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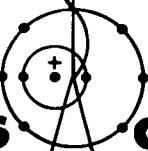
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Polynomial Solutions of the
Schrödinger Equation Applied to
Photon Cross Sections in Atoms



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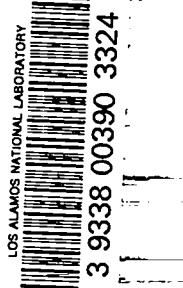
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Polynomial Solutions of the Schrödinger Equation Applied to Photon Cross Sections in Atoms

by

A. L. Merts
Walter Matuska, Jr.



POLYNOMIAL SOLUTIONS OF THE SCHRÖDINGER EQUATION APPLIED TO PHOTON CROSS SECTIONS IN ATOMS

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A. L. Merts and Walter Matuska, Jr.

ABSTRACT

Solutions of the Schrödinger equation with a realistic potential are carried out in detail. To check our methods, we have calculated a few bound-bound, bound-free, and free-free cross sections and compared our values with existing calculations and experimental data. These comparisons, along with a listing of the computer code in its bound-free form, are included.

I. INTRODUCTION

This report intends to show how the CDC-7600 code DEGA-A (Dense Electron Gas Approximation-Absorption) computes the bound-free, free-free, and bound-bound absorption coefficients, σ_{bf} , σ_{ff} , and σ_{bb} , respectively, as a function of photon energy, $h\nu$, from the given potential function $V(r)$ and the electron occupancy of the atom. Assuming $V(r)$ to be exact, the code will do its computation at any desired accuracy, within the machine limits, because the Schrödinger equation is solved using exact power-series expansions, not difference equations.

As the code is now written, any potential function can be used if it adheres to the three following requirements.

$$1. \lim_{r \rightarrow 0} V(r)r^2 = 0.$$

2. After some finite value of r , R_1 , the potential must be $V(r) = -|c|/r$.

3. $V(r)$ must be a negative, monotonically, increasing function.

Although it is not necessary to the internal structure of the code, we would also like $V(r)$ to be a function of temperature, density, and the atomic number of the atom.

Throughout this report, $[0, R_1]$ is called Region 1 and $[R_1, \infty]$ Region 2.

The following $V(r)$ is the one most often used in the code.

Experience has shown that a parameterized potential works well and gives energy levels close to those that Herman and Skillman¹ calculated using their Hartree-Fock-Slater method for isolated neutral atoms.

The potential form for an isolated atom is

$$V(r) = Ze/r(1 + \alpha r)^2 , \quad (1)$$

where $\alpha = 0.6057Z^{1/3}$. However, the form actually used in this report, which is also valid for a compressed atom, is

$$V(r) = -(Z^*e)/R_1 \left(\frac{R_1}{r} + \frac{r^2}{2R_1^2} - 3/2 \right) \quad (2)$$

for $r_0 \leq r \leq R_1$,

where

Z^* is the "effective number" of free electrons,

R_1 is the radius of the sphere representing the spherical atomic volume,

r_0 is the value of the radial distance for which Eq. (2) is equal to the value given in Eq. (3) below, and

e is the electronic charge.

In the inner region, the potential is given by

$$V(r) = -Ze/r(1 + \alpha r)^2 - Z^*e/r \left(\frac{r^2}{2R_1^2} - Bo \right) \quad (3)$$

for $0 \leq r \leq r_0$.

$$B_0 = \left(\frac{Z}{Z^*}\right) \left(\frac{R_1}{r_0}\right) / (1 + \alpha r_0)^2 - \frac{R_1}{r_0} + 3/2 . \quad (4)$$

$$Z^* = Z / (1 + \alpha r_0)^2 \left[\left(\frac{2\alpha r_0}{1 + \alpha r_0} \right) + 1 \right] . \quad (5)$$

After the form of the potential in the two regions is chosen, Eqs. (4) and (5) follow from the potential's continuity and its relation to charge density through Poisson's equation. In the potential outlined above, the value of R_1 is determined by the density of the material being considered. The value of Z^* is chosen by an iterative procedure so that at some finite temperature T , and for an atom occupying a spherical volume of radius R_1 , we have

$$Z = N(Z^*) = \int_0^{R_1} \left[\int_0^{\infty} n(r, T, P) dP \right] 4\pi r^2 dr , \quad (6)$$

where n is the Fermi-Dirac distribution function, representing the number of electrons at point r , having momentum between P and $P + dP$. Using Eq. (5) we have also determined r_0 .

We must correct the above potential for self-interaction. This is done in the simplest possible fashion. We replace Z in Eqs. (2) through (5) with $(Z-1)$ and add the term $-1/r$ to Eqs. (2) and (3). The potential for $r > R_1$ is defined as $-1/r$. This then represents our potential function used to calculate the one-electron energies and the one-electron orbitals from which we calculate the cross sections and f-values.

This potential can be shown to satisfy the three previously stated conditions.

The hydrogenic potential $V(r) = -1/r$ for $0 \leq r \leq \infty$ is often used to check parts of the code because analytic solutions for this potential are known.

The code considers the Schrödinger equation in the form

$$\varphi''(r) + \left[\lambda - 2V(r) - \frac{\ell(\ell+1)}{r^2} \right] \varphi(r) = 0, \quad 0 \leq r \leq \infty , \quad (7)$$

where

$\varphi(r)$ is the radial wave function (however, $\varphi(r)$ will be called the wave function throughout the rest of this report),

λ is the energy eigenvalue, and

ℓ is the angular-momentum quantum number.

Equation (7) has an infinite (in some cases finite, but large) number of discrete bound solutions (negative λ) commonly denoted by 1s, 2s, 2p, 3s, 3p, 3d, etc. Of this infinite sequence, we calculate only the solutions allowed by the electron occupancy. σ_{bb} can be evaluated only at discrete values of $h\nu$, because $h\nu = |\lambda_1 - \lambda_2|$ where λ_1 and λ_2 both represent bound solutions. By using a line profile, we then distribute each σ_{bb} over a narrow range of $h\nu$. However, every positive λ , given ℓ , is an eigenvalue for a free state. This allows us to choose any finite number of positive λ 's. Therefore, we can evaluate σ_{bf} at any energy $h\nu$ above the threshold, and σ_{ff} at any desired value of $h\nu$. Here $h\nu = |\lambda_1 - \lambda_2|$, λ_1 represents either a bound or a free solution, and λ_2 represents a free solution.

II. THE METHOD OF SOLUTION OF THE SCHRÖDINGER EQUATION

A. The Potential Approximation

To solve Eq. (7) on the computer, we choose a finite $R > R_1$ to approximate $r = \infty$, and divide $[0, R]$ into a finite number of intervals. For each of these intervals, r^2 times the potential is approximated by a parabola to some specified degree of accuracy, ξ . This series of fits is started at $r = 0$ with an interval of arbitrary length. In this first interval, we approximate the potential with

$$V(r) \approx c_1 + \frac{c_2}{r} + \frac{c_3}{r^2} . \quad (8)$$

Let r_1 be the left end point of this interval, r_3 the right end point, and r_2 the midpoint. To evaluate the c 's, we solve the set of equations

$$c_1 r_j^2 + c_2 r_j + c_3 = V(r_j) r_j^2 \text{ for } j = 1, 2, 3. \quad (9)$$

These equations have no difficulty at $r = 0$, and they fit the potential exactly at r_1 , r_2 , and r_3 . Because $V(r)$ is a smooth, monotonic function, we can check our fit by checking the validity of

$$|c_1 + \frac{c_2}{r} + \frac{c_3}{r^2} - V(r)| \leq |V(r)| \xi \quad (10)$$

at several points between r_1 and r_3 . If this inequality is not satisfied for all points, we decrease the length of the interval until inequality [Eq. (10)] is satisfied for all points checked. This process is continued until Region 1 is complete. Here c_1 , c_2 , and c_3 should actually be

thought of as $c_{1,i}$, $c_{2,i}$, and $c_{3,i}$, where the subscript i denotes the i th interval.

