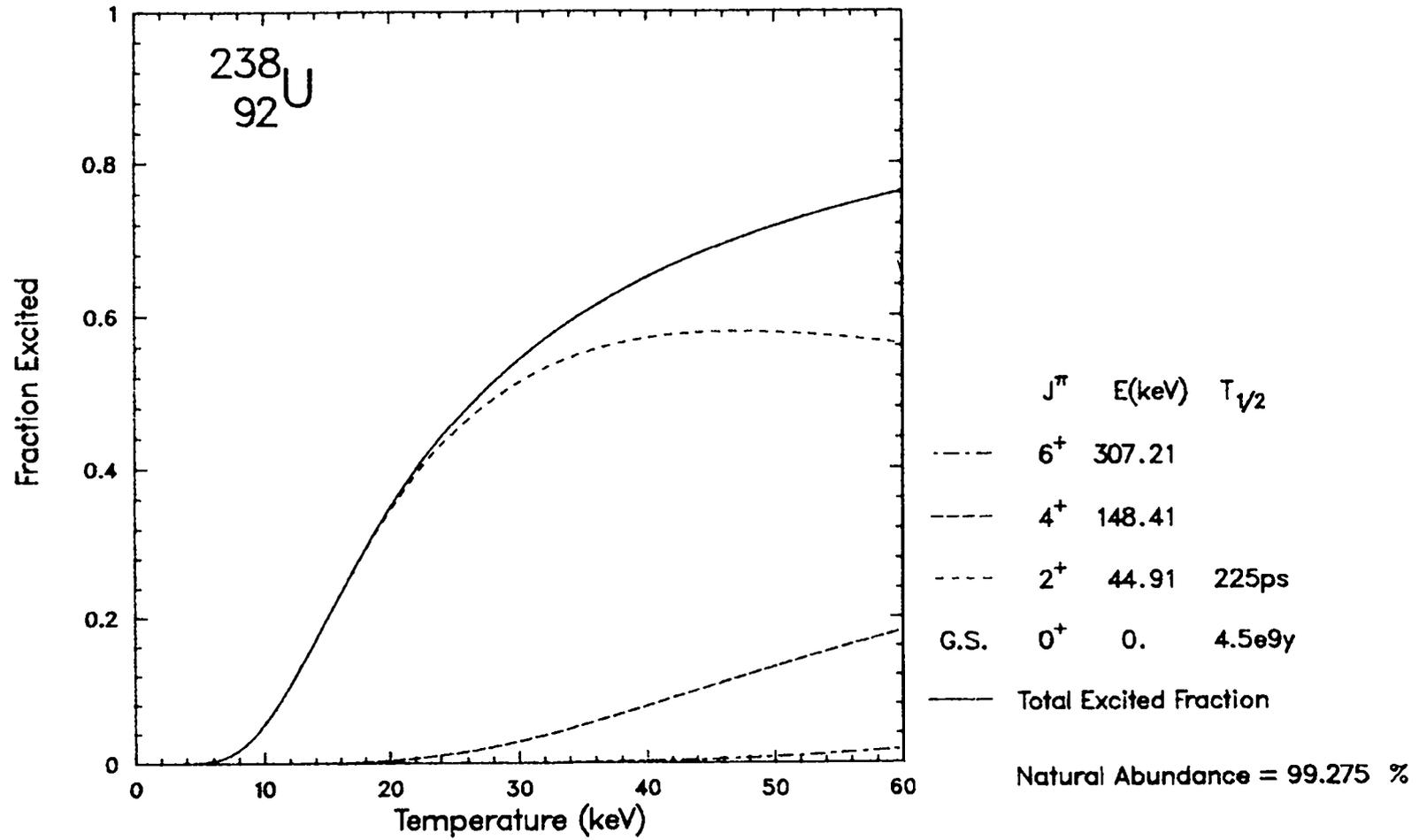


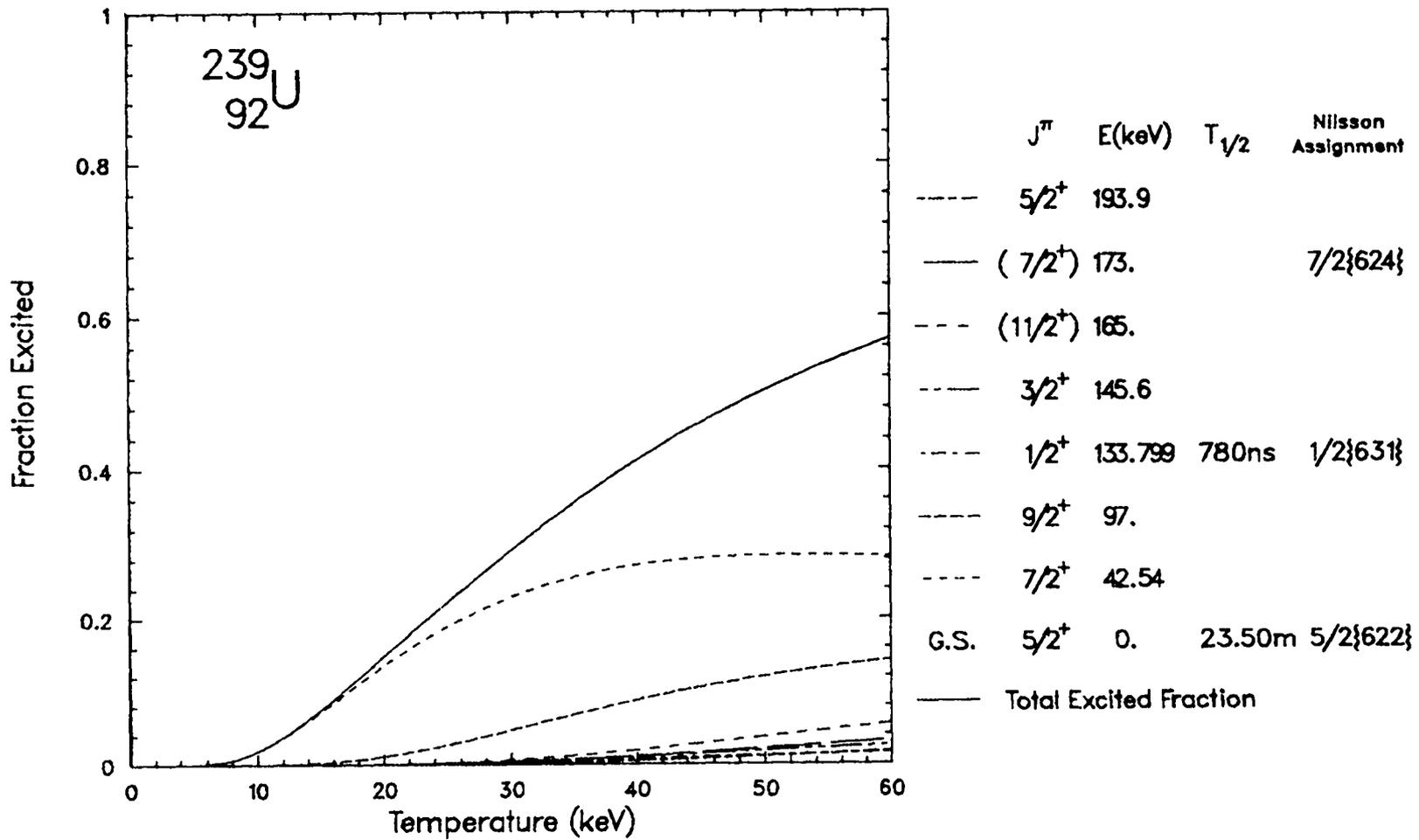
	J^π	E(keV)	$T_{1/2}$	Nilsson Assignment
----	$11/2^+$	197.13		
----	$7/2^+$	171.576		
----	$13/2^-$	170.73		
----	$9/2^+$	150.5		
----	$5/2^+$	129.29		$5/2\{622\}$
----	$11/2^-$	103.03		
----	$7/2^+$	81.77		
----	$5/2^+$	51.69	191ps	
----	$9/2^-$	46.21		
----	$3/2^+$	13.01	.5ns	
----	$1/2^+$.073	25m	$1/2\{631\}$
G.S.	$7/2^-$	0.	$7.04 \times 10^8 \text{y}$	$7/2\{743\}$
----	Total Excited Fraction			

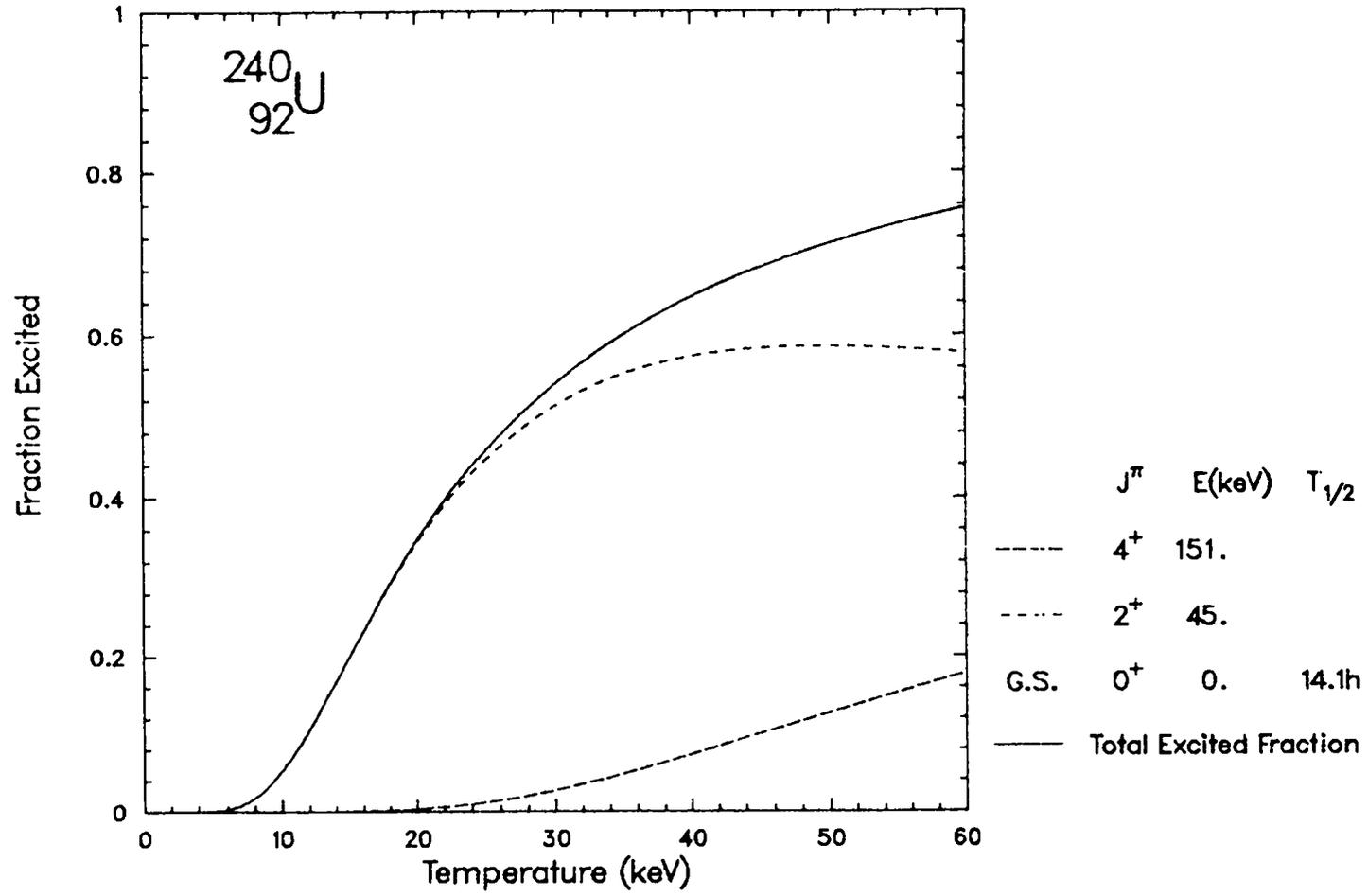
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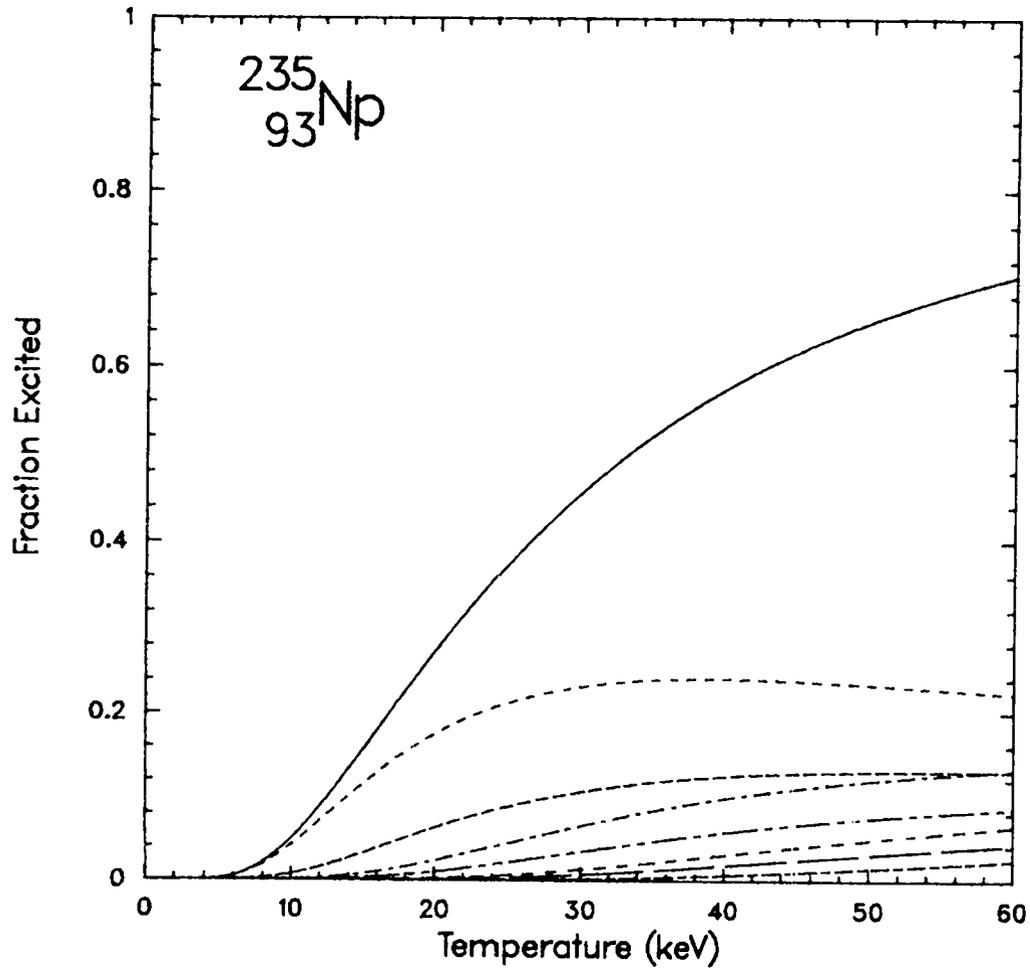