In Region 2, obviously, $c_2 = -1$ and $c_1 = c_3 = 0$. The lengths of the intervals in this region are governed only by an additional condition discussed later. This condition applies to all intervals.

As the code now exists, for a given set of conditions, all solutions to the Schrödinger equation are found by using the same set of intervals over Region 1; however, each solution has its own set of intervals in Region 2. The code could also be written so that each solution would have its own set of intervals over the entire range of r . It would be impractical to require all solutions to have the same set of intervals in Region 2 because the maximum interval lengths allowed for the various solutions in Region 2 are so different.

B. The Expansion of the Radial Wave Function

In the expansion of the wave function, we will need the condition $c_{3,1} = 0$. This is satisfied if the first requirement on the potential is met.

We assume the wave function to have the form

$$\varphi(r) = \sum_{j=1}^{\infty} a_{ji} r^{j-1} \text{ for } i = 1 \quad (11)$$

in the first interval. Dropping the subscript i , we substitute the power series and its second derivative for $\varphi(r)$ and $\varphi''(r)$ and the approximation for $V(r)$ in Eq. (8) into the Schrödinger equation to get

$$\begin{aligned} & \left\{ -[2c_3 + \ell(\ell + 1)] a_1 \right\} / r^2 \\ & + \left\{ -2c_2 a_1 - [2c_3 + \ell(\ell + 1)] a_2 \right\} / r \\ & + \sum_{j=3}^{\infty} \left\{ (\lambda - 2c_1) a_{j-2} - 2c_2 a_{j-1} \right. \\ & \left. + [(j-2)(j-1) - 2c_3 - \ell(\ell + 1)] a_j \right\} r^{j-3} = 0 \quad . \end{aligned} \quad (12)$$

Here we assume that $c_3 = 0$ and $a_j = 0$ for $1 \leq j \leq \ell + 1$. Also $a_{\ell+2}$ is arbitrary because any constant times a solution eigenfunction $\varphi(r)$ is still a solution. As each term in Eq. (12) must be zero for every r in the interval, we now have the recursion relation

$$a_j = \frac{2c_2 a_{j-1} - (\lambda - 2c_1) a_{j-2}}{(j-2)(j-1) - \ell(\ell + 1)} \quad \text{for } j > \ell + 2 \quad . \quad (13)$$

The power-series expansions in all other intervals are also expanded about one of the interval's end points. If expanding about the left end point, we make the substitution $d = r - \rho_i$ and require that $0 \leq d \leq \rho_{i+1} - \rho_i$ where the ρ 's are the end points of the intervals. When it is necessary to expand about the right end point, the roles of ρ_i and ρ_{i+1} are switched and $\rho_i - \rho_{i+1} \leq d \leq 0$. Again omitting the subscript i , the Schrödinger equation can now be written as

$$(\rho^2 + 2\rho d + d^2)\varphi''(d) + (B_1 + B_2 d + B_3 d^2)\varphi(d) = 0 \quad ,$$

where

$$B_1 = b_1 \rho^2 + b_2 \rho + b_3$$

$$B_2 = 2b_1 \rho + b_2$$

$$B_3 = b_1$$

and

(14)

$$b_1 = \lambda - 2c_1$$

$$b_2 = -2c_2$$

$$b_3 = -[2c_3 + \ell(\ell + 1)] \quad .$$

Here we assume the wave function to have the form

$$\varphi(d) = \sum_{j=1}^{\infty} a_{ji} d^{j-1} \text{ for } i > 1 \quad . \quad (15)$$

Substituting the power series and its second derivative for $\varphi(d)$ and $\varphi''(d)$, we get

$$\begin{aligned} & [2\rho^2 a_3 + B_1 a_1] + [6\rho^2 a_4 + 4\rho a_3 + B_1 a_2 + B_2 a_1] d \\ & + \sum_{j=5}^{\infty} [(j-2)(j-1)\rho^2 a_j + (j-3)(j-2)2\rho a_{j-1} \\ & + (j-4)(j-3)a_{j-2} + B_1 a_{j-2}] d^{j-3} = 0 \quad . \end{aligned} \quad (16)$$

with the subscript i omitted. Again, because each term of Eq. (16) must be zero for all values of d , we have the recursion relations

$$a_3 = -B_1 a_1 / 2\rho^2$$

$$a_4 = -(B_2 a_1 + B_1 a_2 + 4\rho a_3) / 6\rho^2$$

$$a_j = -\left\{ B_3 a_{j-4} + B_2 a_{j-3} + [B_1 + (j-4)(j-3)] a_{j-2} \right. \\ \left. + 2(j-3)(j-2)\rho a_{j-1} \right\} / (j-2)(j-1)\rho^2$$

for $j > 4$

(17)

when a_1 and a_2 are known.

We can easily show that $a_1 = \varphi(d)$ and $a_2 = \varphi'(d)$ at $d = 0$. Therefore, a_1 and a_2 will always be known by the right-boundary condition or can be evaluated with the power-series expansion of the wave function in the previous interval.

In practice, we start with $a_j = 0$ for $1 \leq j \leq l+1$ and a_{l+2} an arbitrary nonzero constant to start the power-series expansion in the first interval. Then we evaluate this power-series and its first derivative at its right end point. This determines a_1 and a_2 for the second interval. This process is repeated until we reach some \hat{r} , $0 < \hat{r} < R$, where we evaluate $\varphi_f(\hat{r})$ and $\varphi'_f(\hat{r})$; the determination of \hat{r} is discussed later. At the right boundary, R , $\varphi(R)$, and $\varphi'(R)$ are given by the boundary condition. This enables us to start our successive power-series expansions at R and work our way backward to \hat{r} where we evaluate $\varphi_b(\hat{r})$ and $\varphi'_b(\hat{r})$. We have a solution when $\varphi_f(\hat{r}) = \varphi'_b(\hat{r})$ for $\varphi_f(\hat{r}) = \varphi_b(\hat{r})$. $\varphi_f(\hat{r})$ is simply the value of the wave function at \hat{r} found by forward expansions, and $\varphi_b(\hat{r})$ is the value of the same wave function at \hat{r} found by backward expansions.

C. Determination of the Expansion Interval Length

In real life, these power series can have only a finite number of terms. The maximum number of terms in the present code is 50. This leads to the other condition regulating the maximum length of a particular interval. Let us define

$$\tilde{V}(r) = \left[\lambda - 2V(r) - \frac{\ell(\ell+1)}{r^2} \right] \quad (18)$$

Using this definition, we can write the Schrödinger equation as

$$\varphi''(r) \pm h^2 \varphi(r) = 0, \text{ where } h^2 = \pm \tilde{V}(r) \quad (19)$$

choosing the sign so that $h^2 > 0$. If h is assumed to be constant locally, the solution is either

$$\varphi(r) = Ae^{-hr} + Be^{hr} \quad (20)$$

or

$$\varphi(r) = A \sin hr + B \cos hr, \quad (21)$$

depending upon the sign. Expanding the decreasing exponential solution in a Taylor series about an end point of the interval, we get

$$\varphi(r) = Ae^{-hr_i} \sum_{j=0}^{\infty} (-1)^j \frac{(h\Delta r)^j}{j!} \quad (22)$$

where $\Delta r = r - r_i$ is the maximum allowable interval length. With this series, we can estimate the largest value of $(h\Delta r)$ that allows the series to converge to a specified accuracy in the allotted number of terms. In Region 1, all solutions are considered in estimating the maximum interval length; however, in Region 2 only one solution at a time is considered. The code then plugs the largest encountered value of h into

$$\Delta r = \frac{C}{h} . \quad (23)$$

This C is an input parameter, and for a 50-term expansion and 8-place accuracy a conservative value for C is 6.