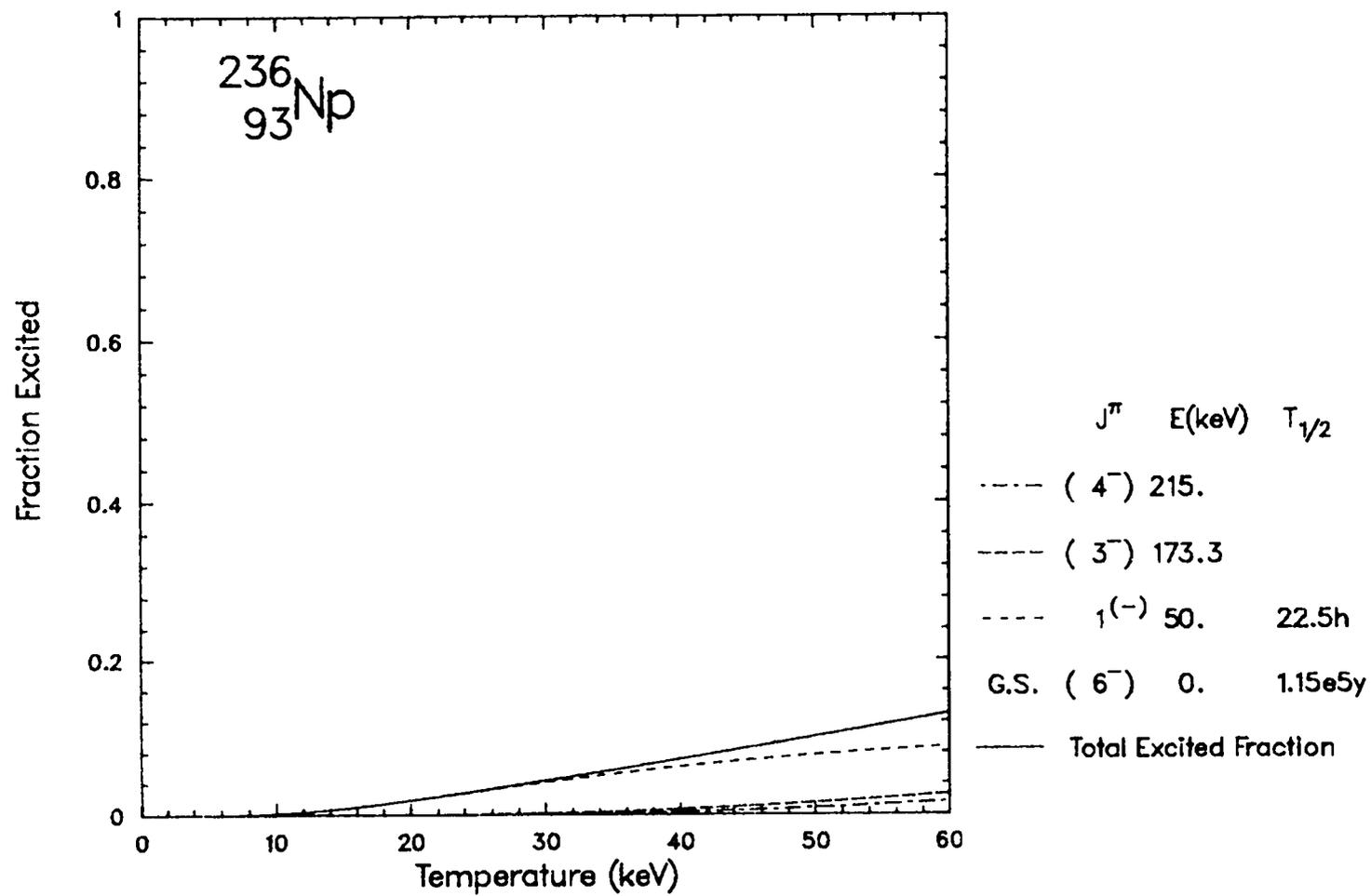


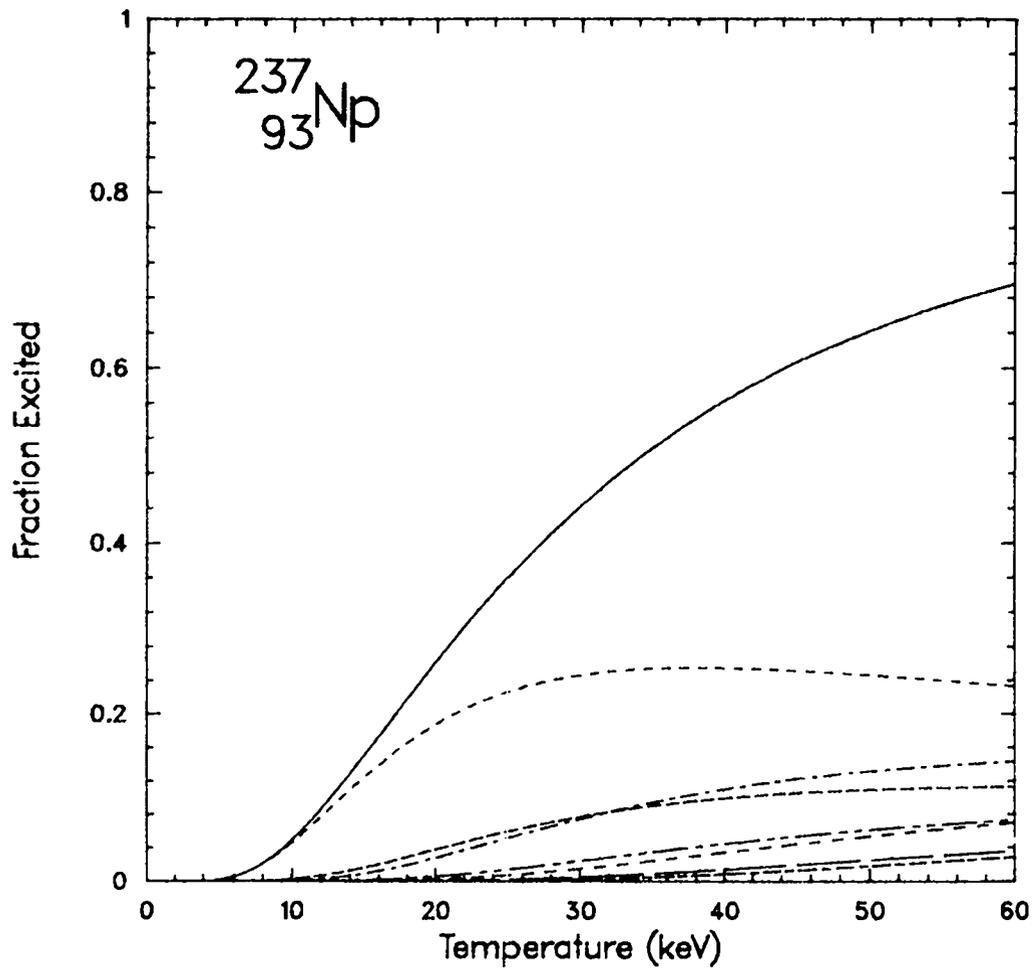




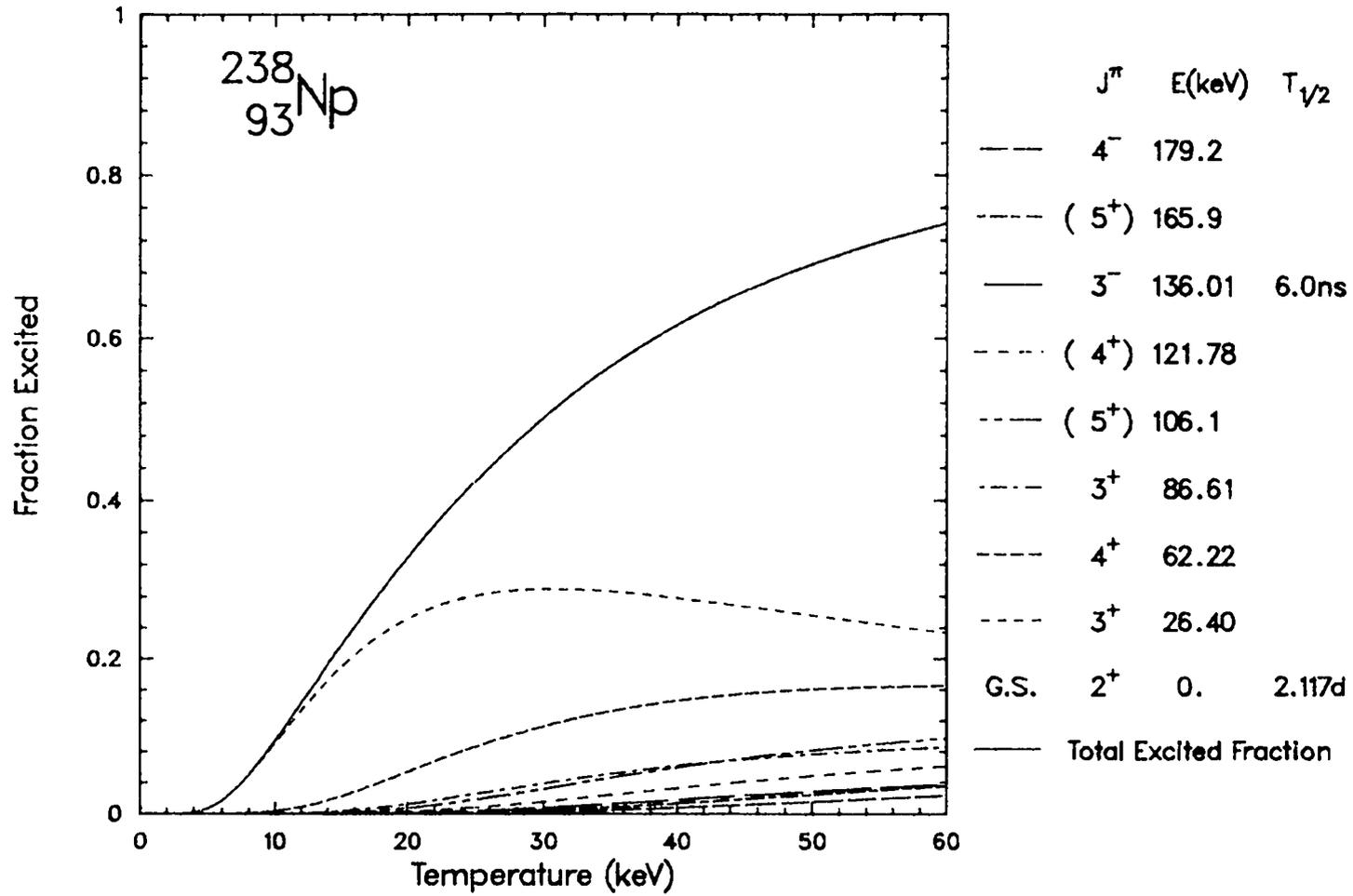


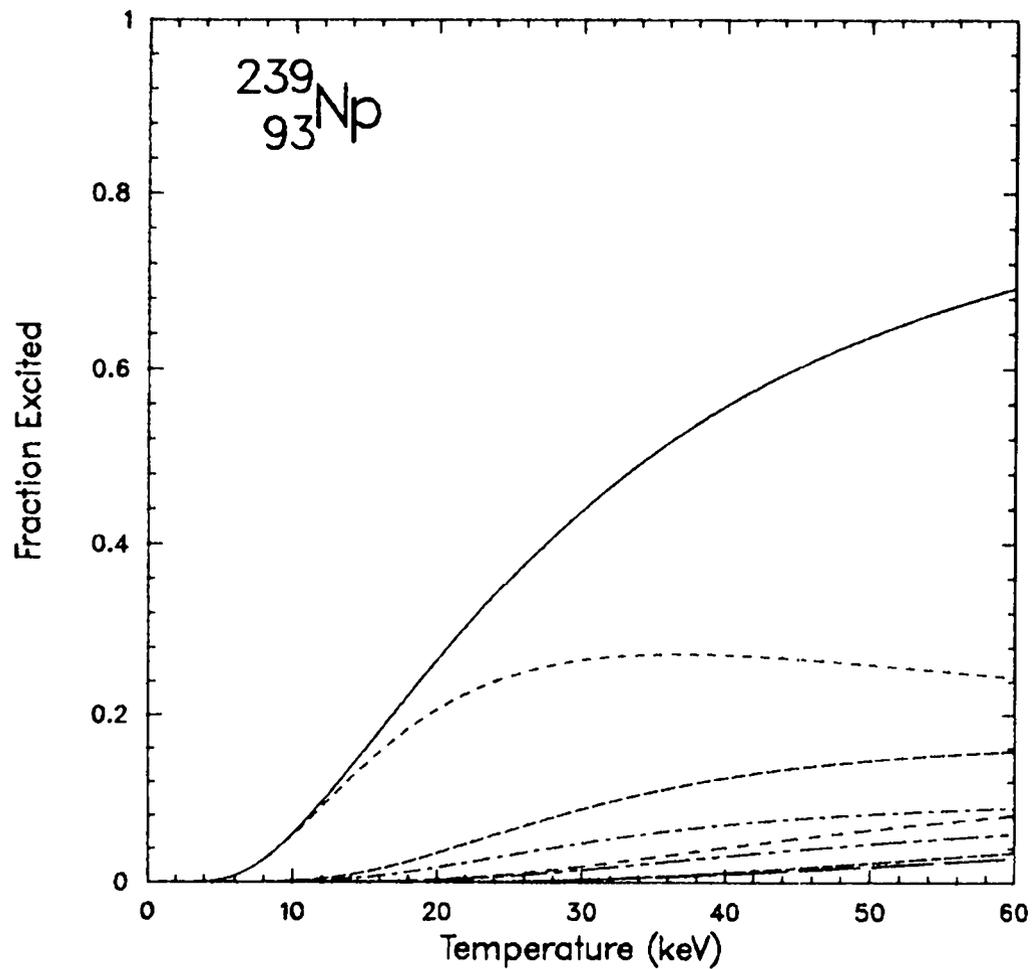
	J^π	E(keV)	$T_{1/2}$	Nilsson Assignment
---	$13/2^+$	201.		
---	$9/2^-$	146.8		
---	$(11/2^+)$	133.		
---	$(7/2^-)$	91.6		
---	$(9/2^+)$	79.1		
---	$(5/2^-)$	49.10	6.9ns	$5/2\{523\}$
---	$(7/2^+)$	34.23		
G.S.	$5/2^+$	0.	396d	$5/2\{642\}$
—	Total Excited Fraction			



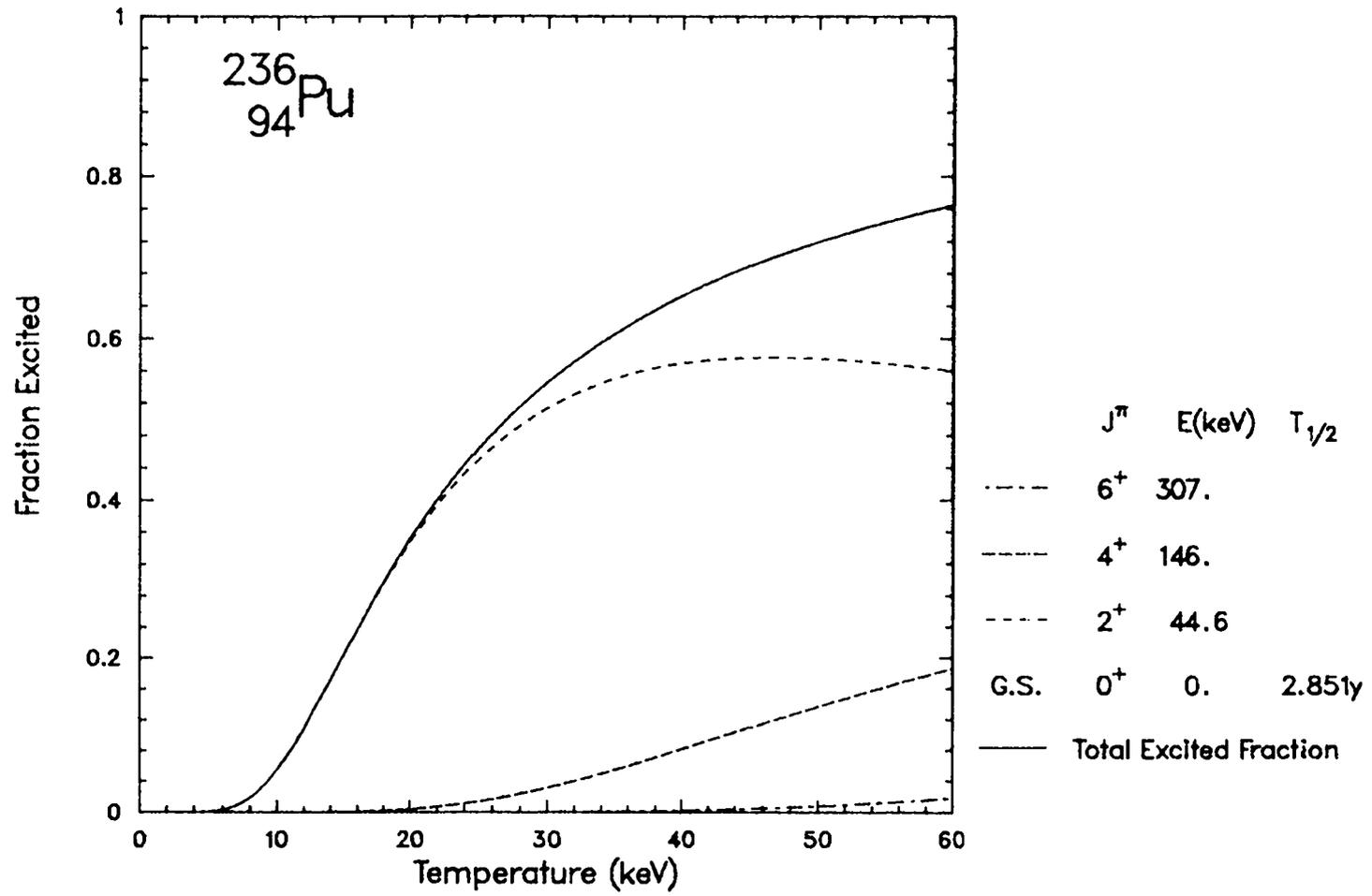


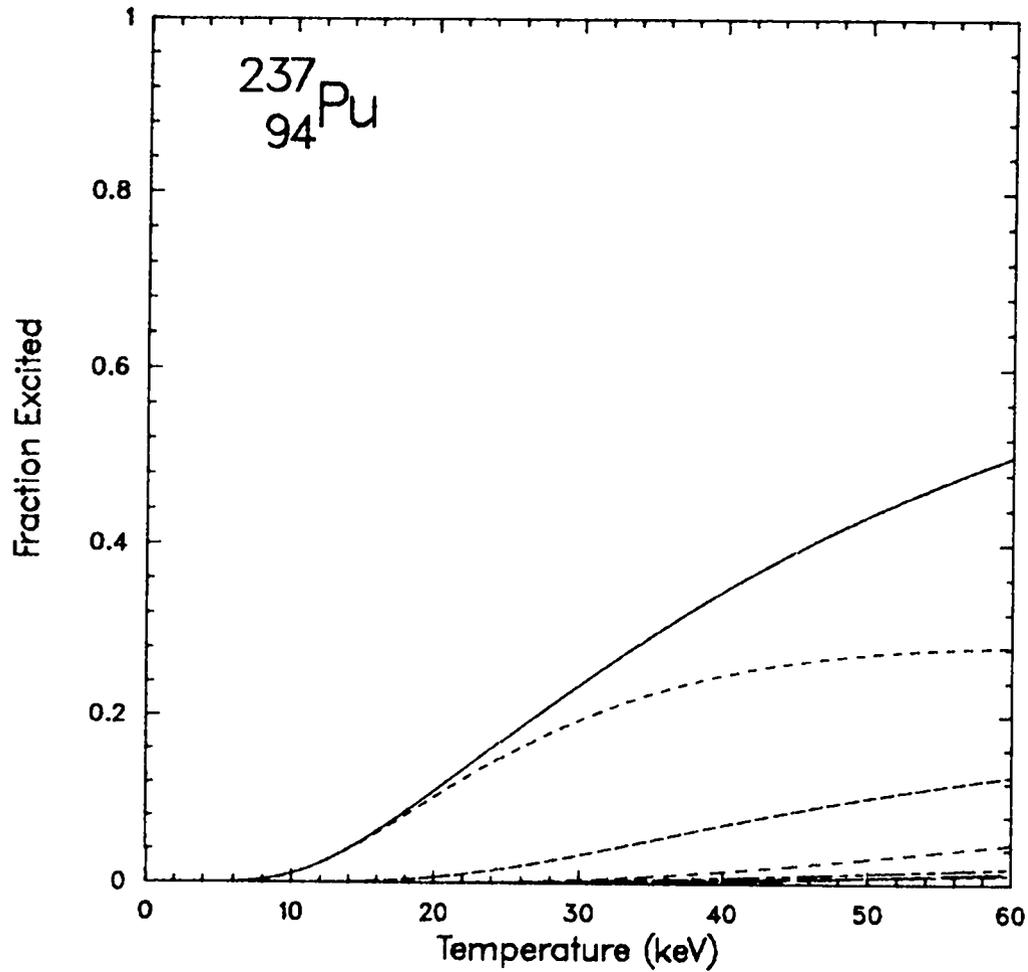
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---	$13/2^+$	192.		
—	$9/2^-$	158.48		
---	$11/2^+$	129.89		
---	$7/2^-$	102.96	80ps	
---	$9/2^+$	75.83		
---	$5/2^-$	59.537	67ns	$5/2\{523\}$
---	$7/2^+$	33.195	61ps	
G.S.	$5/2^+$	0.	2.14e6y	$5/2\{642\}$
—	Total Excited Fraction			



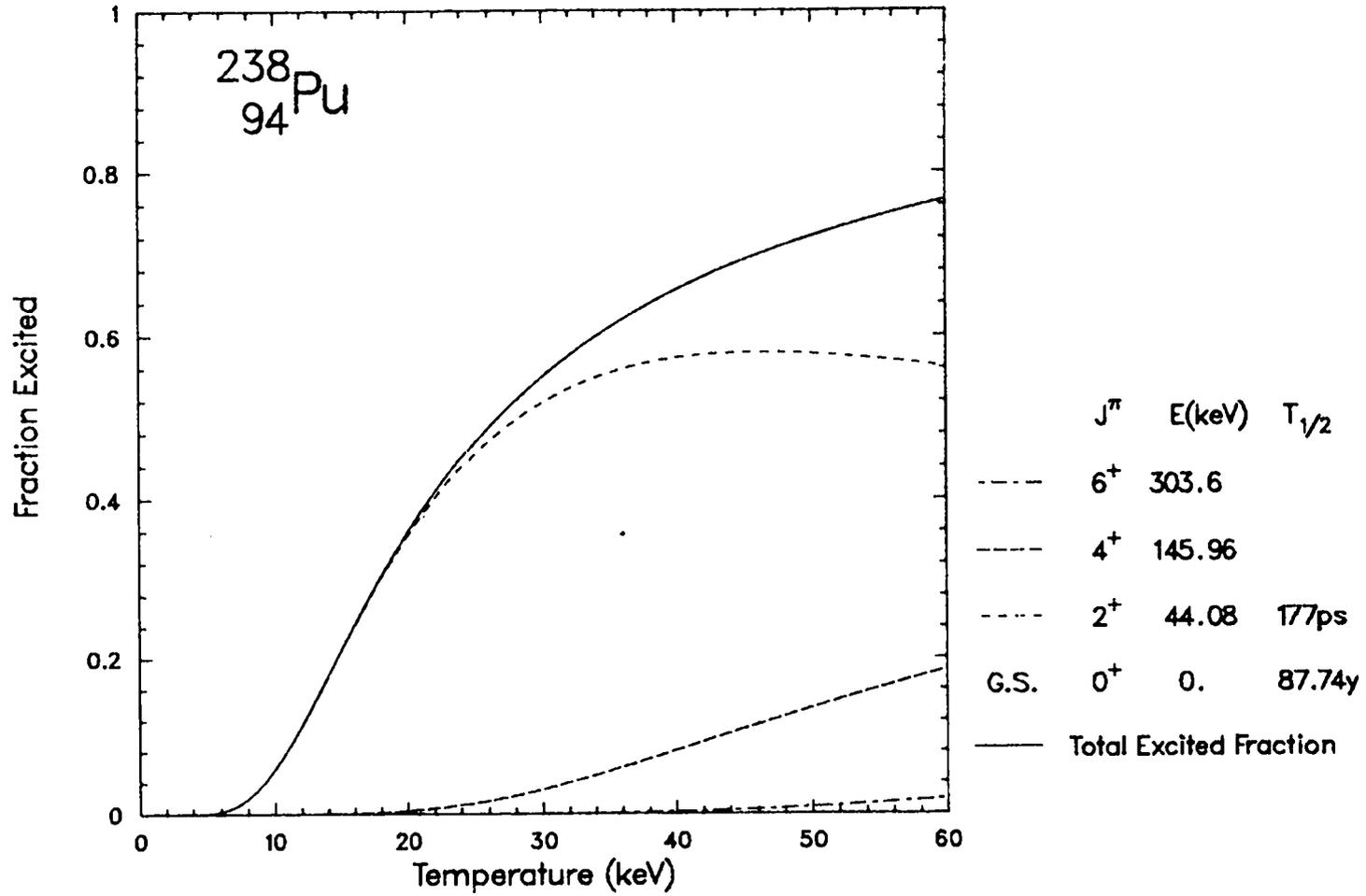


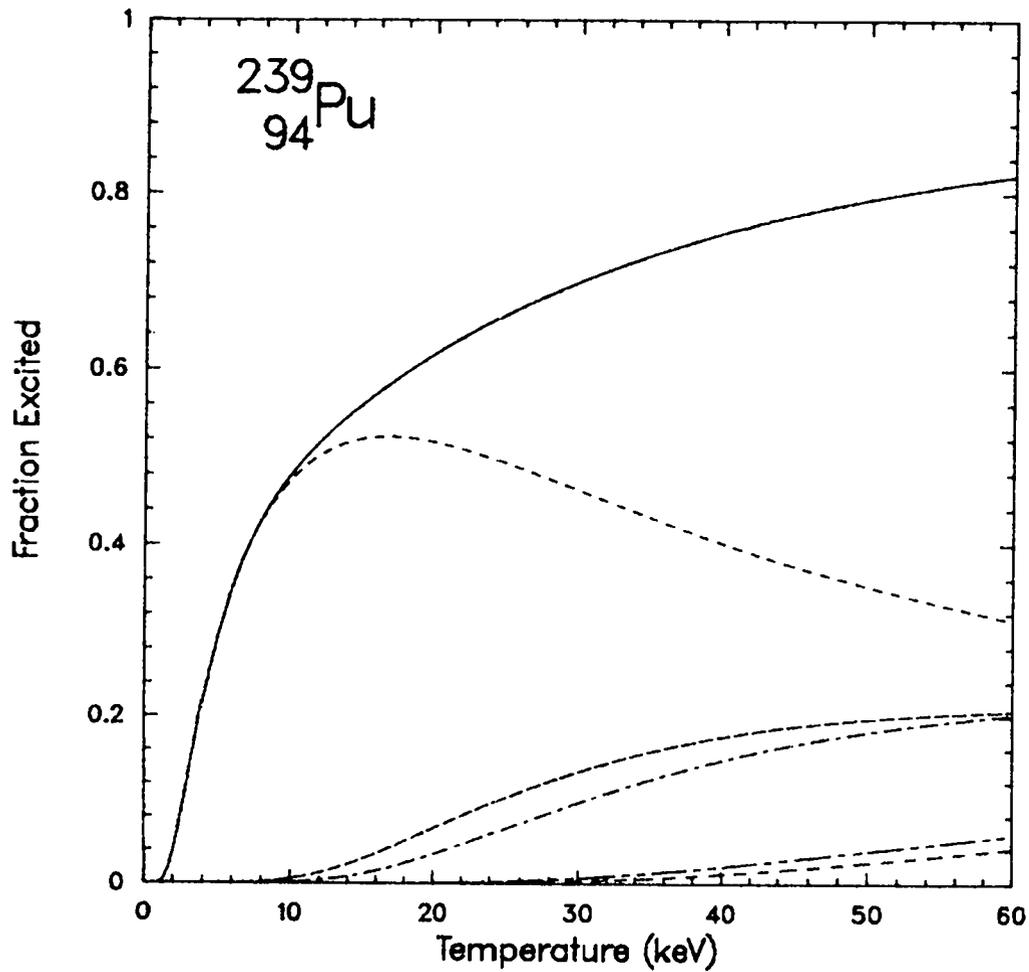
	J^π	E(keV)	$T_{1/2}$	Nilsson Assignment
---	$13/2^+$	180.0		
—	$9/2^-$	173.02		
- - -	$11/2^+$	122.6		
- - -	$7/2^-$	117.73	0.4ns>	
- - -	$5/2^-$	74.669	1.4ns	$5/2\{523\}$
---	$9/2^+$	71.21		
- - -	$7/2^+$	31.135		
G.S.	$5/2^+$	0.	2.35d	$5/2\{642\}$
—	Total Excited Fraction			



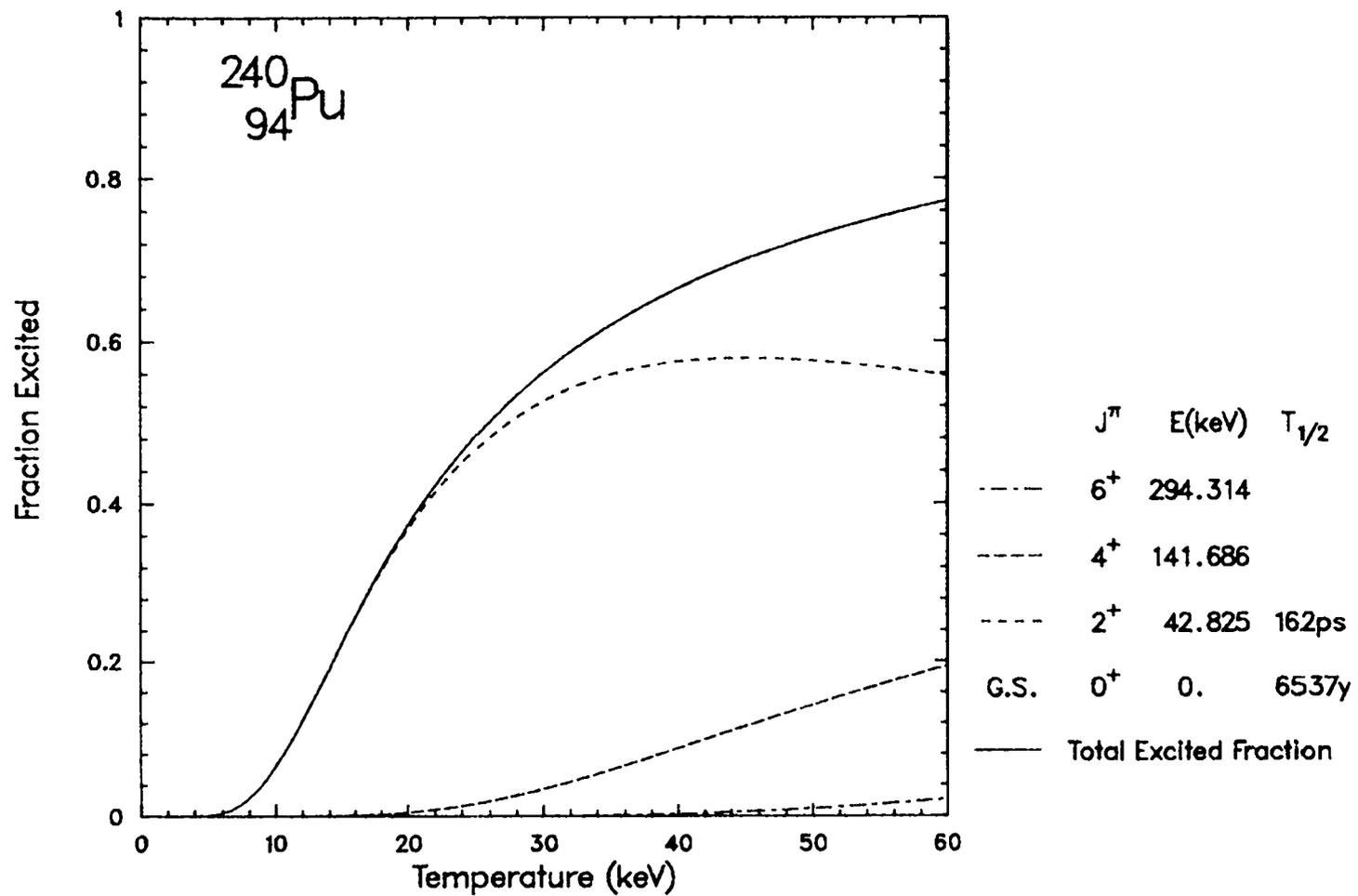


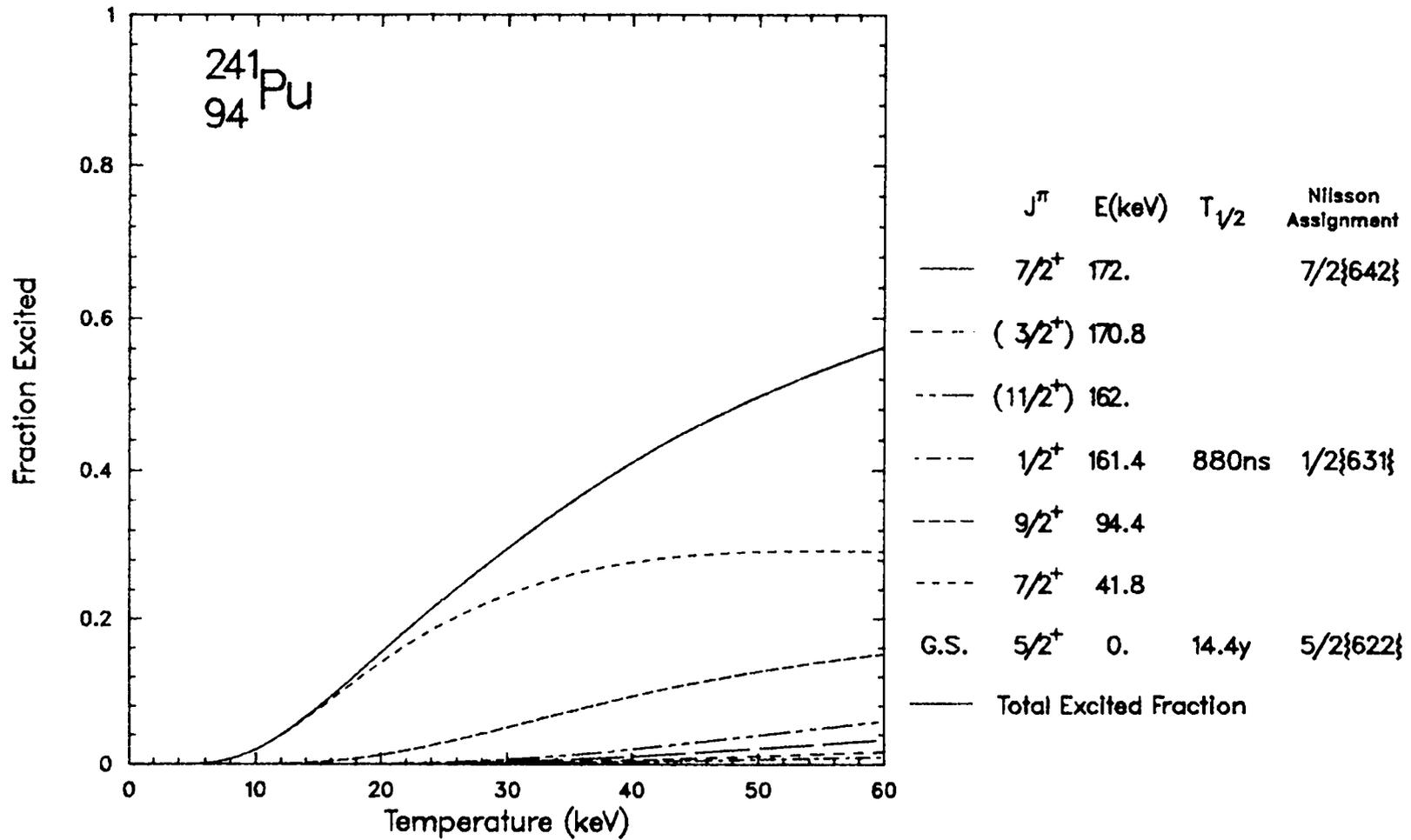
	J^π	E(keV)	$T_{1/2}$	Nilsen Assignment
—	$5/2^+$	201.18		
- - -	$(13/2^-)$	175.		
- - -	$3/2^+$	155.45		
- - -	$1/2^+$	145.544	.18s	$1/2\{631\}$
- - -	$11/2^-$	106.		
- - -	$9/2^-$	47.71		
G.S.	$7/2^-$	0.	45.3d	$7/2\{743\}$
—	Total Excited Fraction			

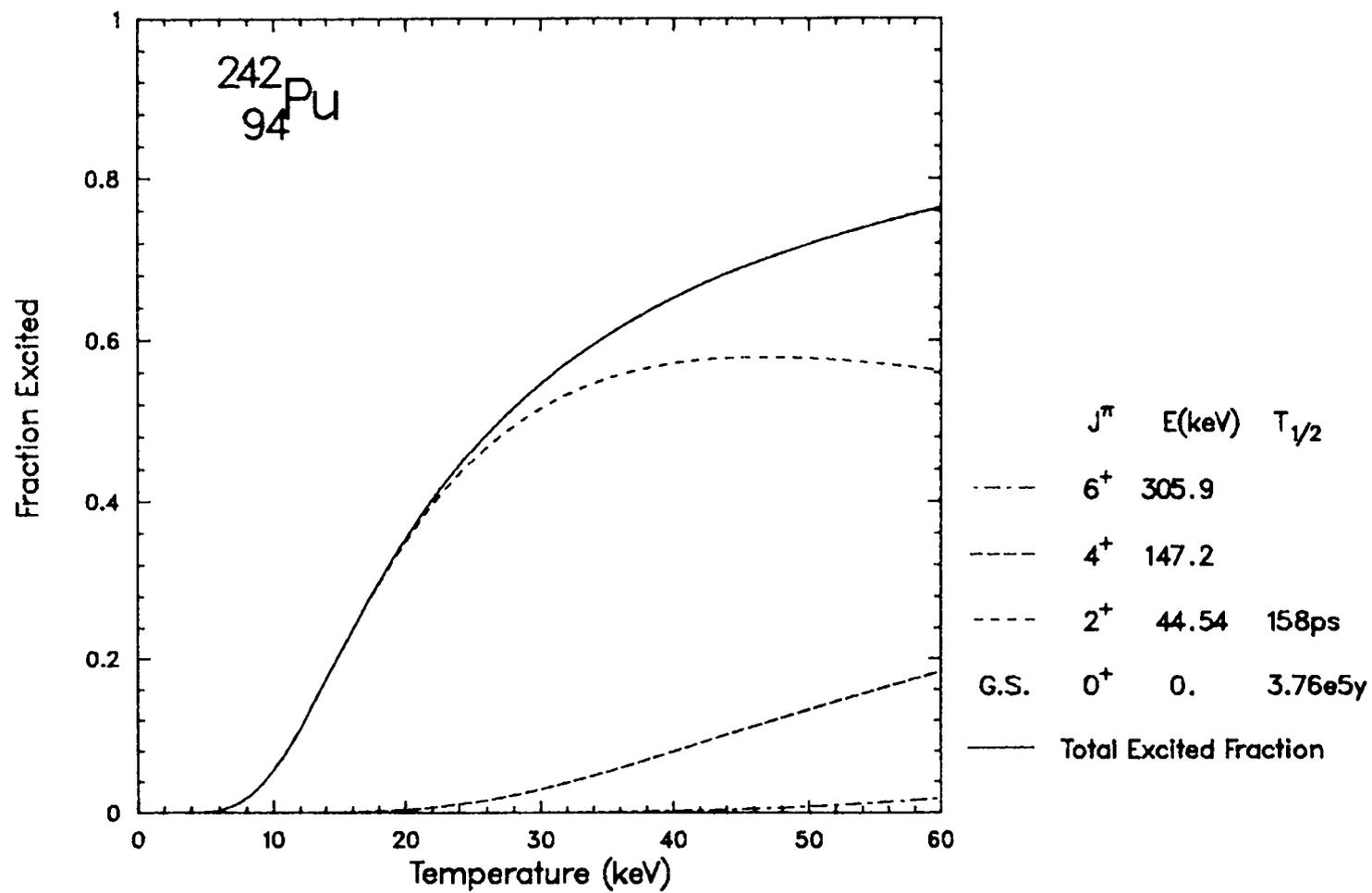


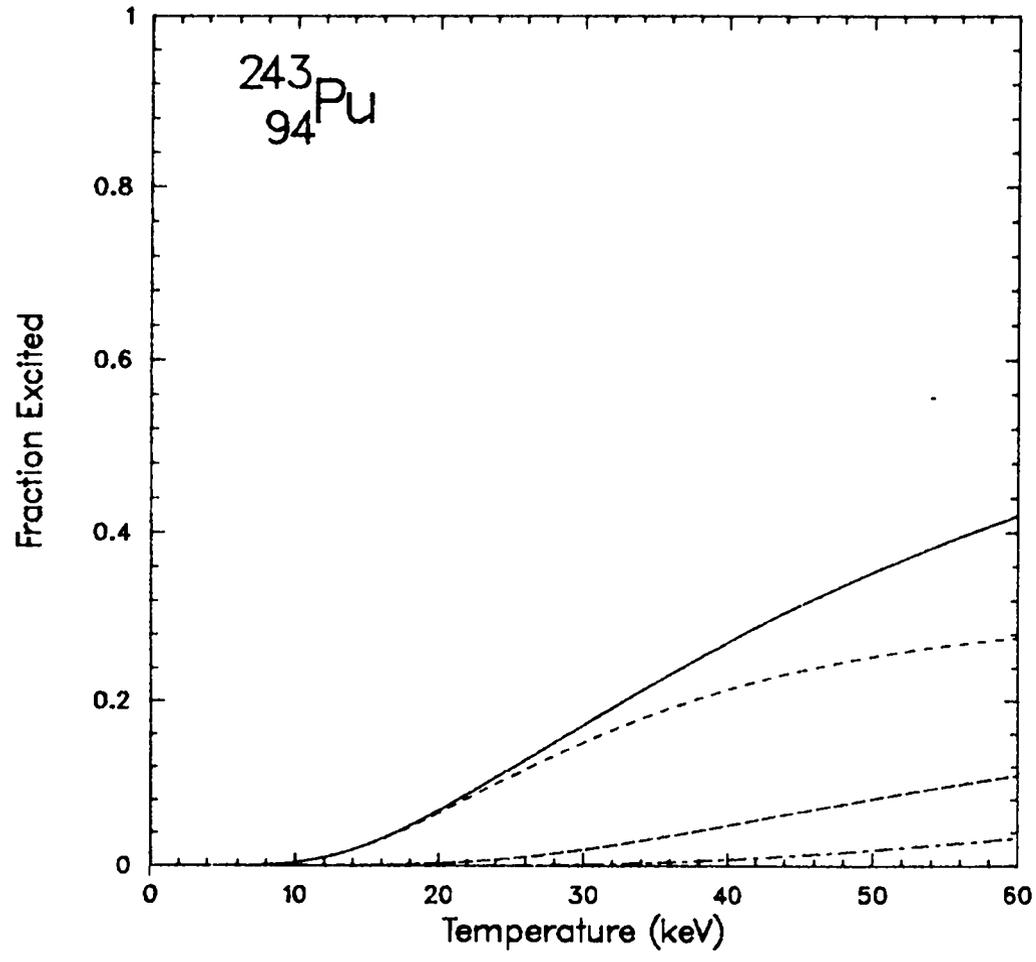


	J^π	E(keV)	$T_{1/2}$	Nilsson Assignment
---	$11/2^+$	194.		
---	$9/2^+$	163.75		
---	$7/2^+$	75.701		
---	$5/2^+$	57.273	100ps	
---	$3/2^+$	7.860		
G.S.	$1/2^+$	0.	24110y	$1/2\{631\}$
—	Total Excited Fraction			