The sinusoidal and increasing exponential solutions have a series similar to Eq. (22), and the interval length is also estimated by Eq. (23).

D. Finding the Join Point \hat{r} for Forward and Backward Integration

Let us consider the question of stability. Here again, Eqs. (20) and (21) can be thought of as local solutions to the Schrödinger equation. If an error is introduced in Eq. (20) during forward integration (increasing r) when the first term is the desired solution, this error will grow exponentially. However, any error introduced will diminish exponentially during backward integration. Likewise, when the second term is the desired solution, backward integration is unstable and forward integration causes any error to diminish exponentially. Equation (21) is considered stable for integration in either direction. Any error introduced into the integration will not grow exponentially; however, once an error is introduced it cannot be diminished as was the case with Eq. (20). Figure 1 shows the regions of stable and unstable integration for the four possible combinations of given conditions.

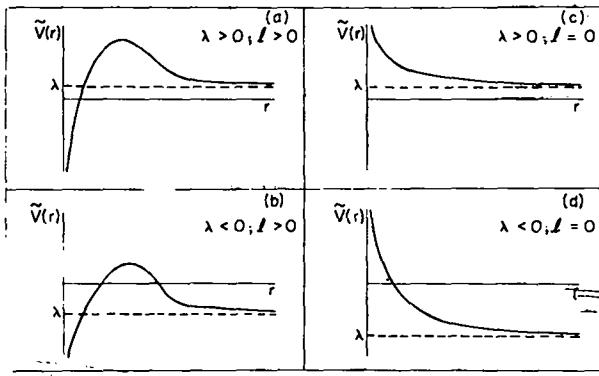


Fig. 1.

Integration is stable in both directions for $\tilde{V}(r) > 0$; integration is stable in only one direction for $\tilde{V}(r) < 0$. λ indicates the asymptotic limit of $\tilde{V}(r)$.

For the cases shown in Figs. 1a and 1b, \hat{r} is chosen such that $\tilde{V}(\hat{r})$ is the maximum value of $\tilde{V}(r)$. For the case shown in Fig. 1c, \hat{r} is the center of the rightmost interval, and for the case shown in Fig. 1d, \hat{r} is chosen such that $\tilde{V}(\hat{r}) = 0$. For positive λ , the value of λ is known and is used to find \hat{r} ; however, for negative λ one has only a maximum and minimum guess at its value at this stage, so the minimum guess is used in evaluating \hat{r} .

E. Boundary Condition at R

1. Bound States—Negative λ . The two right-boundary conditions used in the code are discussed below; however, this method of solving the Schrödinger equation is not limited to these two conditions. For the bound state, the Schrödinger equation becomes

$$\varphi''(r) - |\lambda|\varphi(r) = 0 \text{ as } r \rightarrow \infty . \quad (24)$$

Note that this is true only in Region 2. Because $\varphi(R)$ is arbitrary and

$$\varphi(r) = Ae^{-\sqrt{|\lambda|}r} \quad (25)$$

is the desired solution to Eq. (24), we derive the boundary condition

$$\varphi'(R) = -\sqrt{|\lambda|}\varphi(R) . \quad (26)$$

Although we have no exact relation between R and the accuracy desired, we regulate R by the following method. First, we find the largest root of $\tilde{V}(r)$. R is then taken as some constant (typically 25) times this root. Then, after

the Schrödinger equation is solved using this R , we check the validity of

$$|\varphi(r)|_{\max} < \gamma|\varphi(R)| \quad (27)$$

(10^{-15} is a typical value for γ). If this condition is not satisfied, we simply keep increasing R until it is. A quick method for getting a value near $|\varphi(r)|_{\max}$ is to check $\varphi(r)$ at the end points of the intervals.

2. Free States—Positive λ . The sinusoidal condition given by Carson, Mayers, and Stibbs² is used on the right boundary in the free case. This boundary condition also applies only in Region 2.

For large r , the solution may be written

$$\varphi(r) = M(r) \cos [kr + \delta(r)] \quad (28)$$

in which $k = \sqrt{\lambda}$,

$$\lim_{r \rightarrow \infty} M(r) = M,$$

and

$$\lim_{r \rightarrow \infty} \frac{\delta(r)}{r} = 0 .$$

M fixes the scale of the solution. We shall require the normalization $M = \sqrt{2/\pi k}$.

In Region 2 where $V(r) = -c/r$ for $c > 0$, we assume a solution of the form

$$\varphi(r) = A(r) \cos \left(kr + \frac{c}{k} \ln r \right) + B(r) \sin \left(kr + \frac{c}{k} \ln r \right) . \quad (30)$$

Now substitute Eq. (30) into the Schrödinger equation. Then asymptotic expansions for $A(r)$ and $B(r)$ exist in the form

$$A(r) = \sum a_n / r^n, \quad B(r) = \sum b_n / r^n , \quad (31)$$

where

$$a_{n+1} = \left\{ \left[\ell(\ell+1) + \frac{c^2}{k^2} - n(n+1) \right] b_n - \frac{c}{k} (2n+1)a_n \right\} / 2k(n+1)$$

$$b_{n+1} = \left\{ \left[n(n+1) - \frac{c^2}{k^2} - \ell(\ell+1) \right] a_n - \frac{c}{k} (2n+1)b_n \right\} / 2k(n+1) \quad (32)$$

and

$$a_0 = M, b_0 = 0 . \quad (33)$$

The sums in Eq. (31) are only semiconvergent. Therefore $A(r)$ and $B(r)$ must be evaluated at an r large enough that the sums converge to the desired accuracy.

Equation (30) can also be written as

$$\varphi(r) = M(r) \cos \theta(r) , \quad (34)$$

where

$$M(r) = \sqrt{A(r)^2 + B(r)^2} \quad (35)$$

and

$$\theta(r) = kr + \frac{c}{k} + \ln r + \tan^{-1} \left[\frac{A(r)}{B(r)} \right]$$

The asymptotic series expansion for the solution of $\varphi(r)$ given by Eq. (34) is uniquely determined up to some constant phase α_q ; therefore, we can write

$$\varphi(r) = M(r) \cos [\theta(r) + \alpha_q] , \quad (36)$$

instead of Eq. (34), and we also have

$$\begin{aligned} \varphi'(r) &= M'(r) \cos [\theta(r) + \alpha_q] \\ &- M(r)\theta'(r) \sin [\theta(r) + \alpha_q] . \end{aligned} \quad (37)$$

For sufficiently large R , $\varphi(R)$ and $\varphi'(R)$ are the desired right-boundary conditions. The guesses at R may have to be increased several times before Eq. (31) is satisfied.

The phase α_q is determined by an iteration process that is explained later.