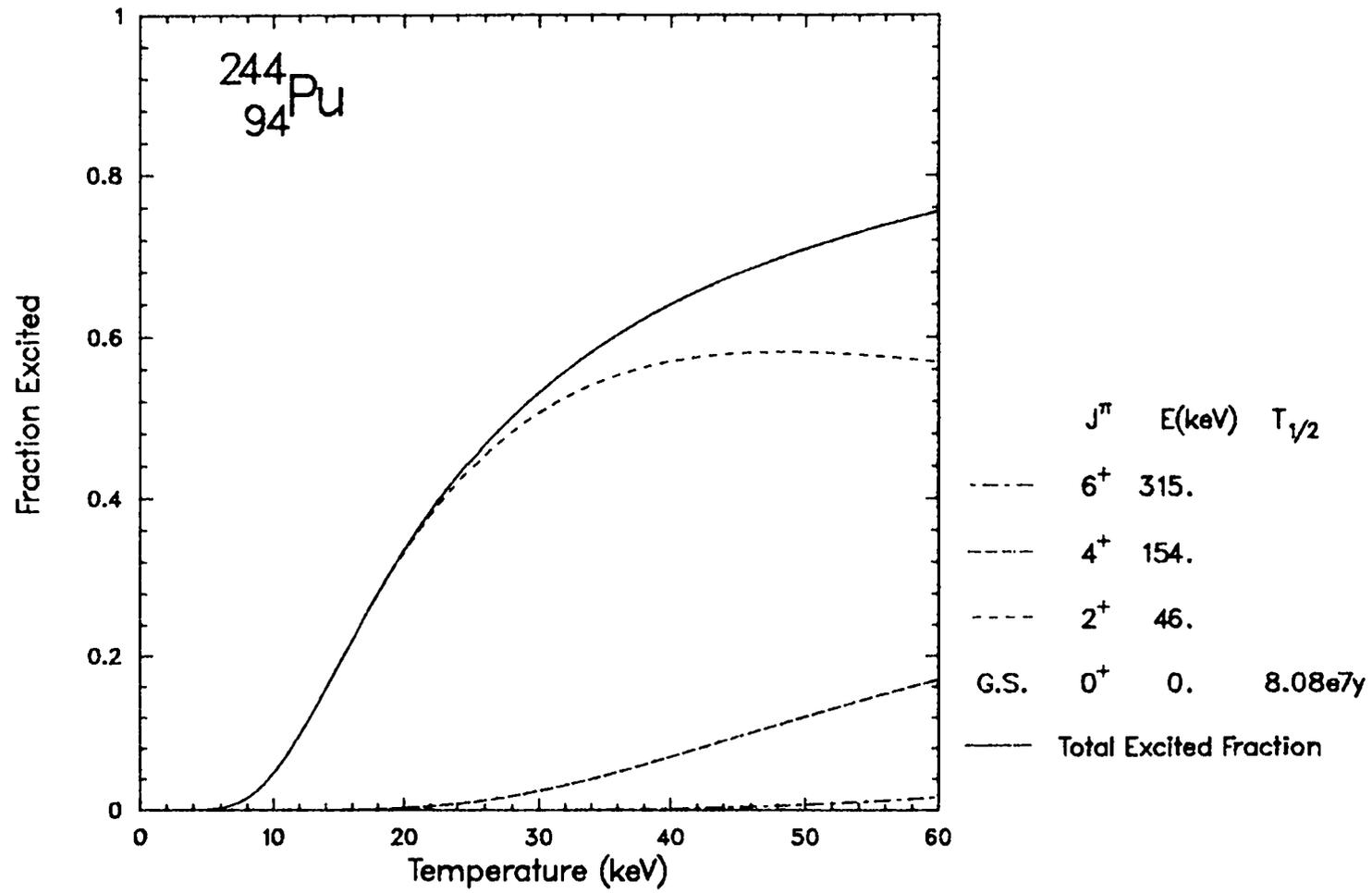


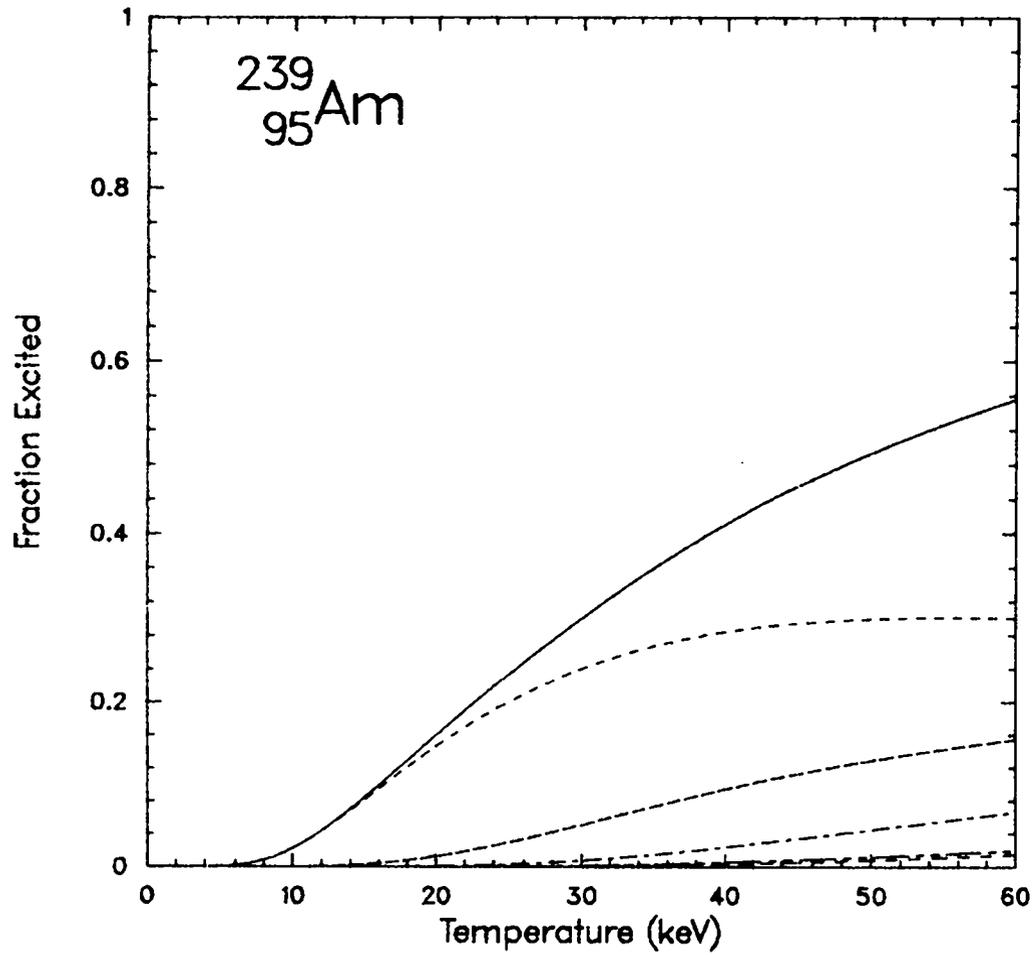




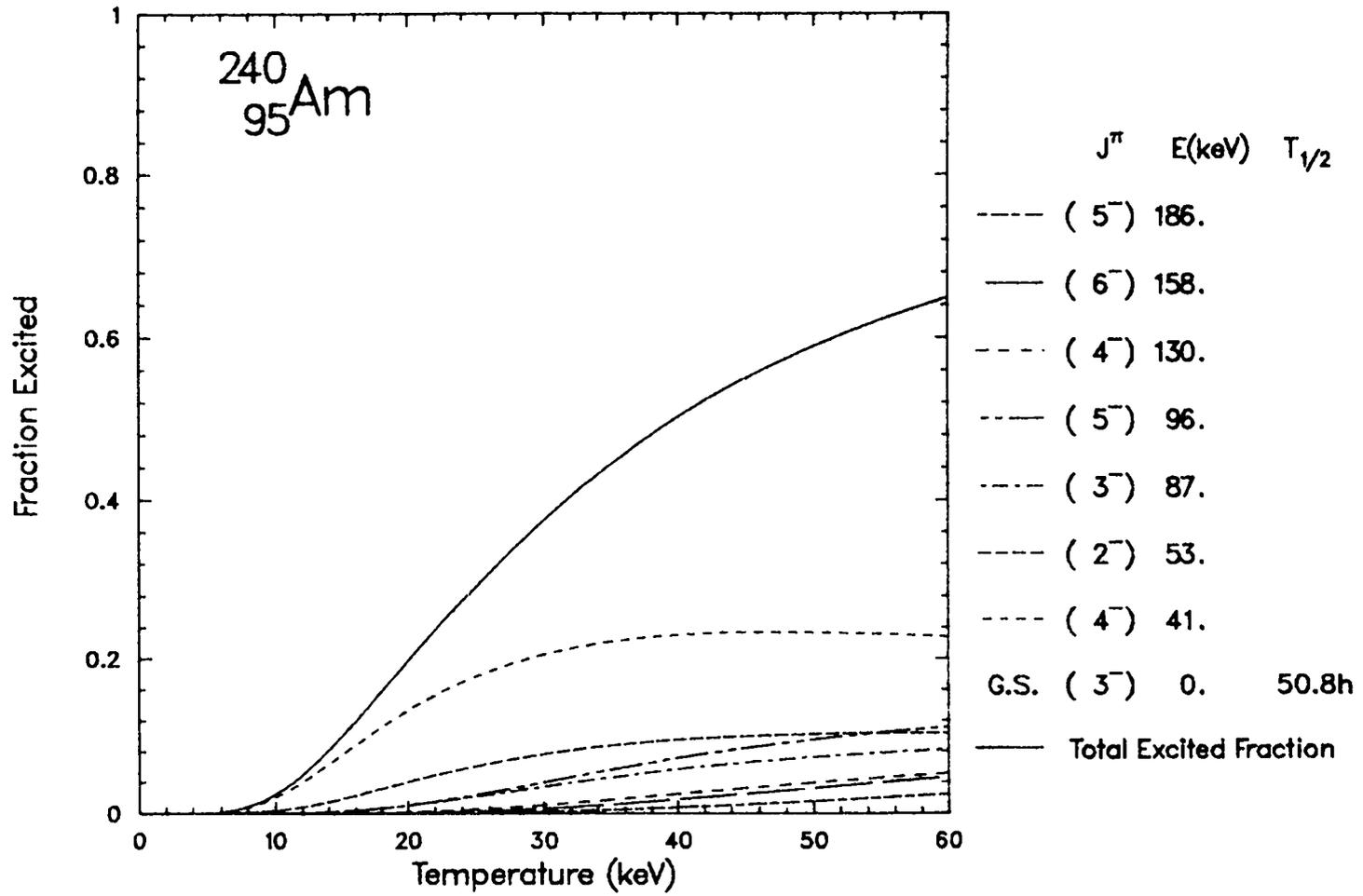


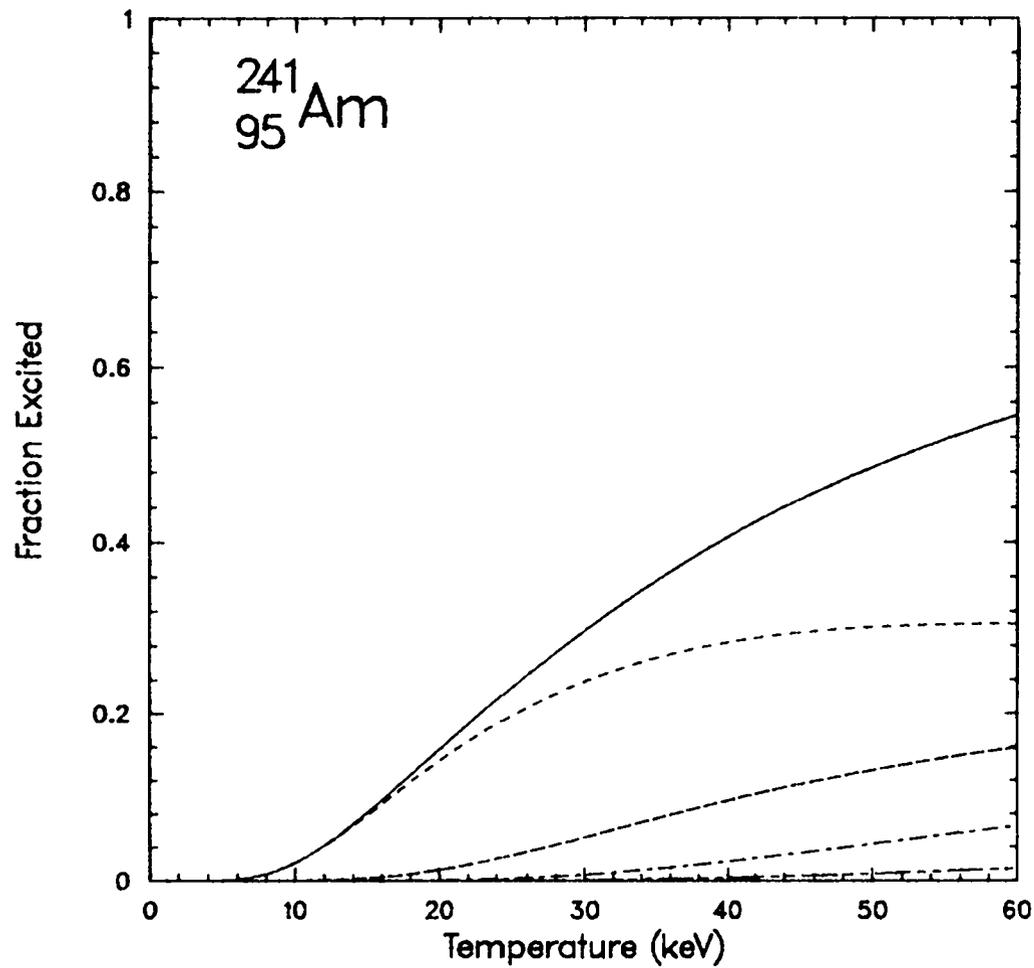
	J^π	E(keV)	$T_{1/2}$	Nilsson Assignment
-----	$(13/2^+)$	204.4		
-----	$11/2^+$	124.4		
-----	$9/2^+$	58.1		
	G.S.	$7/2^+$	0.	4.956h $7/2\{624\}$
—————	Total Excited Fraction			



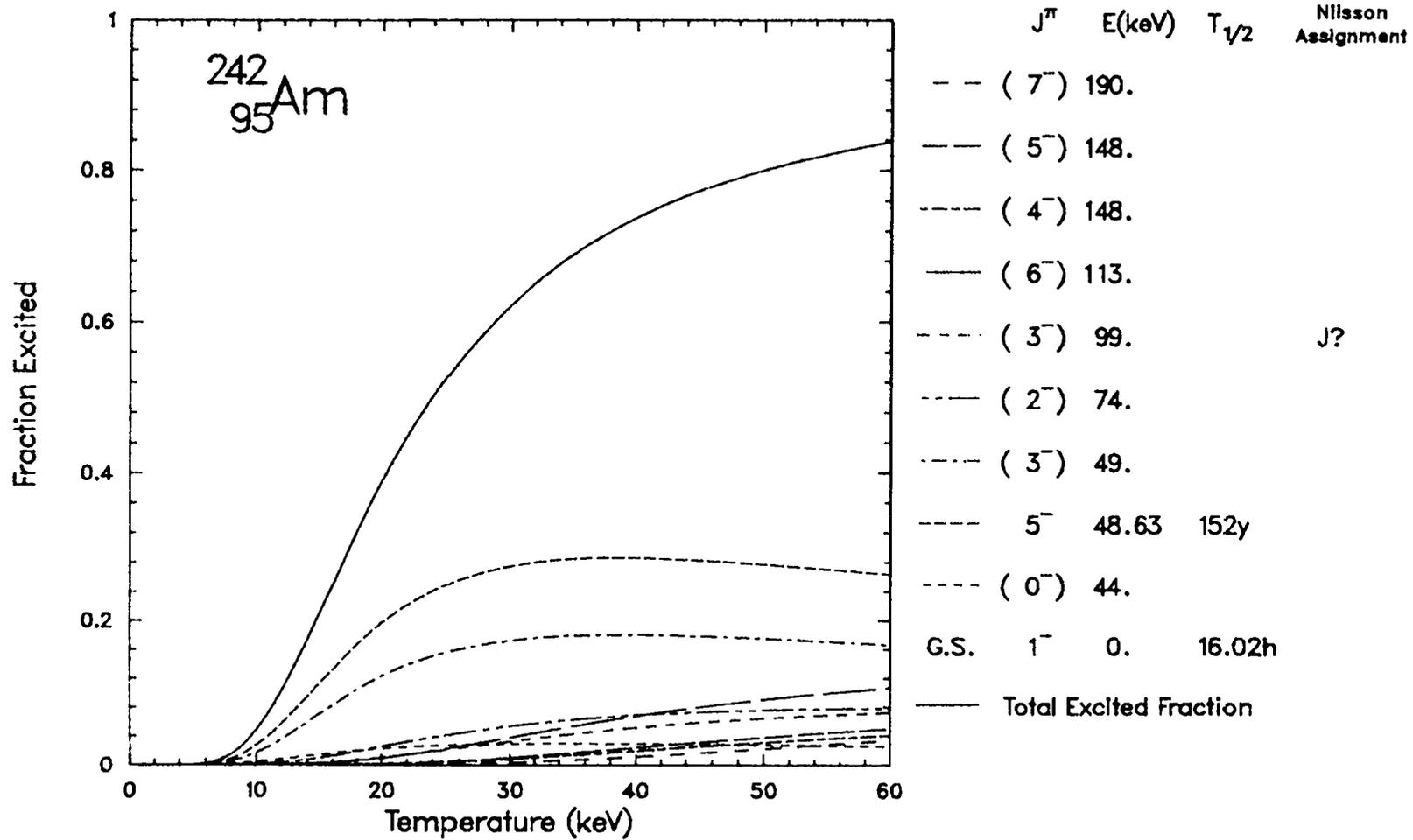


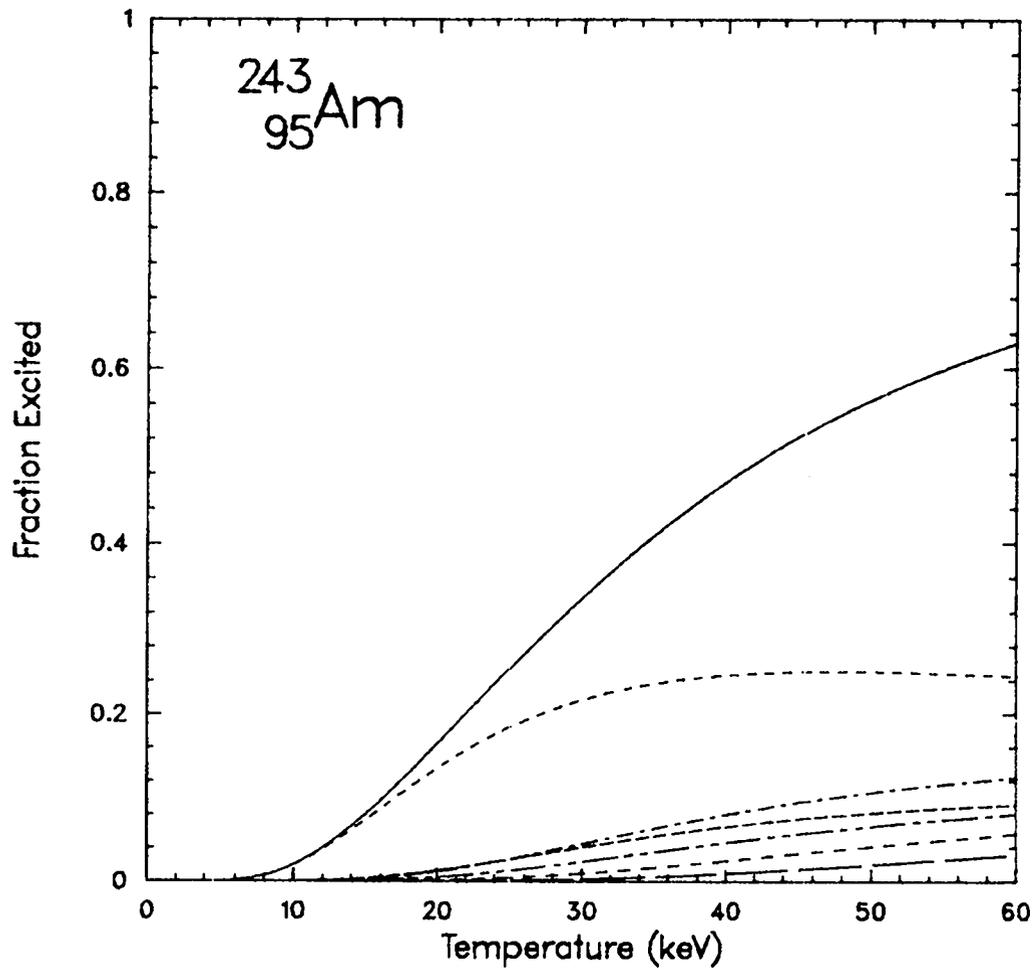
J^π	E(keV)	$T_{1/2}$	Nilsson Assignment
(7/2 ⁺)	220.		
(5/2 ⁺)	187.1		5/2{642}
(11/2 ⁻)	156.		
(9/2 ⁻)	94.		
(7/2 ⁻)	40.7		
G.S.	5/2 ⁻	0.	11.9h 5/2{523}
— Total Excited Fraction			



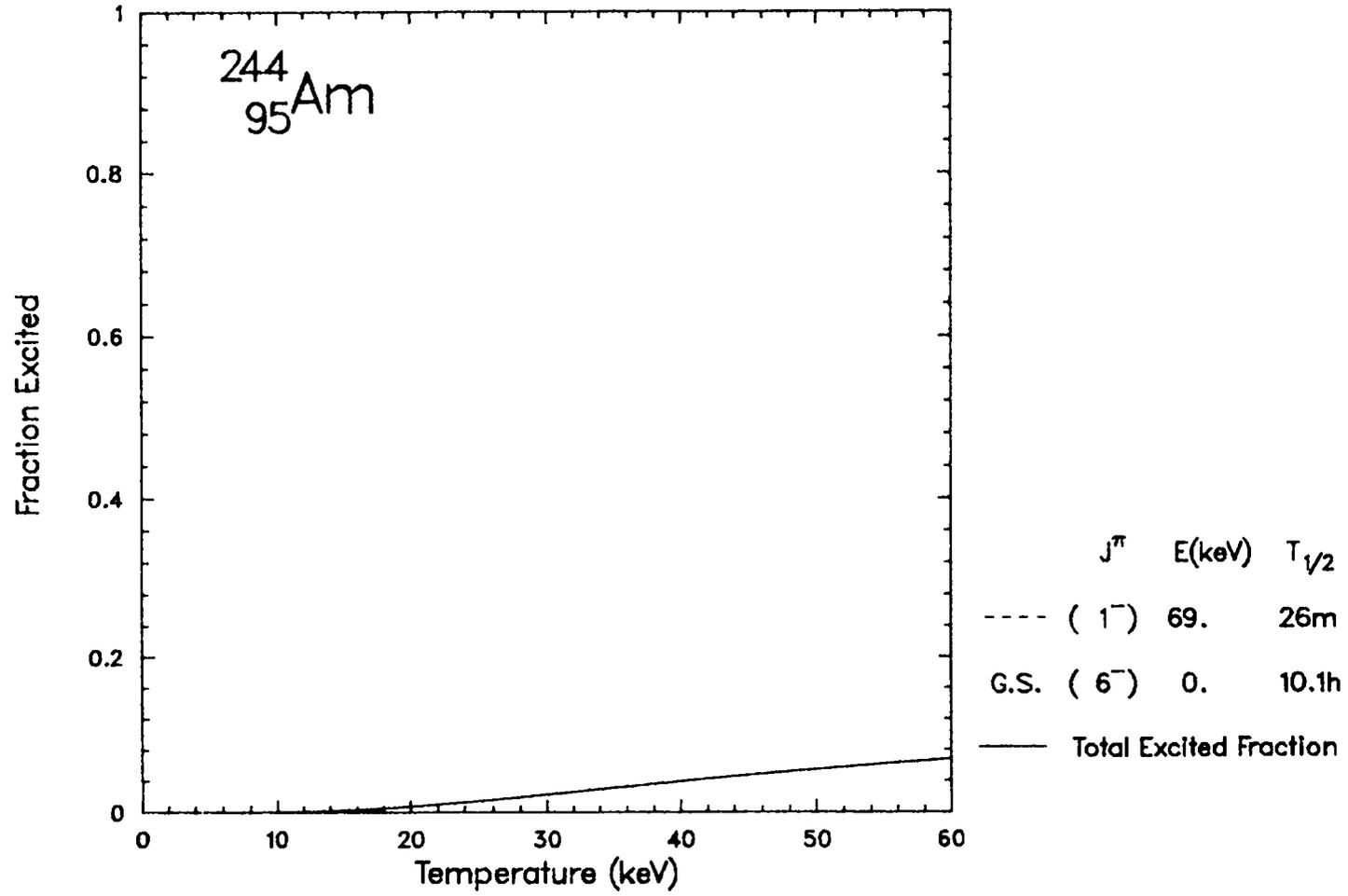


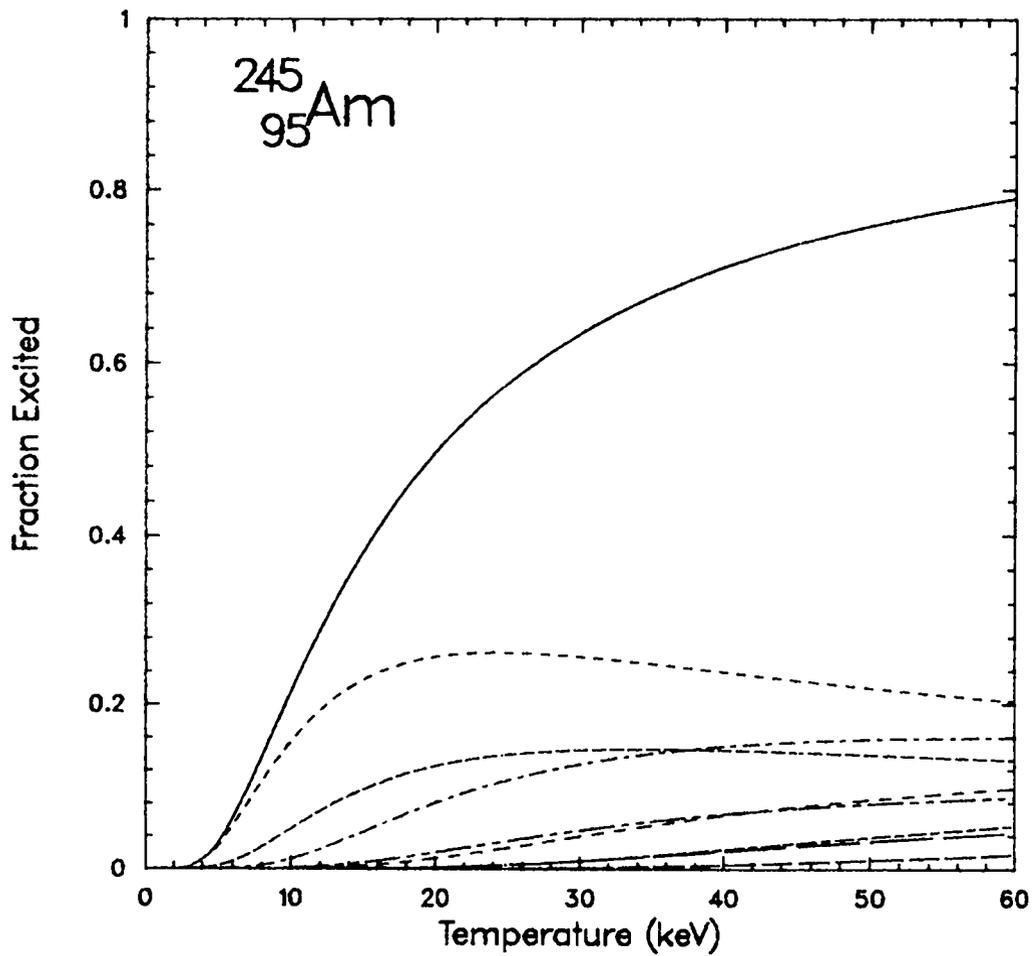
	J^π	E(keV)	$T_{1/2}$	Nilsson Assignment
---	$5/2^+$	205.883		$5/2\{642\}$
-.-.-	$11/2^-$	158.		
-.-.-	$9/2^-$	93.65		
-.-.-	$7/2^-$	41.176		
G.S.	$5/2^-$	0.	432.2y	$5/2\{523\}$
—	Total Excited Fraction			



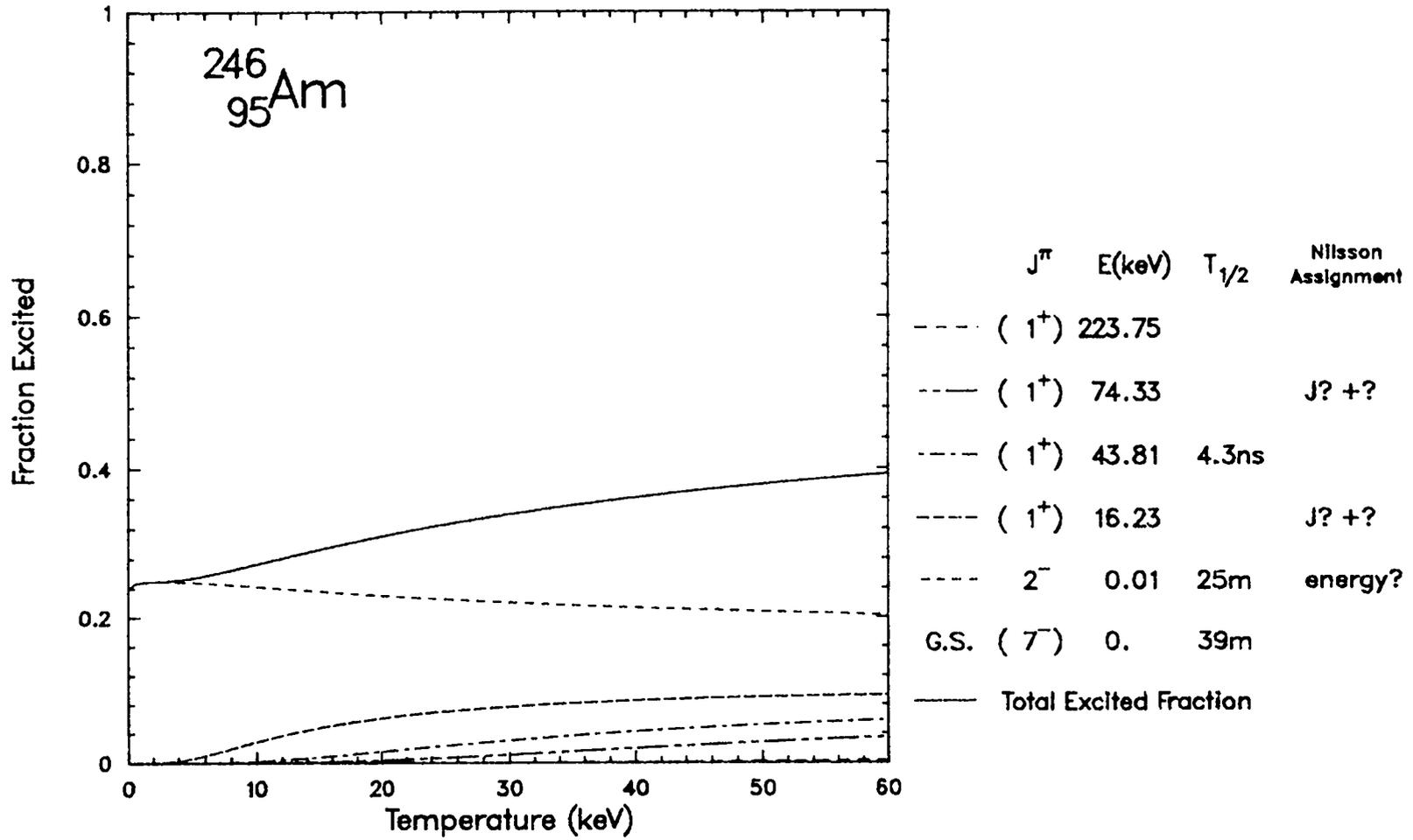


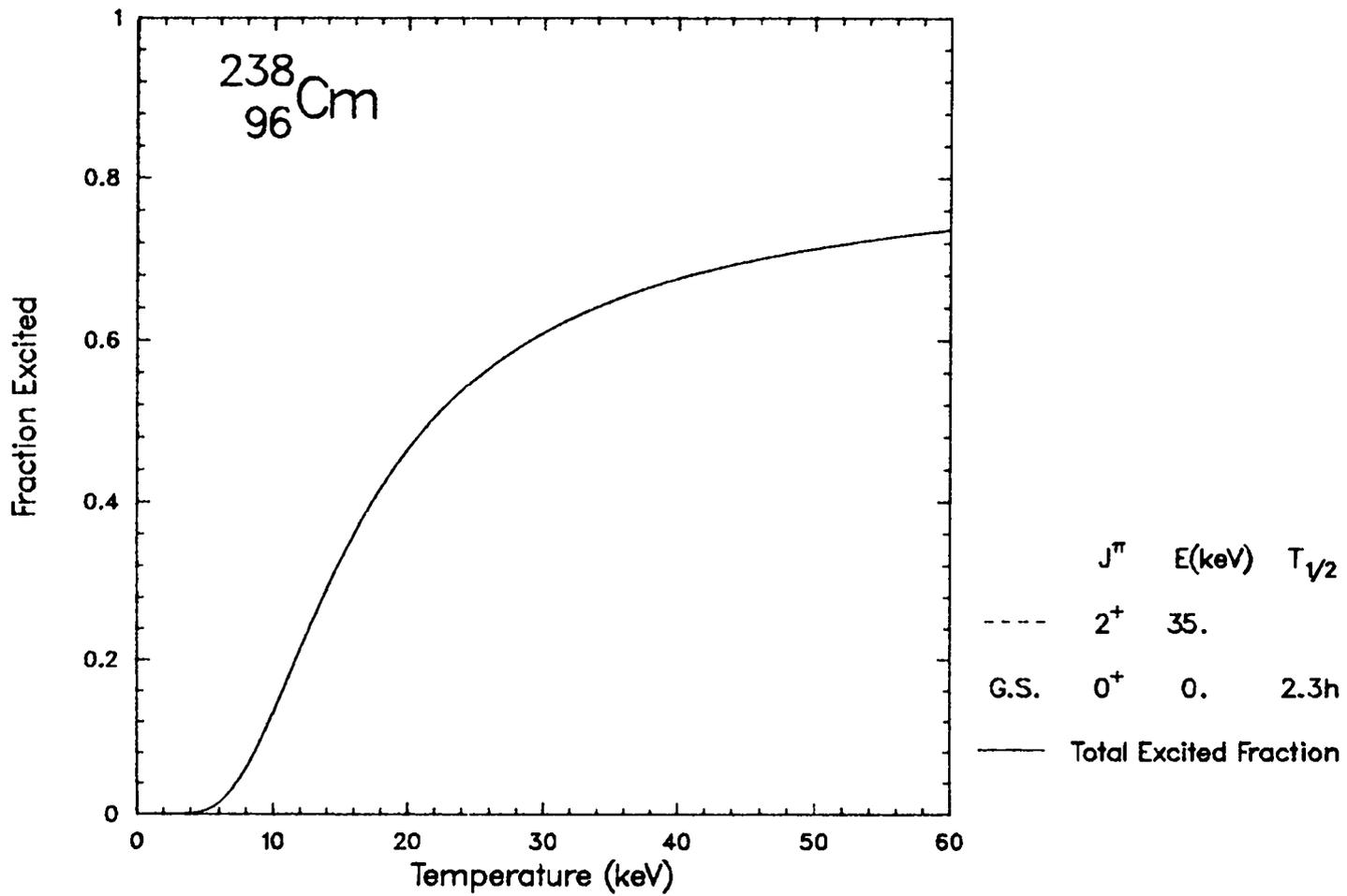
	J^π	E(keV)	$T_{1/2}$	Nilsen Assignment
—	$(11/2^+)$	189.3		
- - -	$(9/2^+)$	143.5		
- - -	$7/2^+$	109.3		
- - -	$9/2^-$	96.4		
- - -	$5/2^+$	84.	2.34ns	$5/2\{642\}$
- - -	$7/2^-$	42.2		
G.S.	$5/2^-$	0.	7380y	$5/2\{523\}$
—	Total Excited Fraction			

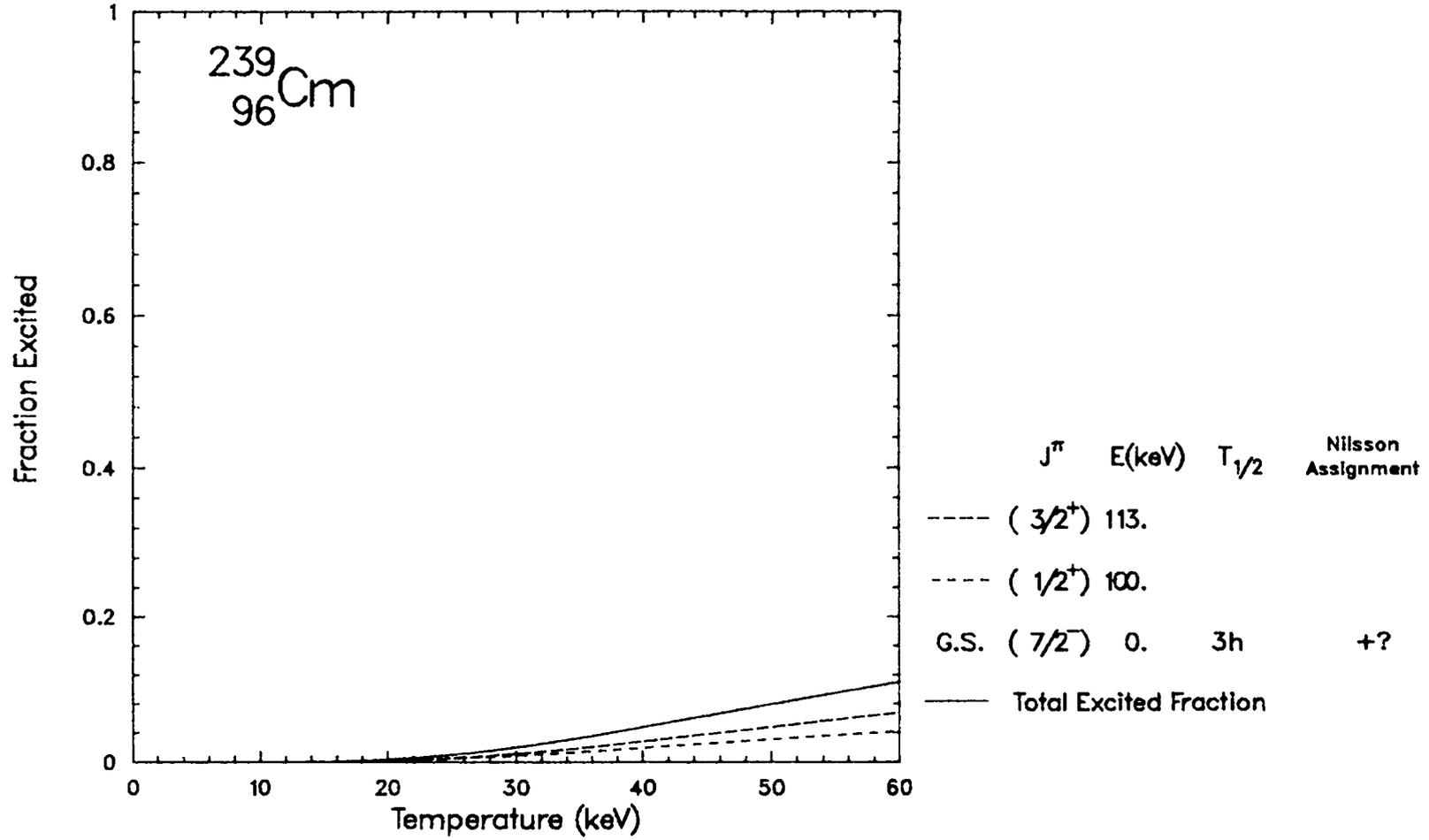


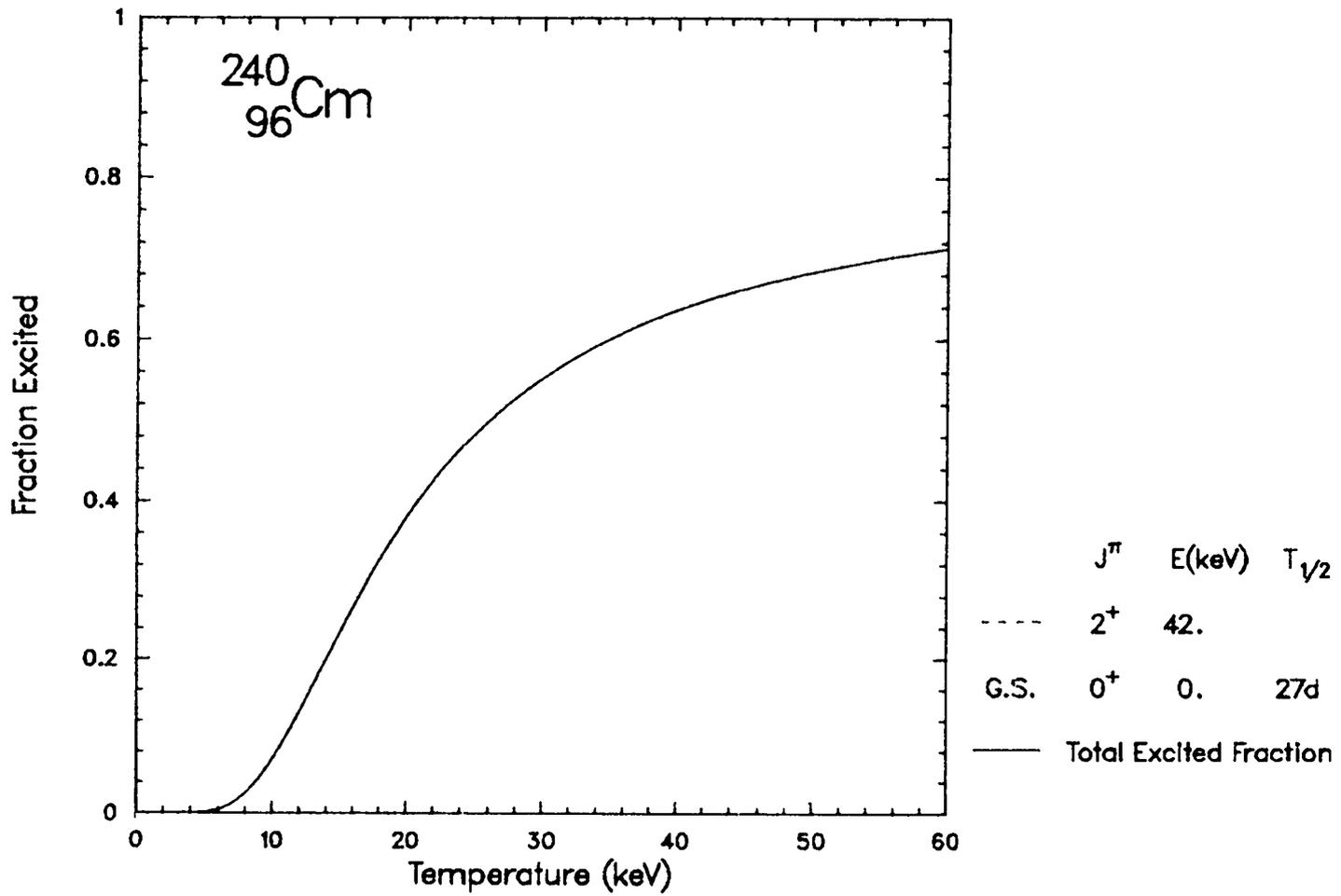


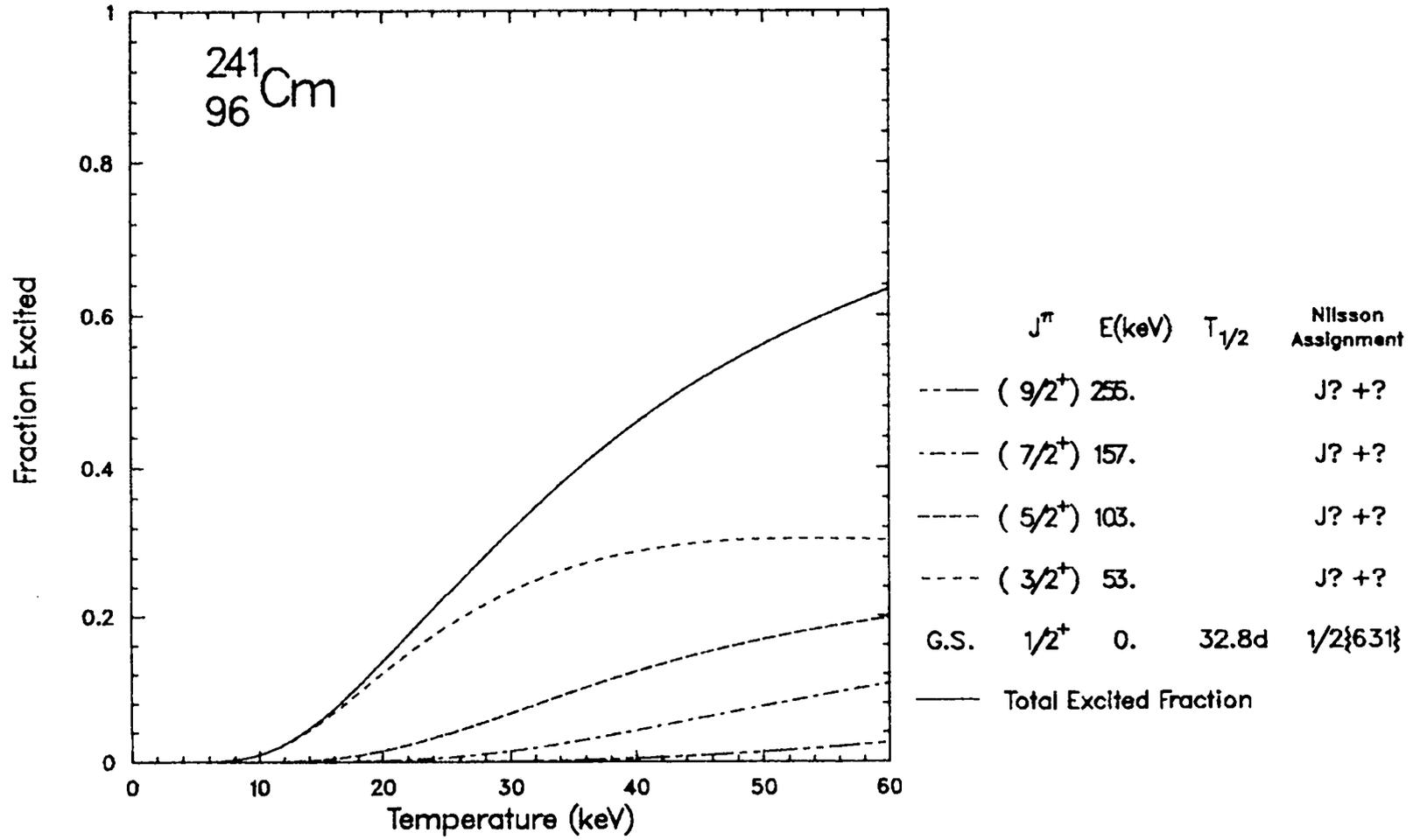
	J^π	E(keV)	$T_{1/2}$	Nilsson Assignment
---	$(11/2^-)$	190.82		
---	$(13/2^+)$	134.51		
---	$(9/2^-)$	124.59		
---	$(11/2^+)$	87.65		
---	$(7/2^-)$	70.43		
---	$(9/2^+)$	47.07		
---	$(5/2^-)$	27.93		$5/2\{523\}$
---	$(7/2^+)$	19.20		
G.S.	$(5/2^+)$	0.	2.05h	$5/2\{642\}$
---	Total Excited Fraction			