III. DETERMINATION OF THE EIGENVALUES AND PHASE FACTORS

A. The Eigenvalue

As stated previously, for the bound state, λ is varied until we find a $[\varphi(\lambda, r), \lambda]$ that solves the Schrödinger equation. We start with a minimum and a maximum guess at λ . This difference in λ is divided into a specified number of logarithmically equal λ -intervals. We define

$$F(\lambda) = \frac{\varphi_b(\lambda, \hat{r})}{\varphi_f(\lambda, \hat{r})} \varphi'_f(\lambda, \hat{r}) - \varphi'_b(\lambda, \hat{r}) \quad (38)$$

at the end points of these λ -intervals and look for a sign change in $F(\lambda)$ in each. If we detect a sign change in an interval, we use the Regula Falsa³ method to find the root of $F(\lambda)$ in that interval. As $F(\lambda)$ also changes sign through poles, we check to reject these intervals.

When we find a $[\varphi(\lambda, r), \lambda]$ solution, we must determine whether it is the desired one for specified quantum numbers n and ℓ , where $\ell \leq n - 1$. We have the desired solution when

$$I = n - \ell - 1 , \quad (39)$$

where I is the number of roots in $\varphi(r)$. I is found using a Sturm Sequence.³ If Eq. (39) is not satisfied, we reject this solution and continue our search. The value of λ so obtained is called the eigenvalue.

B. Phase Determination

In the free state, λ is specified and the phase α_q at the right boundary is varied over the range $0 \leq \alpha_q \leq \pi$ until we find a $[\varphi(\alpha_q, r), \alpha_q]$ that solves the Schrödinger equation. To find this solution, we again use the Regula Falsa method to find the root of $F(\alpha_q)$ where

$$F(\alpha_q) = \frac{\varphi_b(\alpha_q, \hat{r})}{\varphi_f(\alpha_q, \hat{r})} \varphi'_f(\alpha_q, \hat{r}) - \varphi'_b(\alpha_q, \hat{r}) . \quad (40)$$

Here, we need not check for poles or unwanted solutions as was necessary for the bound states.

C. Normalization

Even though the wave functions need not be normalized to be solutions to the Schrödinger equation, they must be normalized to produce correct absorption coefficients. We define $\varphi(r)$ as normalized when, for bound states:

$$\int_0^{\infty} \varphi(r) \varphi(r) dr = 1 , \quad (41)$$

and, for free states:

$$\int_0^{\infty} \varphi_{\lambda} \varphi'_{\lambda} dr = \delta(\lambda - \lambda') . \quad (42)$$

The free states have this normality built into the right-boundary condition. However, for each bound state, we evaluate

$$\int_0^{\infty} \varphi(r)\varphi(r) dr = \beta^2 , \quad (43)$$

and the normalized wave function is then $\varphi(r)/\beta$. Equation (43) is evaluated by polynomial multiplication and integration over each interval of r .

IV. EVALUATION OF MATRIX ELEMENTS

Now that we have found all of the necessary solutions to the Schrödinger equation, we compute the matrix elements, H_{mn} , used in evaluating the absorption coefficients. The matrix elements are found by

$$H_{mn} = 2 \int_0^{\infty} \varphi_m(r) \frac{\partial V(r)}{\partial r} \varphi_n(r) dr , \quad (44)$$

where m and n refer to eigen solutions of the Schrödinger equation. If one wave function is bound and the other is free, H_{mn} is used in evaluating σ_{bf} . Likewise, if both are bound, the result is σ_{bb} , and if both are free, the result is σ_{ff} .

Equation (44) is evaluated by summing the integrals calculated in each expansion interval. Because $\partial V(r)/\partial r$ decreases as r^{-2} and $\varphi(r)$ decreases exponentially for bound states, this integral converges rapidly to a specified accuracy at some finite value of r , provided at least one $\varphi(r)$ represents a bound state. However, if both wave functions represent free states, the convergence is much slower, because each bound wave function asymptotically approaches a constant amplitude. Here, convergence is achieved only through the r^{-2} decrease in $\partial V(r)/\partial r$.

In the first interval we have

$$\frac{\partial V(r)}{\partial r} = -c_{2,i} r^{-2} , \quad (45)$$

multiplied by the polynomial representations of $\varphi_m(r)$ and $\varphi_n(r)$ that can be integrated easily. In the rest of the intervals, we have

$$\frac{\partial V(d)}{\partial d} = -\frac{c_{2,i}(\rho_i + d) + 2c_{3,i}}{(\rho_i + d)^3} , \quad (46)$$

which, by continued long division, can be written as a converging power series in d when $|d/\rho_i| < 1$. Now, multiplying these three polynomials, we get a polynomial that can be integrated easily.

V. EXAMPLES

A. Bound-Free Absorptions

In the code, λ , r , $V(r)$, and H_{mn} are dimensionless parameters. Both λ and $V(r)$, when multiplied by one Rydberg, are energies expressed in Rydbergs, and r , when multiplied by one Bohr radius, is a length expressed in Bohr radii.

The bound-free absorption coefficient is given by

$$\sigma_{bf}(hv) = 10.756 \times 10^6 \sum \frac{\ell_{\max} H_{mn}^2 \eta}{|\lambda_m - \lambda_n|^3 g} , \quad (47)$$

where

ℓ_{\max} is the maximum of ℓ_m and ℓ_n .

η is the number of electrons in the bound state that can make this transition.

g is the maximum possible degeneracy given by $2(2\ell + 1)$ for the ℓ of the bound state.

Here λ_m , λ_n , and H_{mn} are dimensionless numbers and σ_{bf} is expressed in barns per atom. Also when $hv = 13.605 |\lambda_m - \lambda_n|$, hv is expressed in electron volts. The sum in Eq. (47) is over all possible bound-free transitions at the given hv .

Figures 2 through 7 show examples of bound-free absorptions for cold, normal-density beryllium, carbon, aluminum, iron, copper, and lead as computed by DEGA-A. In these figures, the continuous line was computed by DEGA-A and the X's are experimental data given by Storm and Israel.⁴ In Fig. 5, the three experimental points at the m edge for iron were given by Carter and Givens.⁵ In Fig. 4, DEGA-A was compared with calculations by Barfield, Koontz, and Huebner⁶ for aluminum at low photon energies.

Even though the bound-free cross sections have been computed down to the lowest edge in these examples, we make no claims about the accuracy of the copper and lead cross sections at these low photon energies.

None of the cross sections in this report include electron spin or relativistic effect.

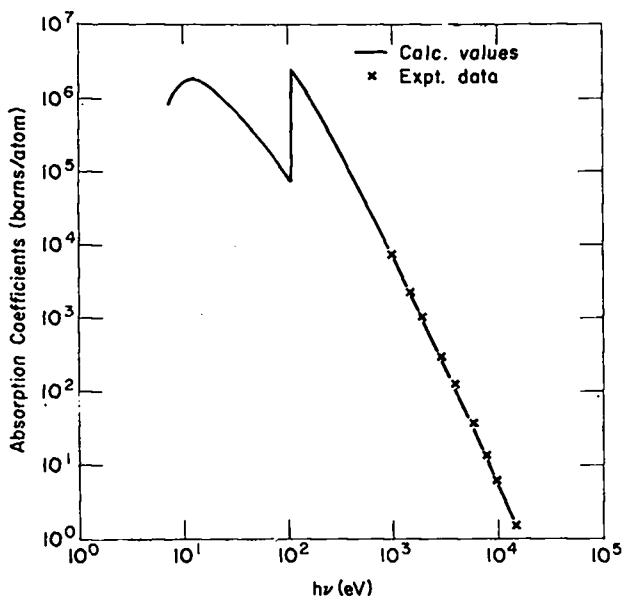


Fig. 2.