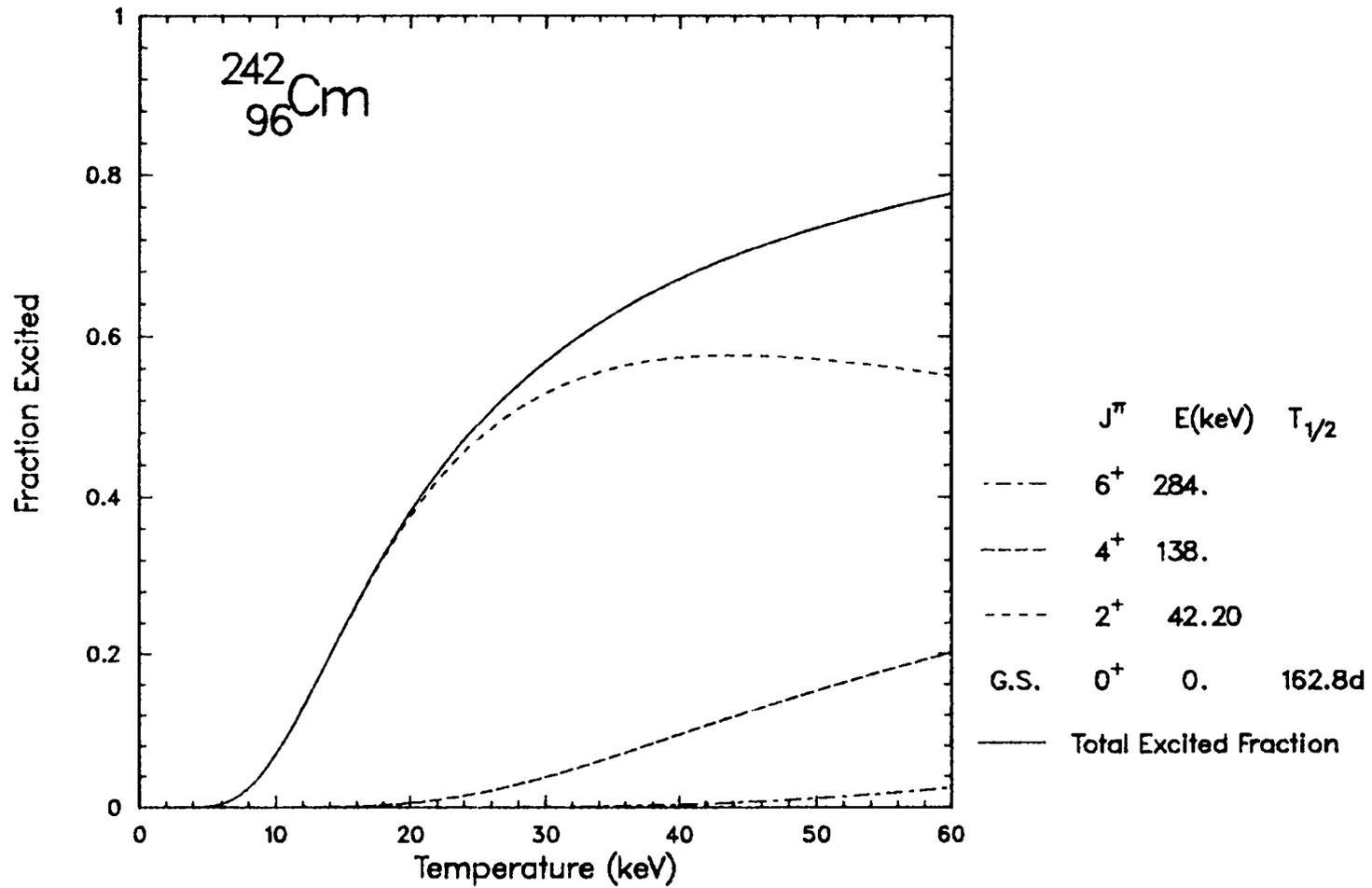


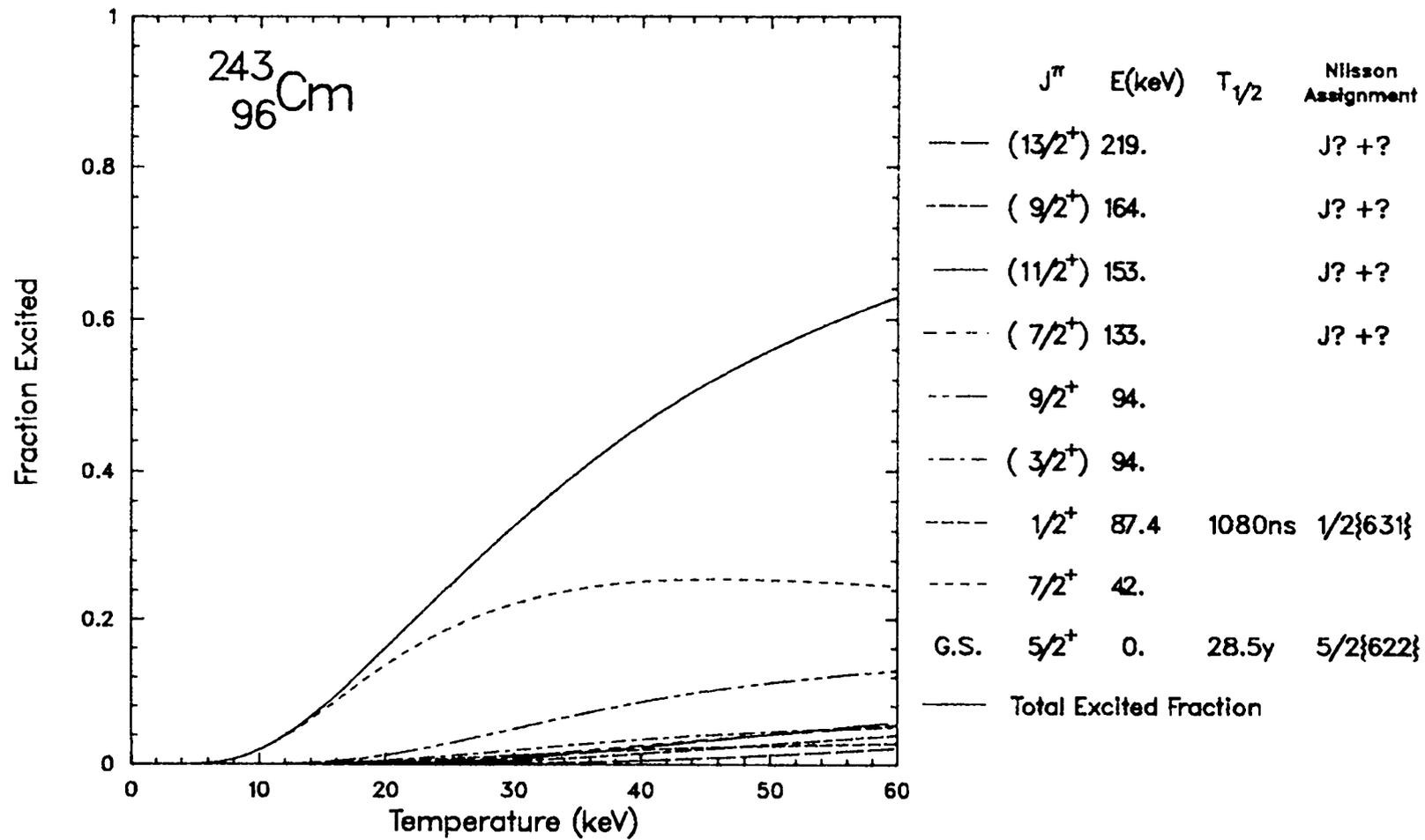


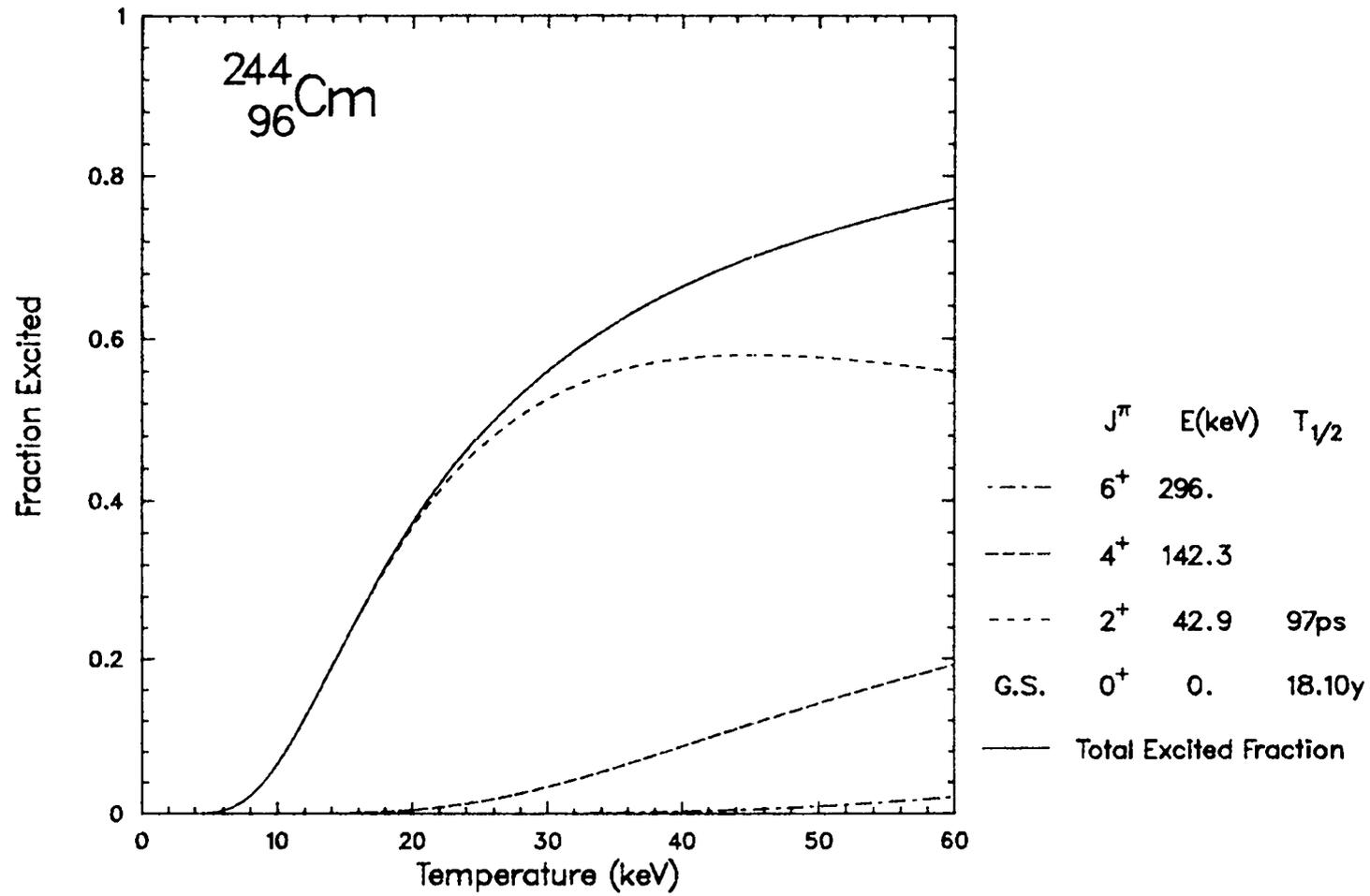


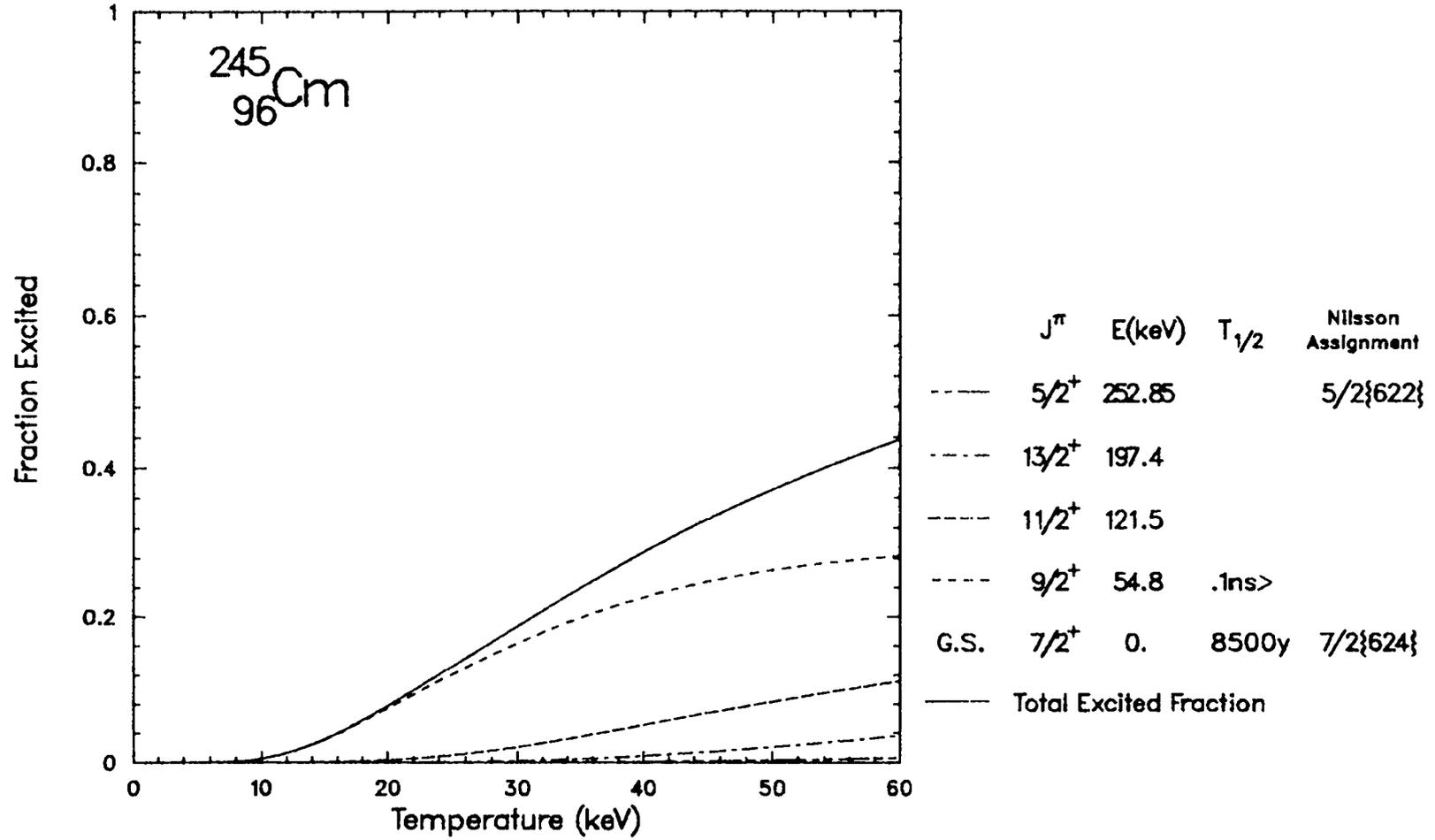


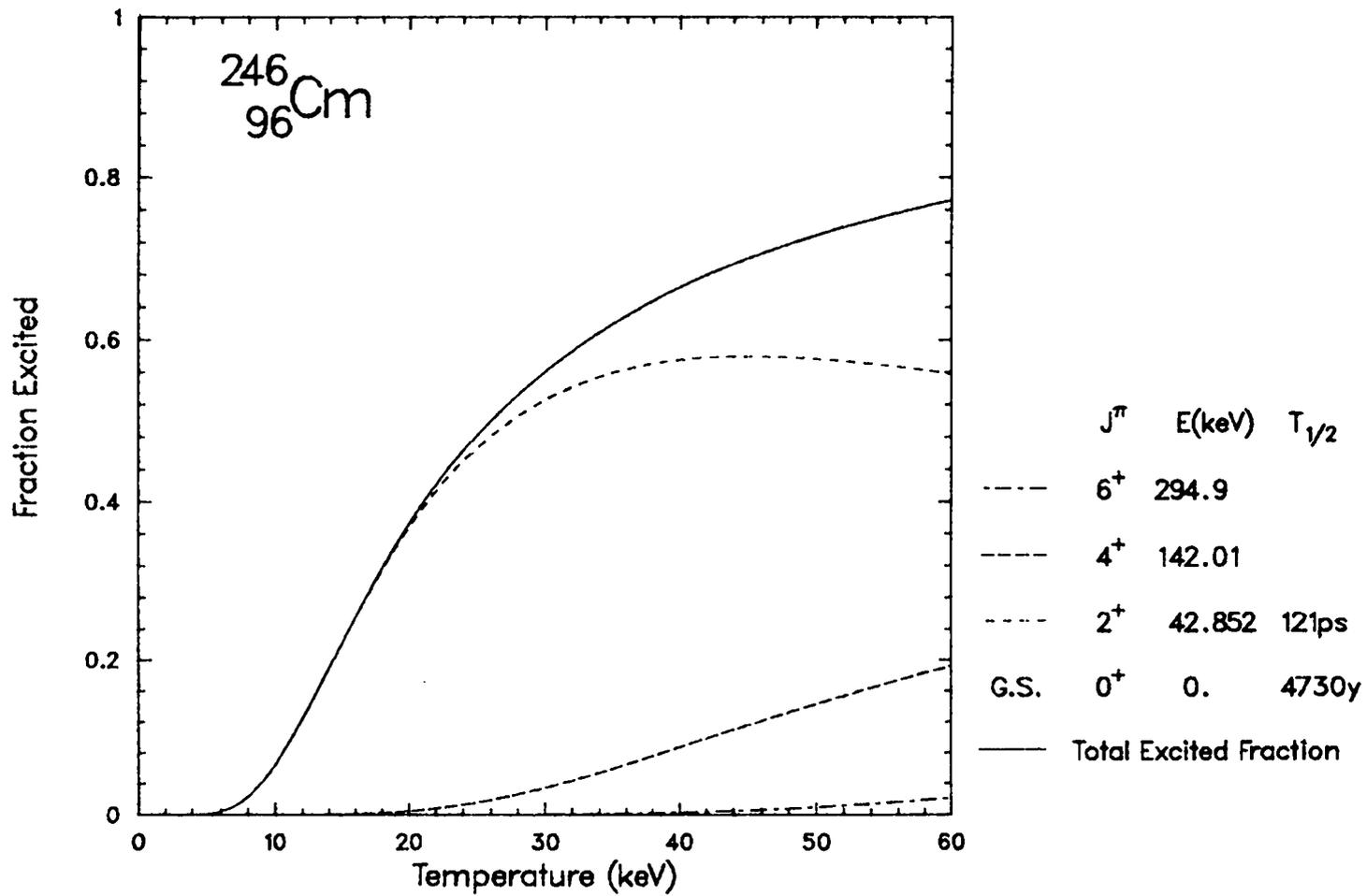


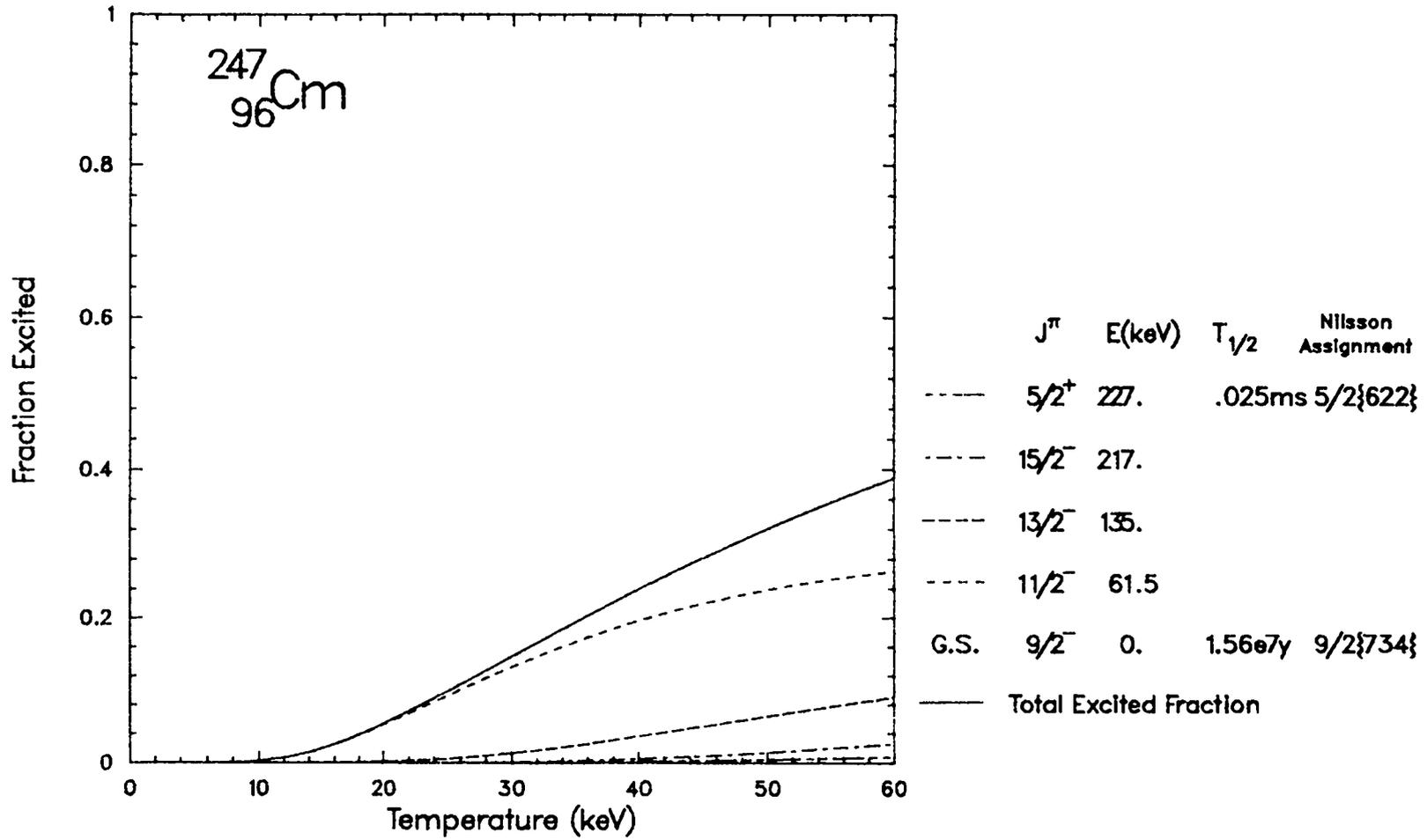


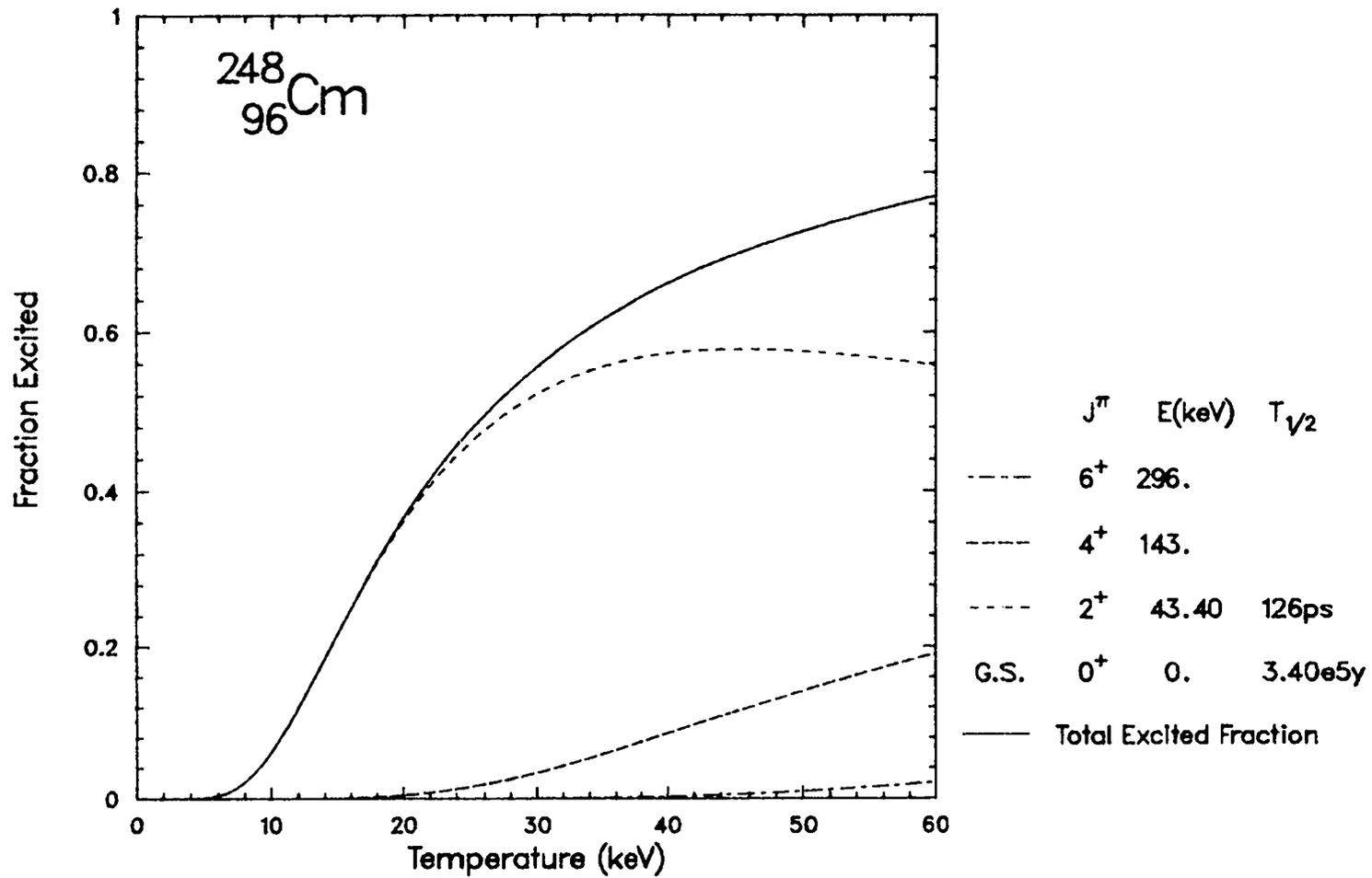


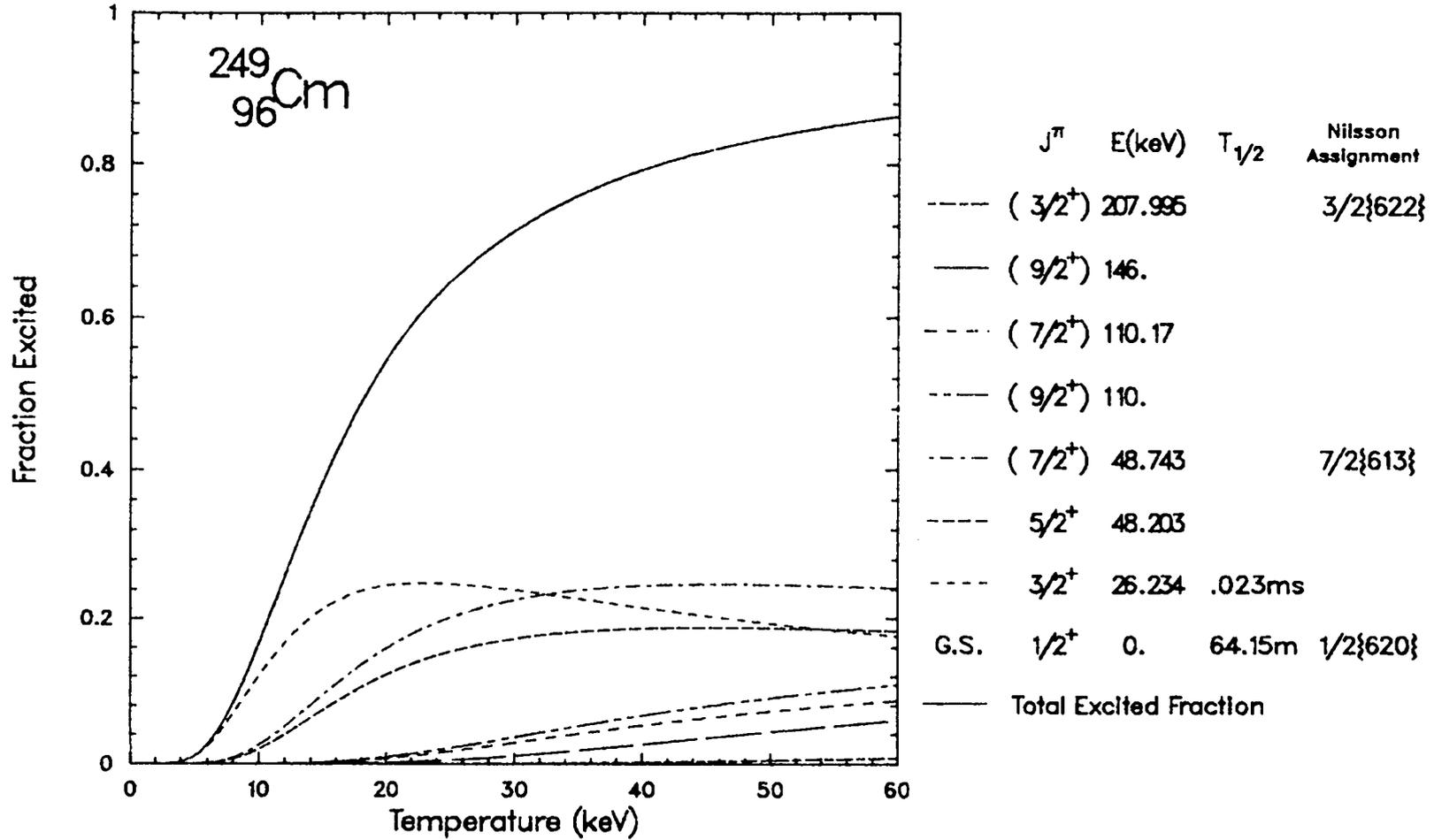


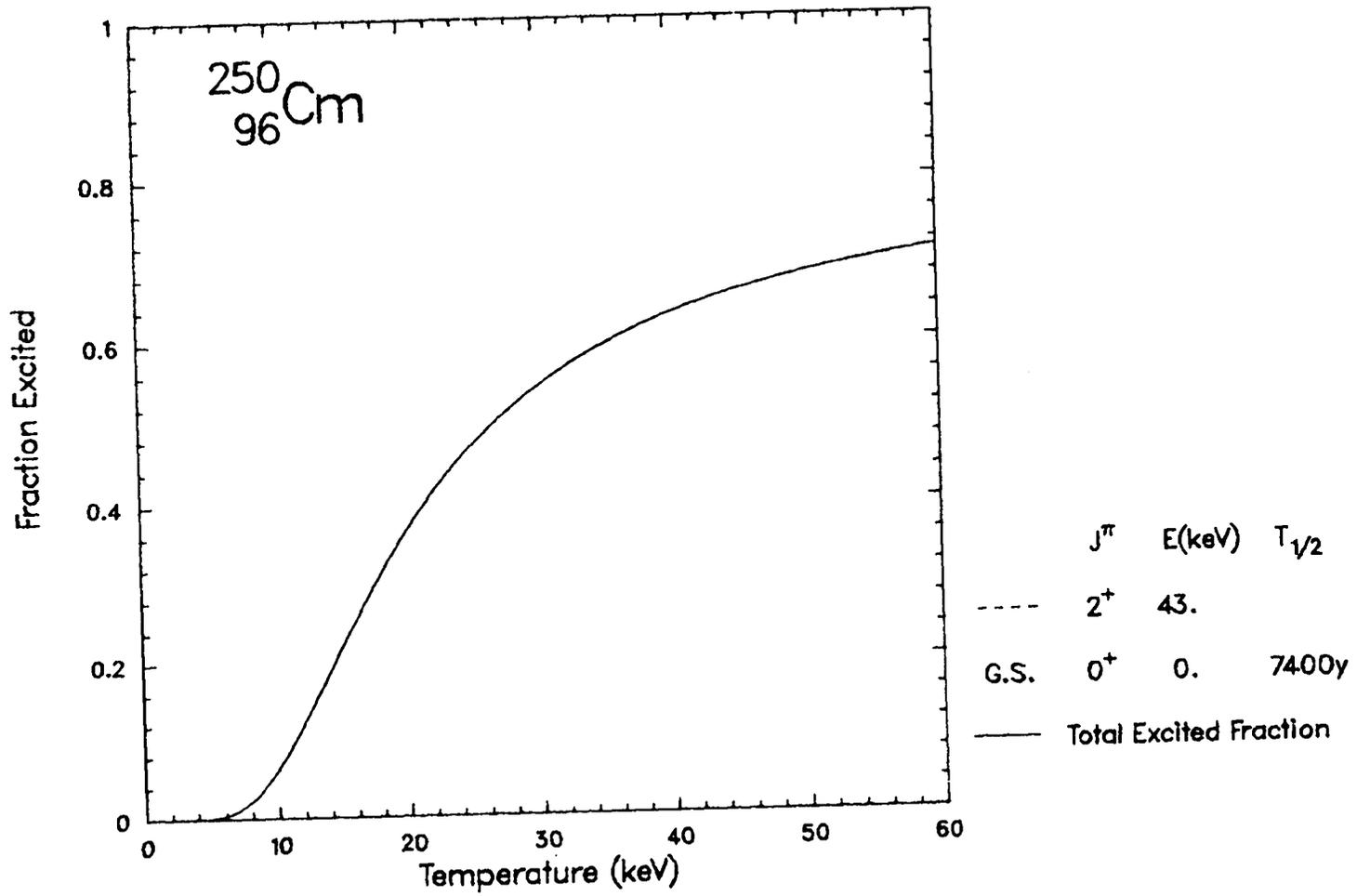


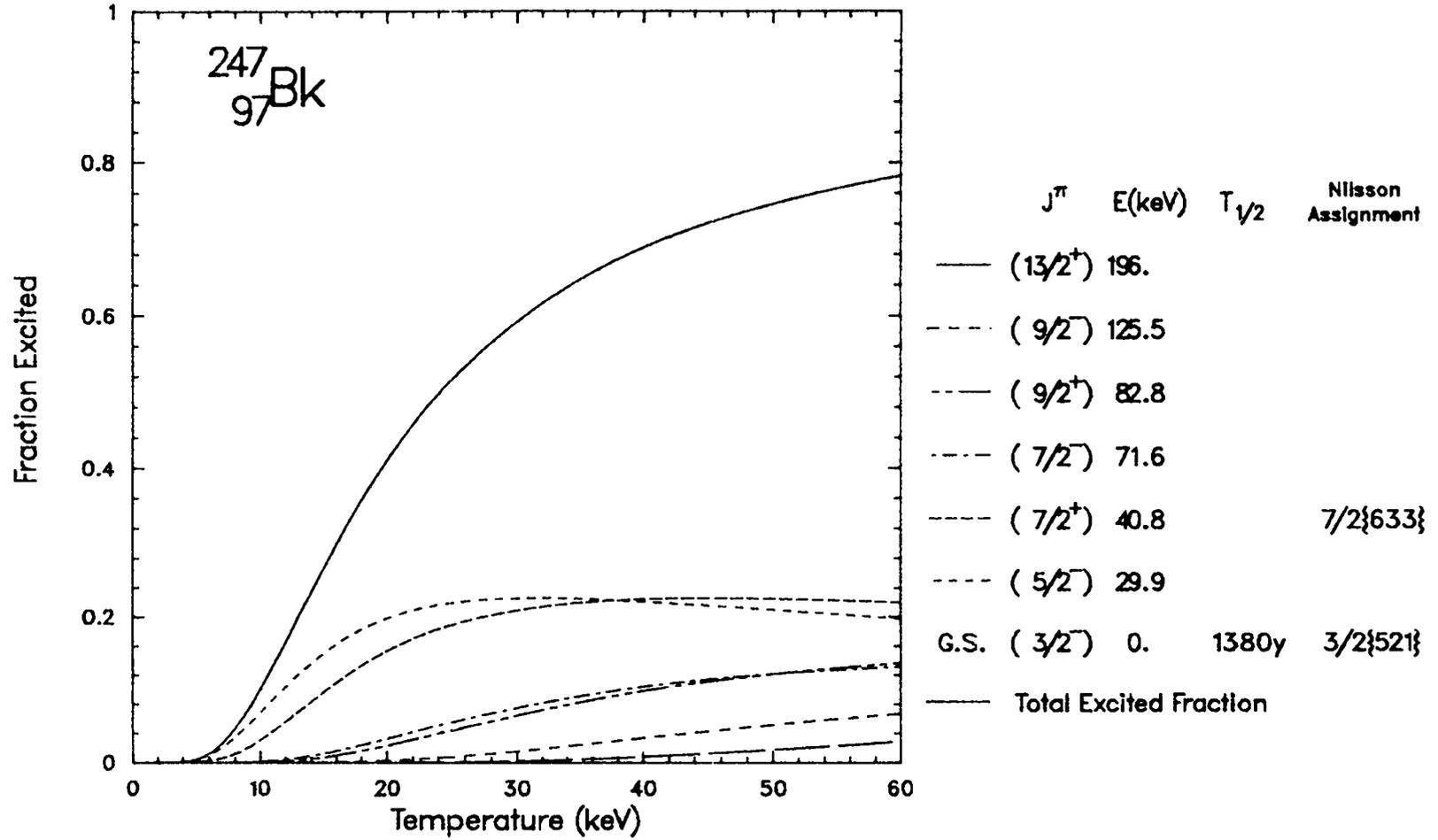