Bound-free absorption coefficients for cold, normal density (1.845 g/cm^3) Be. ($Z = 4$, $r_0 = 1.406$, $R_1 = 2.355$)

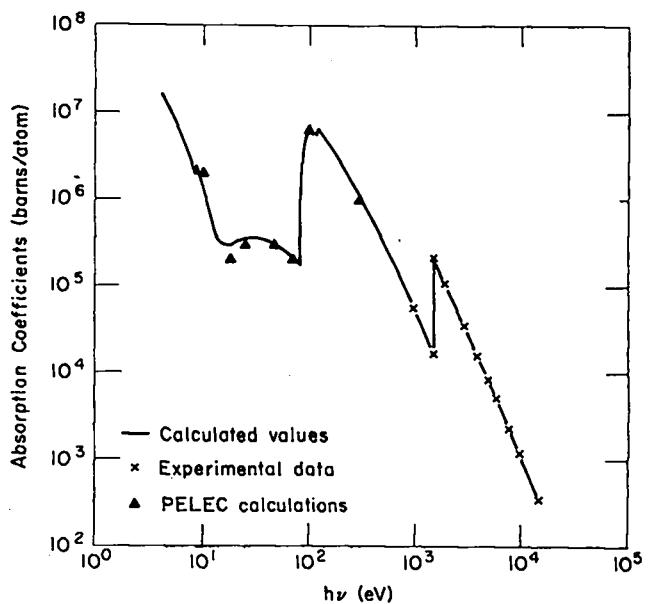


Fig. 4.

Bound-free absorption coefficients for cold, normal density (2.699 g/cm^3) Al. ($Z = 13$, $r_0 = 1.699$, $R_1 = 2.990$)

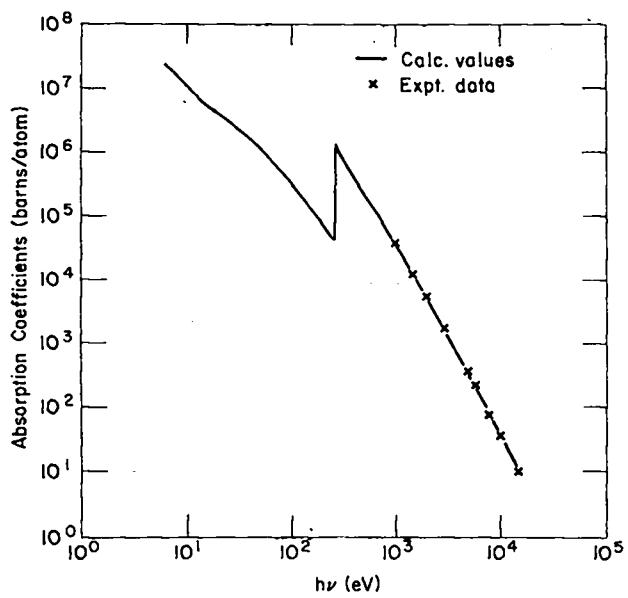


Fig. 3.

Bound-free absorption coefficients for cold, normal density (2.25 g/cm^3) C. ($Z = 6$, $r_0 = 1.442$, $R_1 = 2.426$)

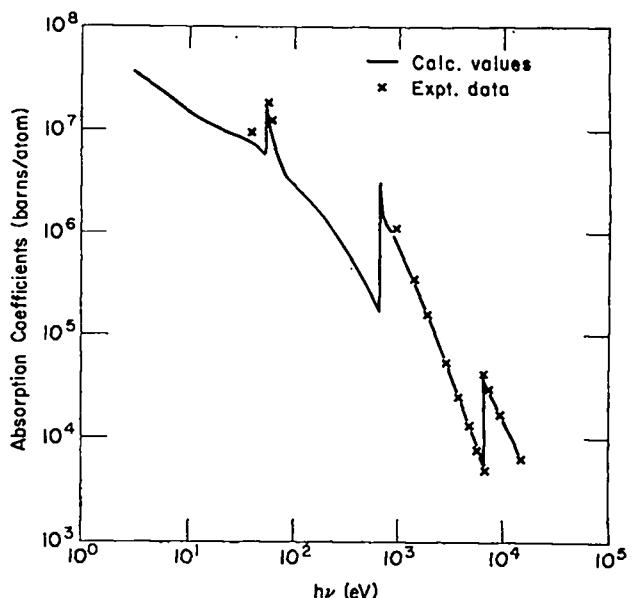


Fig. 5.

Bound-free absorption coefficients for cold, normal density (7.85 g/cm^3) Fe. ($Z = 26$, $r_0 = 1.512$, $R_1 = 2.670$)

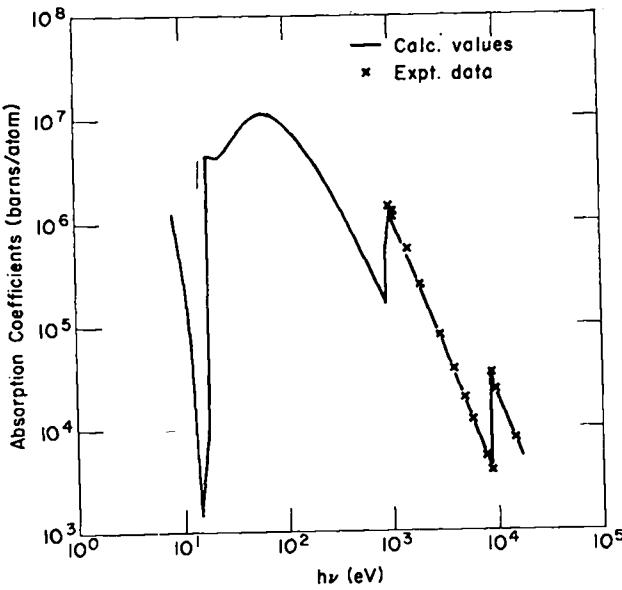


Fig. 6.
Bound-free absorption coefficients for cold, normal density (8.89 g/cm^3) Cu. ($Z = 29$, $r_0 = 1.517$, $R_1 = 2.674$)

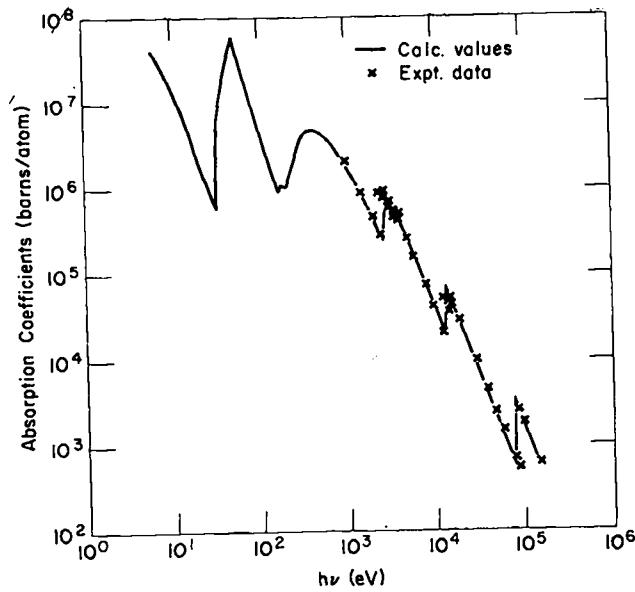


Fig. 7.
Bound-free absorption coefficients for cold, normal density (11.34 g/cm^3) Pb. ($Z = 82$, $r_0 = 2.003$, $R_1 = 3.656$)

B. Bound-Bound Absorptions

In checking the bound-bound case, we consider hydrogen, lithium, beryllium, sodium, potassium, and strontium. A formula similar to Eq. (47) can be derived for $\sigma_{bb}(hv)$.² However, because the data found in the literature⁷ appeared in a different form, we used the formula

$$\tau = \frac{4H_{mn}^2}{|\lambda_m - \lambda_n|^4 (4\ell_{max}^2 - 1)} \quad (48)$$

to make our numbers directly comparable. See Table I.
Squares of dipole moments for hydrogen were computed by

$$M^2 = \frac{4H_{mn}^2}{|\lambda_m - \lambda_n|^4} . \quad (49)$$

These results checked with the values of the squares of dipole moments* given by Bethe and Salpeter.⁸ Note that Eq. (49) is not defined by the method presented in this report when $\lambda_m = \lambda_n$.