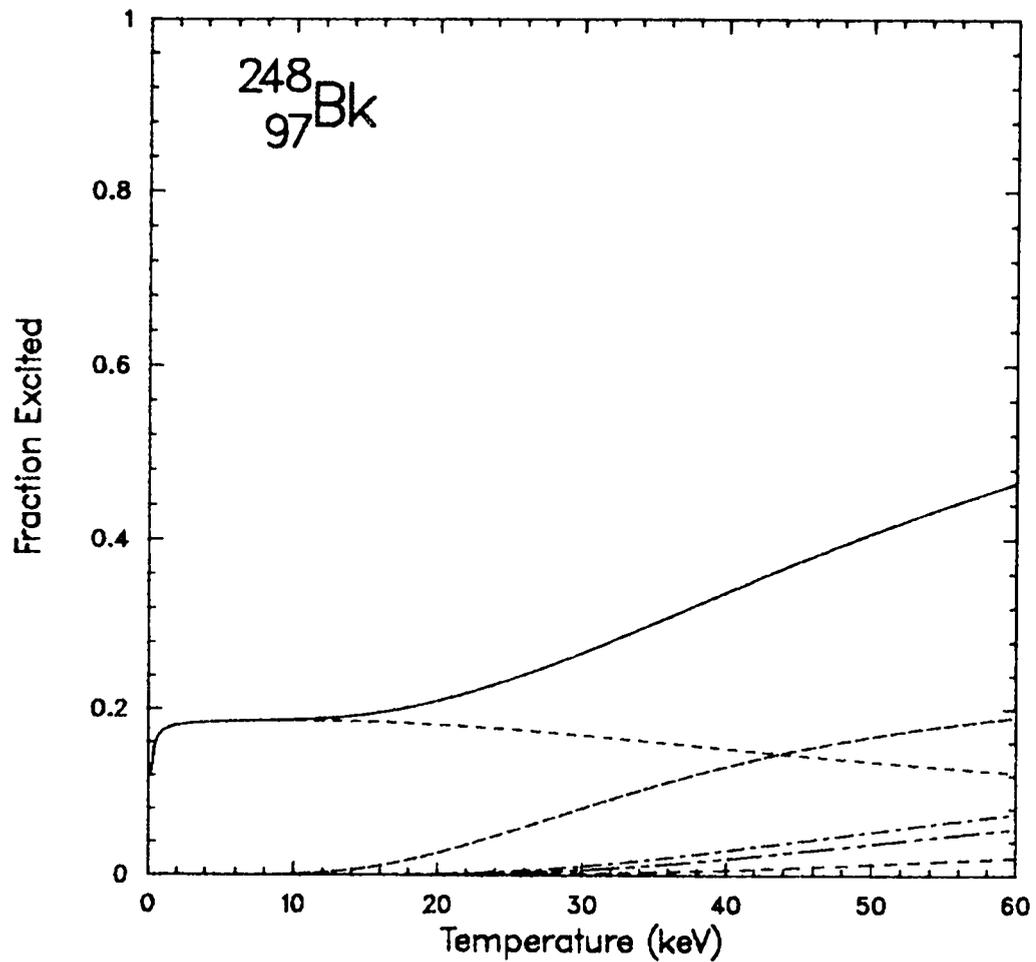






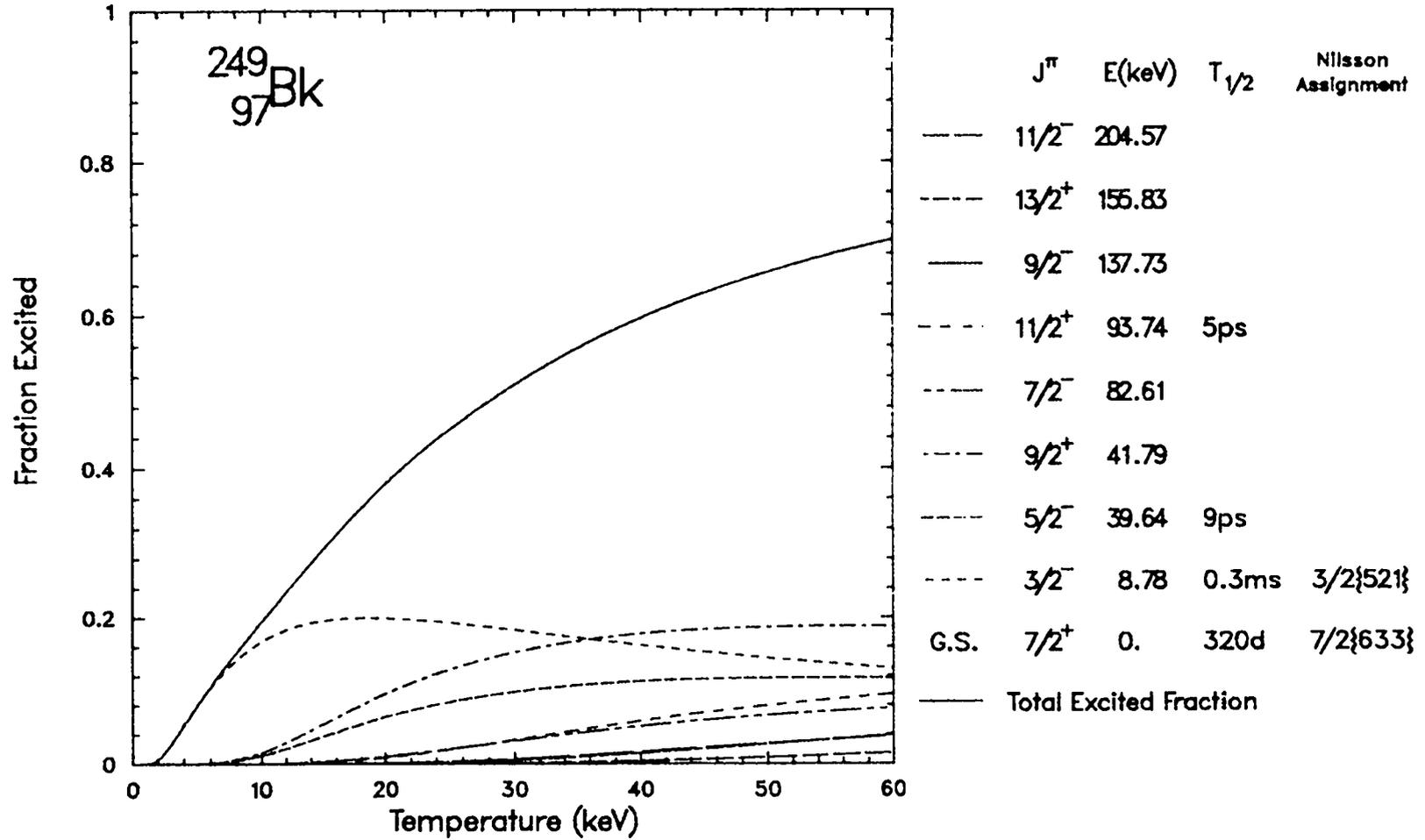


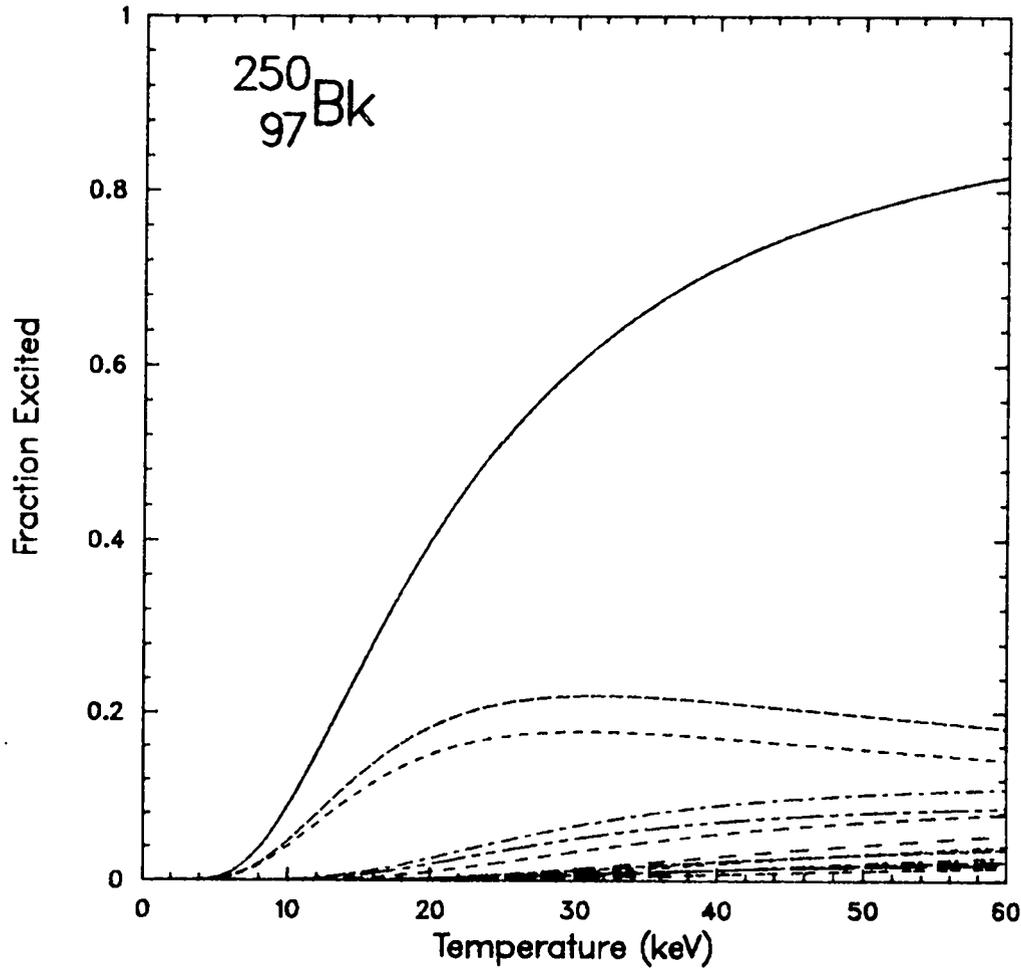




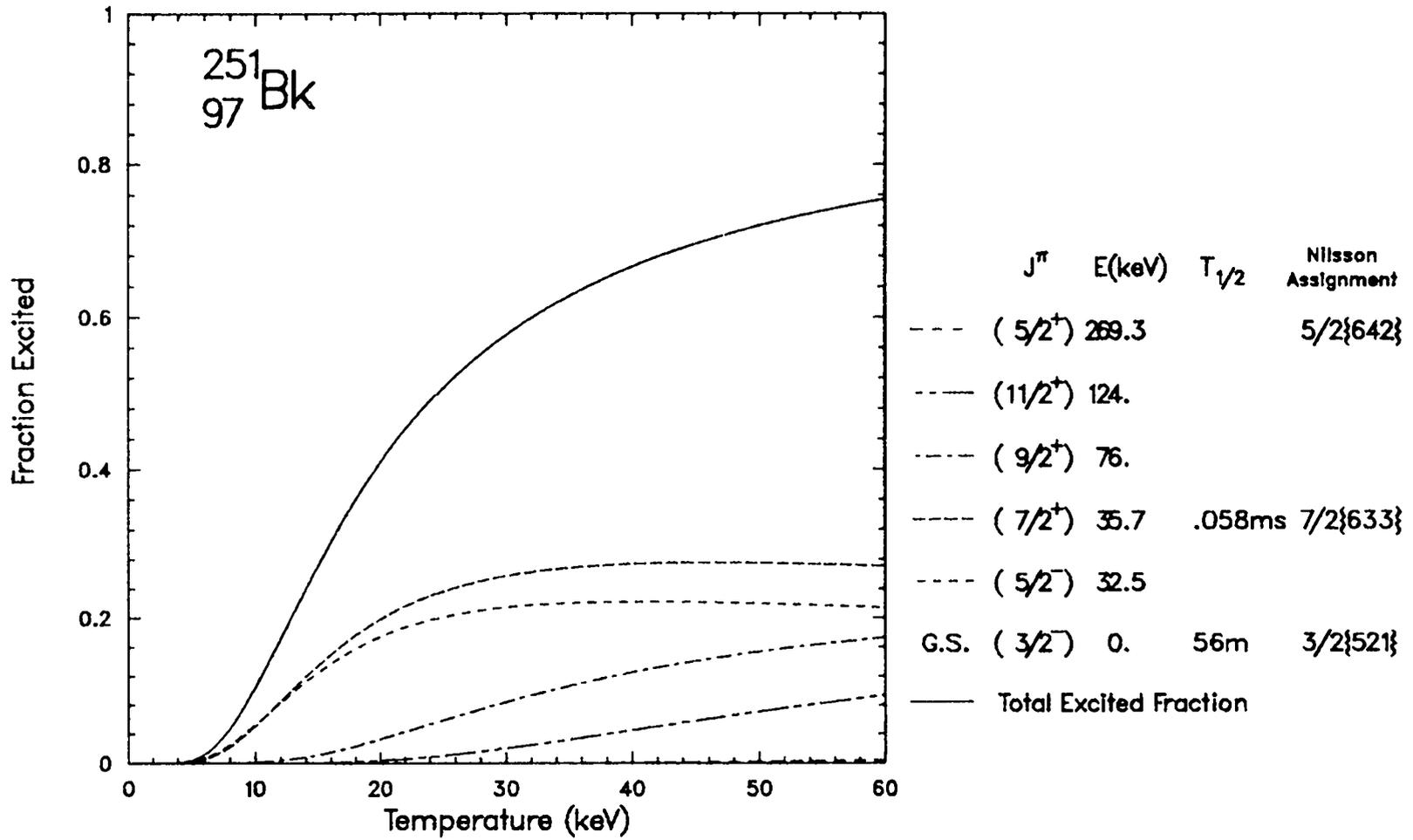
$^{248}_{97}\text{Bk}$

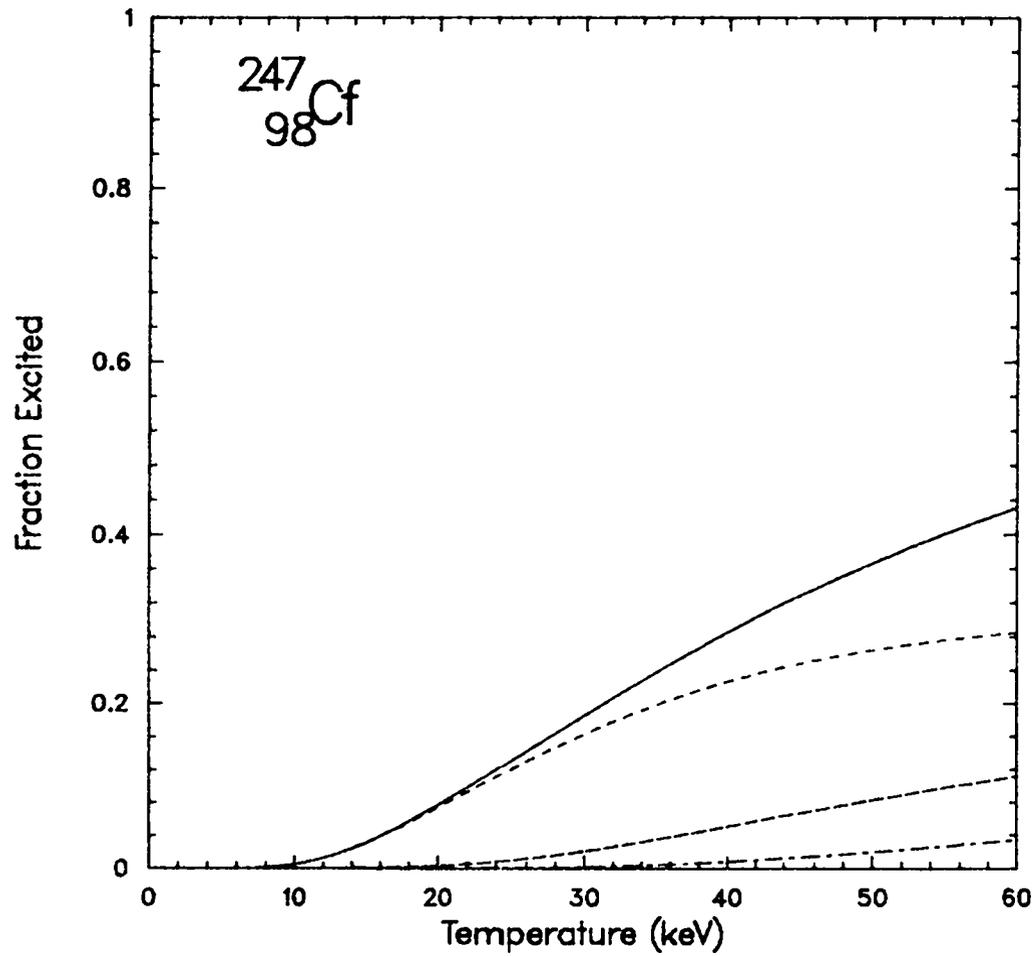
	J^π	E(keV)	$T_{1/2}$	Nilsson Assignment
---	$(4)^-$	171.5	J?	
---	$(8)^+$	151.32		
---	$(8)^-$	135.		
---	$(7)^+$	70.64		
---	$1^{(-)}$	0.1	23.7h	energy?
G.S.	$(6)^+$	0.	>9y	
—	Total Excited Fraction			