To check the code to more digits than given by Bethe and Salpeter (the CDC 7600 is a 14-digit machine), $H_{1s,2p}$ was computed to the maximum possible accuracy using the hydrogenic potential and was compared with its analytic solution. We know that for hydrogen

$$\varphi_{1s} = 2re^{-r} \quad (50)$$

and

$$\varphi_{2p} = \frac{1}{2\sqrt{6}} r^2 e^{-r/2}$$

When these analytic expressions for φ are used in Eq. (44) along with $V(r) = -1/r$, we obtain

$$H_{1s,2p} = \frac{8}{9\sqrt{6}} = 0.36288736930121$$

and DEGA-A computed

$$H_{1s,2p} = 0.36288736930118 .$$

*Compare with Table 13, page 264, Bethe and Salpeter.⁸

TABLE I
TRANSITION INTEGRAL τ
FOR COLD, NORMAL DENSITY ELEMENTS

Element	Transition	Transition Integral τ			
		Screened-Hydrogenic	Coulomb Approx	Self-Cons Field	DEGA-A
Li I ^a	2p-2s	5.96	5.42	5.5-5.6	4.26
	3p-2s	0.011	0.016	0.011-0.020	0.071
	3s-2p	1.72	2.39		1.75
	4s-2p	0.105	0.177		0.148
	5s-2p	0.029	0.056		0.044
	6s-2p	0.013	0.025		0.020
	3d-2p	1.28	1.14		0.748
	4d-2p	0.19	0.18		0.148
Be I ^b	2s2p-2s ²	2.27	2.03	1.86	3.29
Na I ^c	3p-3s	3.41	6.0	6.7	3.63
	4p-3s	0.211	0.047	0.051	0.026
	4s-3p	2.06	6.09	6.2	3.60
K I ^d	4p-4s	4.61	8.05	9.05	7.77
Sr I ^e	5d-5p	0.483	0.42		1.39

^aZ=3, r₀=1.928, and R₁=3.263.

^bZ=4, r₀=1.406, and R₁=2.355.

^cZ=11, r₀=2.264, and R₁=3.986.

^dZ=19, r₀=2.714, and R₁=4.950.

^eZ=38, r₀=2.475, and R₁=4.518.

C. Free-Free Absorptions

1. Discussion of Gaunt Factors. A formula similar to Eq. (47)² can be derived for σ_{ff} (hv) in terms of Gaunt factors g_{ff} ; however, here we only compute Gaunt factors for hydrogen and sodium and compare some of these results with Karzas and Latter.⁹ Gaunt factors can be evaluated with

$$g_{ff}(\lambda_a, hv) = \frac{\pi\sqrt{3}}{8(Z_{eff})^2} \sum_{\ell=0}^{L'} \left[(\ell+1) H_{\ell+1,\ell}(\lambda_a, hv)^2 + \ell H_{\ell-1,\ell}(\lambda_a, hv)^2 \right] \quad (51)$$

when the sum converges rapidly enough to be practical. Here λ_a is the initial energy of the electron, hv is the photon energy, Z_{eff} is the effective number of free elec-

trons in the atom under consideration, and L' is a finite integer approximation to infinity. The matrix elements are still defined by Eq. (44), but we rewrite the equation as

$$H_{mn}(\lambda_a, hv) = 2 \int_0^\infty \varphi_m(\lambda_a, r) \frac{\partial V(r)}{\partial r} \varphi_n(\lambda_a + hv, r) dr \quad (52)$$

to define the association between energy levels and quantum numbers.

The sum in Eq. (51) is not always converging rapidly. Results for other than a coulomb potential can often be obtained in these cases by making use of the formula¹⁰

$$g_{ff}(\lambda_a, hv) = g_{ff}^c(\lambda_a, hv) + \frac{\pi\sqrt{3}}{8} \sum_{\ell=0}^L \left\{ (\ell+1) [H_{\ell+1,\ell}(\lambda_a, hv)^2 - H_{\ell+1,\ell}^c(\lambda_a, hv)^2] + \ell [H_{\ell-1,\ell}(\lambda_a, hv)^2 - H_{\ell-1,\ell}^c(\lambda_a, hv)^2] \right\}, \quad (53)$$

where g_{ff}^c is the coulombic Gaunt factor for the initial energy and photon energy under consideration, H_{mn}^c is a coulombic matrix element defined by Eq. (52) using $V(r) = -1/r$, and L is an integer sufficiently large so that the sum has converged to a predetermined accuracy. A graph of $g_{ff}^c(\lambda_a, h\nu)$ is given by Karzas and Latter who circumvented the slow convergence problem in Eq. (51) by using hypergeometric functions. Applications of this procedure are limited to the coulomb potential.

The method for obtaining a noncoulombic $\sigma_{ff}(h\nu)$, as described in this report, never requires the evaluation of a $Z_{eff}(\lambda_a, h\nu)$. In terms of coulombic Gaunt factors, $g_{ff}^c(\lambda_a, h\nu)$, $Z_{eff}(\lambda_a, h\nu)$ must also be evaluated and then $Z_{eff}(\lambda_a, h\nu) g_{ff}^c(\lambda_a, h\nu)$ must be used as the desired Gaunt factor. However, Eqs. (51) and (53) give the desired noncoulombic $g_{ff}(\lambda_a, h\nu)$ for $Z_{eff} = 1$ when the matrix elements are computed by DEGA-A using a realistic potential.

2. Checks on Method. For the first check on the code, we computed several Gaunt factors with Eq. (51) using the coulomb potential, $V(r) = -1/r$, and compared these results with the Karzas and Latter graph. Here comparisons were made up to, at most, three significant figures, which is the maximum accuracy for reading the graph. Table II shows that for several cases we were able to reproduce the Karzas and Latter values. In the remaining cases, Eq. (51) had not converged for $\ell = 34$, the maximum value of ℓ used in these calculations.

Cold, normal-density sodium ($Z = 11$, $r_0 = 2.264$, $R_1 = 3.986$) was arbitrarily used in the next check (Fig. 8). Here, for low photon energies and low initial energies, the Gaunt factors using the sodium potential and $Z_{eff} = 1$ should approach the coulombic Gaunt factors. Also, for large photon energies and large initial energies, the Gaunt factors using the sodium potential and $Z_{eff} = 11$ should approach the coulombic Gaunt factors. In both cases, the sodium Gaunt factor for $(\lambda_a, h\nu)$ is compared with the coulombic Gaunt factor for $(\lambda_a/(Z_{eff})^2, h\nu/(Z_{eff})^2)$.