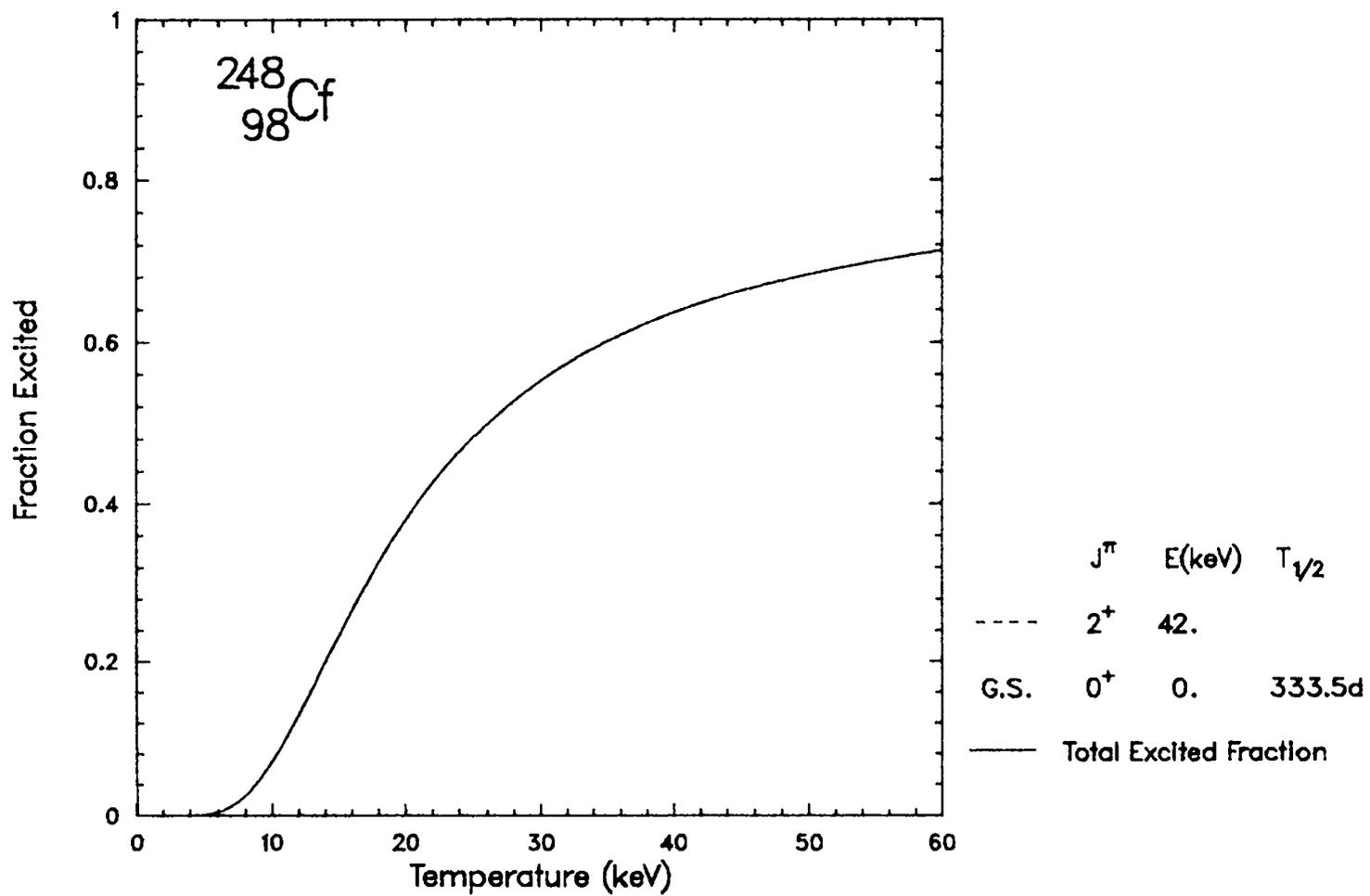


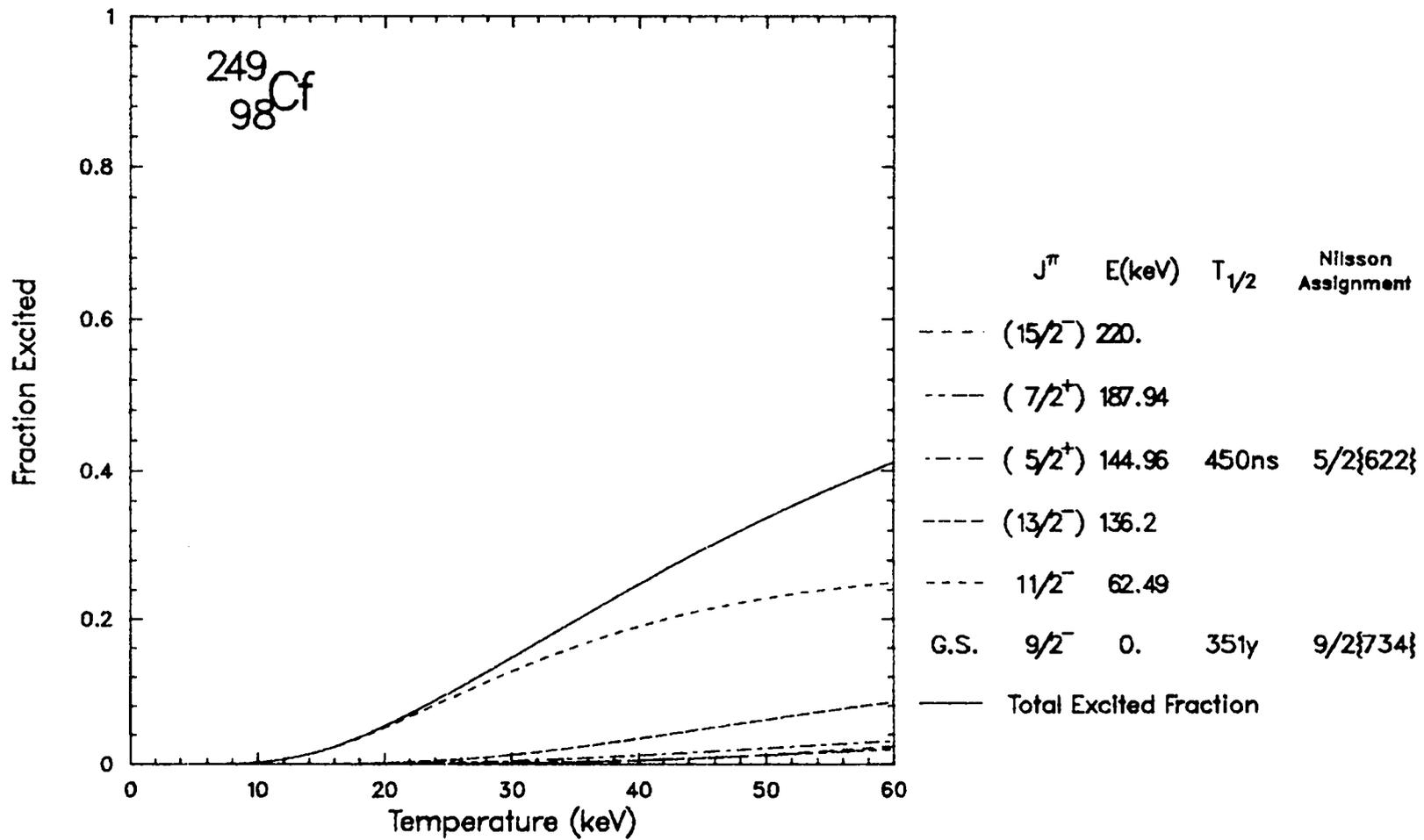
	J^π	E(keV)	$T_{1/2}$
----	4^+	148.595	
----	2^-	146.472	
----	5^-	137.32	
----	6^+	130.492	
----	2^-	125.007	
----	3^+	115.442	
----	1^-	103.828	
----	5^-	97.493	
----	4^-	80.258	38ns
----	5^+	78.326	.21ms
----	4^+	35.587	.029ms
----	3^-	34.472	
----	G.S.	2^-	0. 3.217h
----	Total Excited Fraction		

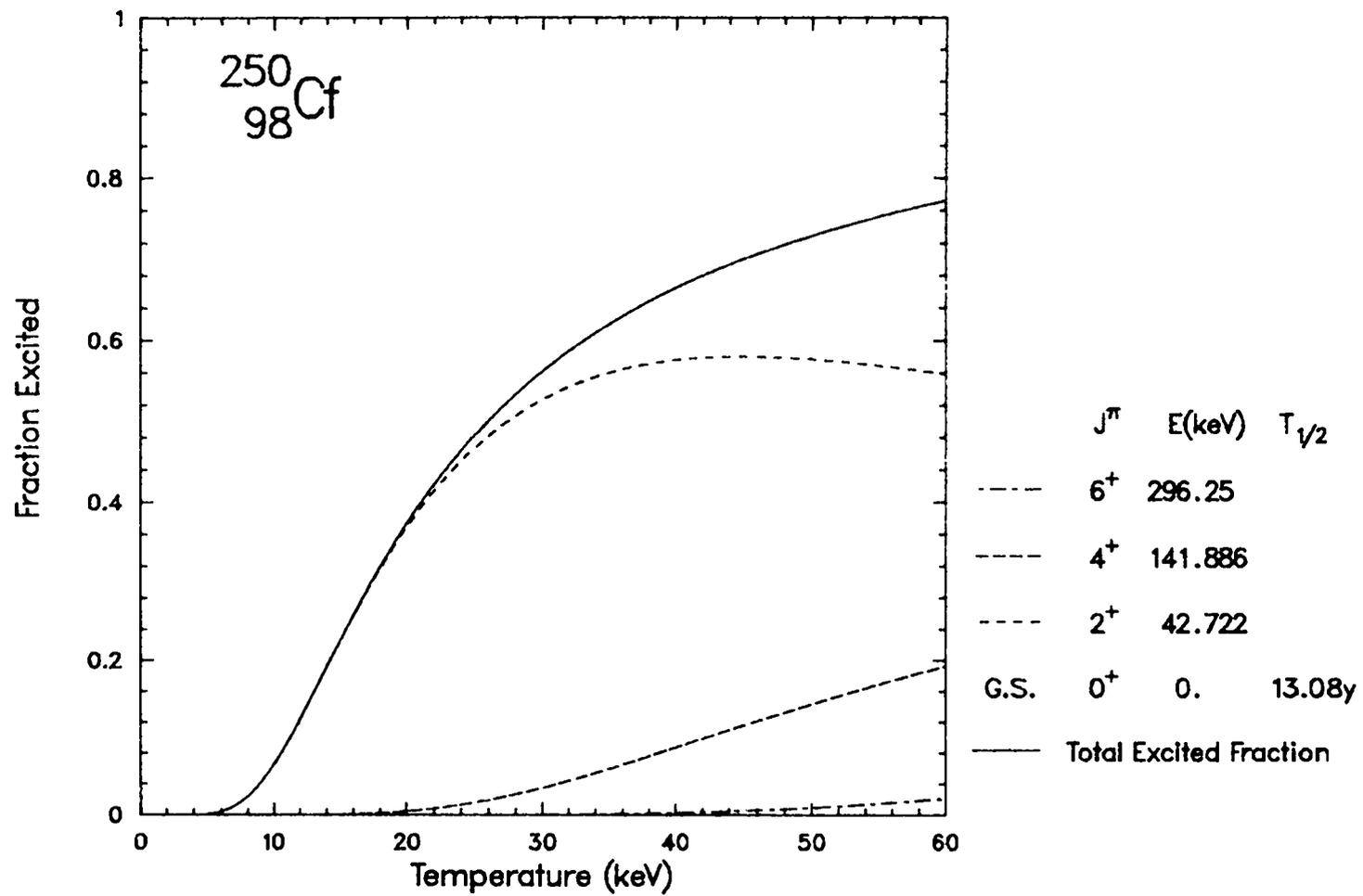


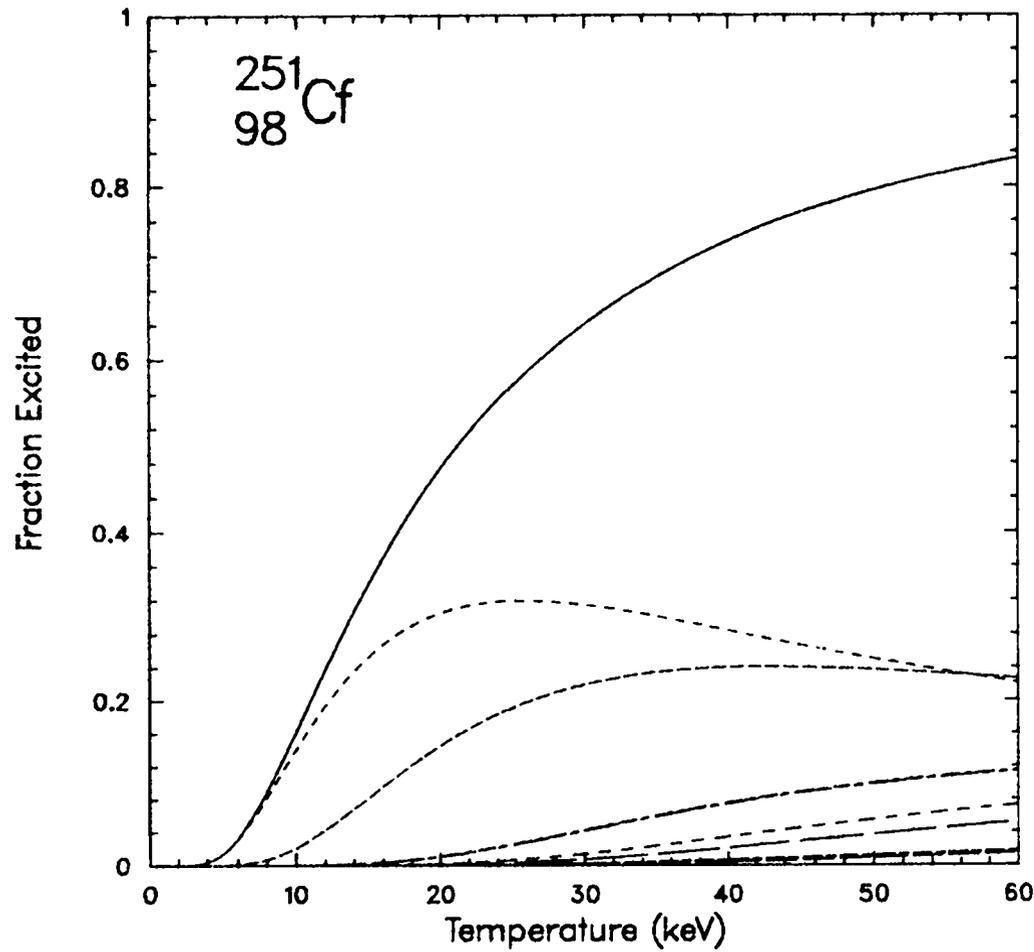


	J^π	E (keV)	$T_{1/2}$	Nilsson Assignment
---	(13/2 ⁺)	201.0		
---	(11/2 ⁺)	122.1		
---	(9/2 ⁺)	55.0		
---	G.S. (7/2 ⁺)	0.	3.11h	7/2{624}
—	Total Excited Fraction			



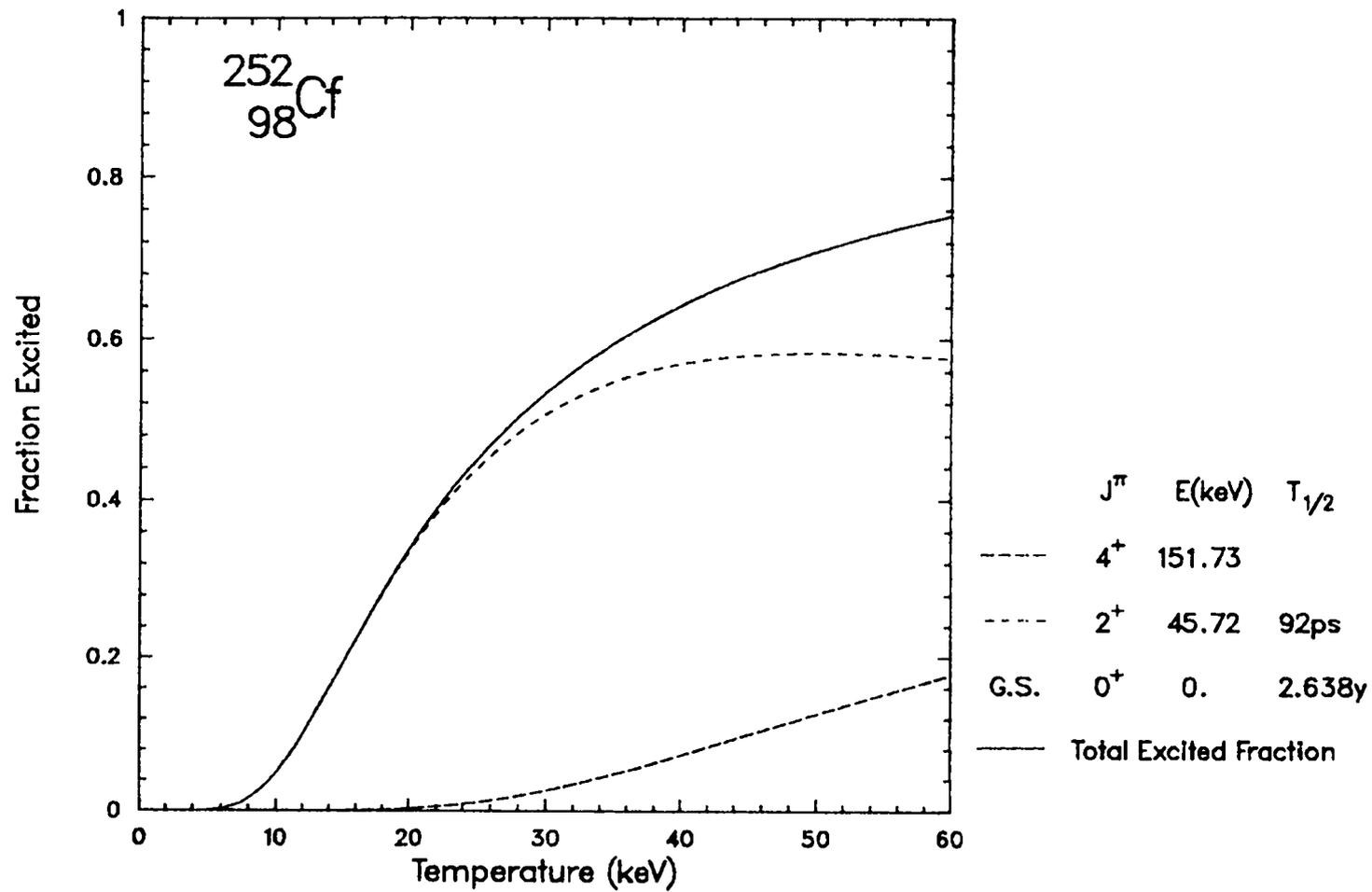


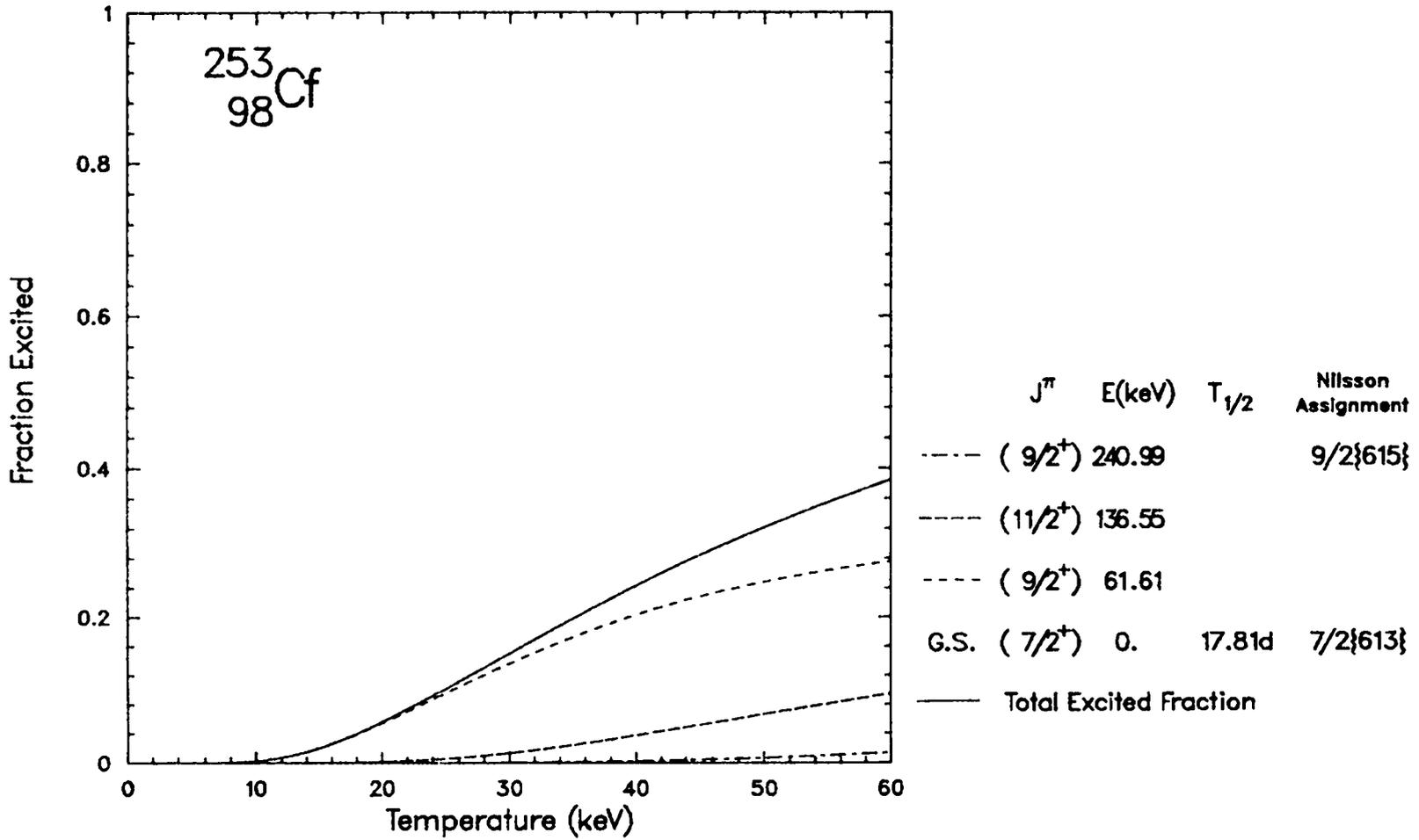




$^{251}_{98}\text{Cf}$

	J^π	E(keV)	$T_{1/2}$	Nilsson Assignment
---	$5/2^+$	211.72		
- - -	$3/2^+$	177.69		$3/2\{622\}$
—	$9/2^+$	166.31		
- - -	$9/2^+$	146.46		
- - -	$7/2^+$	106.304	38ns	$7/2\{613\}$
- - -	$7/2^+$	105.73		
- - -	$5/2^+$	47.828		
- - -	$3/2^+$	24.825		
G.S.	$1/2^+$	0.	898y	$1/2\{620\}$
—	Total Excited Fraction			





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