3. Discussion of Screening. The general screening effects are noted for the small electron kinetic energy and the small photon energy shown in Fig. 8. As the photon energy is held fixed and the electron energy is increased, the calculated Gaunt factor increases faster than would be expected from the coulombic case. The qualitative reason for this follows. As the electron energy is increased, the electron wave function samples in greater and greater detail the structure of the atom (the shielding), and as a result the effective charge Z_{eff} increases with increasing energy. The result is that, relative to a coulomb potential, the cross section is raised. However, as the energy of the electron and the photon increase, we eventually arrive at a

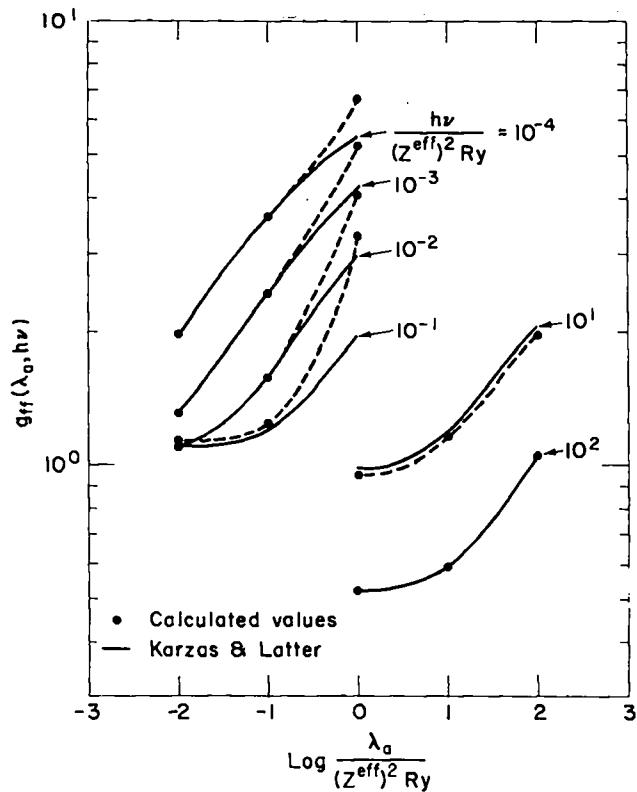


Fig. 8.
A comparison of coulombic and shielded potential (NaI) Gaunt factors.

point where the wave function of the electron oscillates sufficiently rapidly that it is essentially seeing the coulomb field of the nucleus. The effective charge is then the nuclear charge and we have agreement with the coulomb field results. This corresponds to the lower right-hand curves of Fig. 8.

4. Numerical Results. The purpose of Table II is to illustrate a trend in the convergence rate for each of Eqs. (51) and (53) as a function of $(\lambda_a, h\nu)$. An integer in parentheses indicates the value of ℓ for which the series was terminated. For example, where $(\lambda_a, h\nu) = (1.0, 0.01)$, Eq. (51) has summed to 3.07 by 34 terms, whereas Eq. (53) has summed to within 2% of the expected (converged) value of 4.10 by three terms. Here convergence means no change in the sum to the accuracy given in Table II. Also, for the coulombic case at this energy pair, Eq. (51) has not converged for $\ell = 34$. For the $(1.0, 10)$ entry, both Eqs. (51) and (53) have converged by $\ell = 3$ for the sodium case, and Eq. (51) has converged by $\ell = 3$ in the coulombic case.

Table II also shows that neither Eq. (51) nor (53) has converged for the entries labeled with footnote b. The use

TABLE II

**CALCULATIONS OF COLD, NORMAL DENSITY SODIUM
AND COULOMBIC GAUNT FACTORS^a**

λ_a (Ry)	hv(Ry)	$g_{ff}^c(\lambda_a, hv)$ from Karzas and Latter	$g_{ff}^c(\lambda_a, hv)$ Calculated Using Eq. (51)	$g_{ff}(\lambda_a, hv)$ for Na Calculated Using Eq. (51)	$g_{ff}(\lambda_a, hv)$ for Na Calculated Using Eq. (53)
0.01	0.0001	1.97	0.83(34)	0.83(34)	1.97(3) 1.97(34)
	0.001	1.32	1.20(34)	1.20(34)	1.32(3) 1.32(34)
	0.01	1.11	1.11(29)	1.09(29)	1.09(3) 1.09(29)
	0.1	1.08	1.08(14)	1.11(14)	1.11(3) 1.11(14)
	1.0	1.10	1.10(3)	1.51(3)	1.51(3) 1.51(9)
0.1	0.0001	3.65	1.34(34)	1.34(34)	3.64(3) 3.65(34)
	0.001	2.46	1.41(34)	1.40(34)	2.45(3) 2.45(34)
	0.01	1.58	1.53(34)	1.53(34)	1.58(3) 1.58(34)
	0.1	1.21	1.21(24)	1.24(24)	1.24(3) 1.24(24)
	1.0	1.13	1.13(3)	1.99(3)	1.99(3) 1.99(11)
1.0	0.0001	5.5	1.92(34)	3.01(34)	6.50(3) 6.59(25) 6.59(34)
	0.001	4.2	1.92(34)	3.01(34)	5.20(3) 5.29(25) 5.29(34)
	0.01	3.0	1.97(34)	3.07(34)	4.02(3) 4.10(25) 4.10(34)
	0.1	1.95	1.89(34)	3.23(34)	3.22(3) 3.29(25) 3.29(34)
	1.0	1.31	1.31(15)	5.50(15)	5.44(3) 5.50(15) 5.50(22)
	10.	0.97	0.97(3)	37.4(3)	37.4(3) 37.4(7)
10.0	0.01	4.55	2.23(34)	27.5(34)	26.7(3) 29.8(25) 29.8(34)
	0.1	3.25	2.19(34)	27.6(34)	25.5(3) 28.6(25) 28.7(34)
	1.0	2.09	2.06(34)	29.6(34)	26.6(3) 29.6(25) 29.6(34)
	10.	1.20	1.20(10)	50.6(10)	49.4(3) 50.6(10) 50.6(16)
	100.	0.59	0.59(3)	106.7(3)	106.7(3) 106.7(7)
100.0	0.1	4.55	2.28(34)	102.2(34)	82.6(3) 104.3(25) 104.5(34)
	1.	3.30	2.31(34)	102.4(34)	81.7(3) 103.2(25) 103.4(34)
	10.	2.08	2.05(34)	106.1(34)	85.8(3) 106.0(25) 106.1(34)
	100.	1.06	1.06(10)	125.4(10)	121.0(3) 125.4(10) 125.4(15)
	1000.	0.42	0.42(3)	117.7(3)	117.7(3) 117.7(7)
1000.0	10.0 ^b	3.30	2.31(34)	187.3(34)	122.4(3) 185.7(25) 188.3(34)
	100. ^b	2.07	1.89(17)	187.7(34)	129.0(3) 172.8(10) 183.1(17)
	1000.	0.99	0.99(10)	141.3(10)	135.2(3) 141.3(10) 141.3(15)
	10,000.	0.36	0.36(3)	74.1(3)	74.1(3) 74.1(7)
10,000.0	100.0 ^b	3.30	2.31(34)	244.8(34)	132.1(3) 235.4(25) 245.8(34)
	1000. ^b	2.06	2.03(34)	232.2(34)	139.5(3) 228.1(25) 232.2(34)
	10,000.	0.98	0.98(10)	128.1(10)	122.4(3) 128.1(10) 128.1(15)
	100,000.	0.35	0.35(3)	51.8(3)	51.8(3) 51.8(7)

^aAll values in this table, with the exception of the Karzas and Latter entries, were computed with the DEGA-A code. An integer in parentheses is the value of ℓ for which either Eq. (51) or (53) was terminated to obtain the Gaunt factor. These integers illustrate the speed of convergence of Eqs. (51) and (53).

^bNeither Eq. (51) nor (53) has converged.

of a geometric sum enables the extrapolation of Eq. (51) to results that should represent a lower bound to the infinite sum. Numerical checks indicate that this extrapolation is good to 10% or better. To derive this extrapolation formula, let us simplify Eq. (51) by setting

$$Y_{\ell}^1 = (\ell + 1) H_{\ell+1,\ell}(\lambda_a, hv)^2 \quad (54)$$

and

$$Y_{\ell}^2 = \ell H_{\ell-1,\ell}(\lambda_a, hv)^2 .$$

From calculations, we note that both $(\log Y_{\ell}^1, \ell)$ and $(\log Y_{\ell}^2, \ell)$ approximate straight lines for large values of ℓ . (The $(\log Y_{\ell}, \ell)$ pair is not to be confused with the (λ_a, hv) pair.) Figure 9 illustrates this point for $(1000, 100)$. The straight line for Y_{ℓ}^1 is written as

$$\log Y_{\ell}^1 = s(\ell - \ell') + q , \quad (55)$$

and two known points, $(\log Y_{\ell'}^1, \ell')$ and $(\log Y_{\ell'+1}^1, \ell' + 1)$, are chosen to evaluate s and q . Equation (55) can also be written as

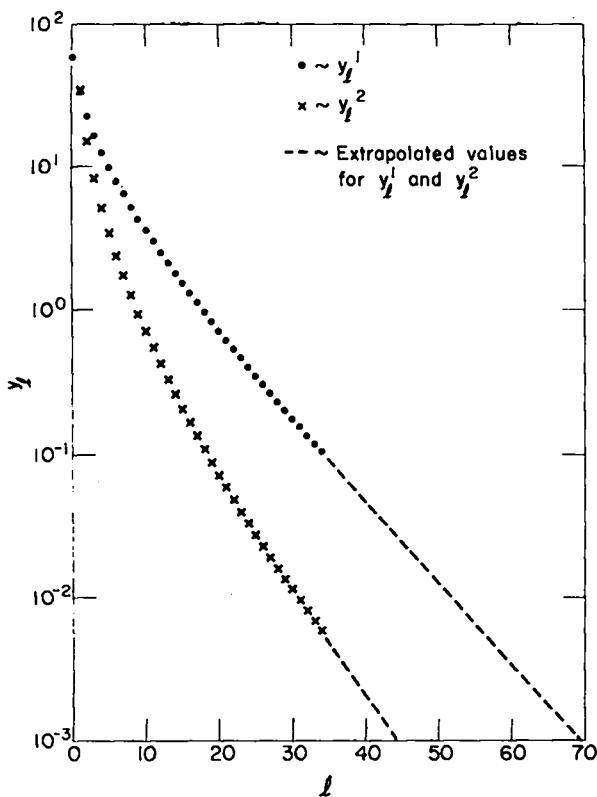


Fig. 9.

A graphic representation of the terms in Eq. (51) and the extrapolation indicated in Eq. (56).

$$Y_{\ell}^1 = e^q (e^s)^{\ell - \ell'} . \quad (56)$$

Now using Eq. (56) to take the infinite sum for all $\ell \geq \ell'$, we have the extrapolation formula

$$\sum_{\ell=\ell'}^{\infty} Y_{\ell}^1 = e^q / (1 - e^s) . \quad (57)$$

The above procedure is repeated using Y_{ℓ}^2 . These two extrapolated values are added to the number obtained by summing Eq. (51) to $\ell = \ell' - 1$. The results obtained by using this extrapolation formula are given in Table III.

TABLE III
EXTRAPOLATED VALUES OF
GAUNT FACTORS

λ_a	hv	$g_{ff}(\lambda_a, hv)$ for Na Calculated Using Eq. (51); ℓ in Parentheses	$g_{ff}(\lambda_a, hv)$ for Na Calculated Using Extrapolated Form of Eq. (51); ℓ' in Parentheses
1000.0	10.0	187.3 (34)	189.5 (27) 189.9 (34)
	100.	187.7 (34)	188.3 (27) 188.3 (34)
10,000.0	100.0	244.8 (34)	259.0 (27) 261.7 (34)
	1000.	232.2 (34)	234.2 (27) 234.3 (34)

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APPENDIX DEGA-A

DEGA-A in its present form is a research and not a production code. The version, whose listing follows, only calculates bound-free absorptions. The code lists these absorption coefficients and makes plots as seen in the previous section. With slight modifications in the coding, bound-bound and free-free absorptions can be calculated.

There are several free parameters that regulate the accuracy of the code. Most of these parameters are set at the beginning of the code; however, a few are found throughout the code. The values in the listing will give at least four-place accuracy. The user should feel free to vary these parameters as he pleases and at his own risk.

Data are read into the bound-free version of DEGA-A with the following FORTRAN statements.

```

2 FORMAT (8F10.3)
7 FORMAT (16I5)
133 FORMAT (F15.5,2I5)
      READ 2, Z, RR2, RR
      IF (Z.LT.0.0) end job
      READ 7, ISSMAX
      READ 7, (NSUBSHL(ISS), ISS = 1, ISSMAX)
      READ 7, KWKB
      DO 132 K = 1, KWKB
132 READ 133, XLAMWKB(K), LWKB(K), NWKB(K)
      READ 7, IHNUMAX
      READ 2, (HNUVEC(IHNU), ACOFVEC(IHNU),
              IHNU = 1, IHNUMAX)

```

Z is the atomic number of the element under consideration.

RR2 is the same as r_o on page 1.

RR is the same as R_1 on page 1. Units for RR2 and RR are number of Bohr Radii.

ISSMAX is the number of subshells under consideration.

NSUBSHL(ISS) is an array that contains the number of electrons in each subshell. The entries are read into this array in the order 1s, 2s, 2p, 3s, 3p, 3d, etc., up to the last occupied subshell. If any previous subshell is vacant, it must be assigned the value zero.

KWKB

is the number of bound wave functions to be computed. The necessary free wave functions are generated internally by the code.

XLAMWKB(K)

is an array that contains guesses at the eigenvalues of the bound states. Units are number of Rydbergs.

LWKB(K)

is an array that contains the quantum numbers ℓ . $\ell = 0$ for s - states, $\ell = 1$ for p - states, $\ell = 2$ for d - states, etc.

NWKB(K)

is an array that contains the quantum numbers n . $n = 1$ for the 1s state, $n = 2$ for the 2s and 2p states, $n = 3$ for the 3s, 3p, and 3d states, etc.

For each K, XLAMWKB(K), LWKB(K), and NWKB(K) should be consistent with Eq. (39). These guesses at bound eigenvalues can be read in any order. NSUBSHL(ISS) should be defined for each of these guesses at a bound eigenvalue.

IHNUMAX

is the number of $(hv, \sigma_{bf}(hv))$ pairs from a separate source that one wants to compare with the results of DEGA-A. This option is illustrated by the X's in Figs. 2 through 7. If IHNUMAX equals zero, no $(hv, \sigma_{bf}(hv))$ pairs will be read.

HNUVEC(IHNU)

is the array that contains the hv 's given in electron-volts.

ACOFVEC(IHNU)

is the array that contains the $\sigma_{bf}(hv)$'s given in barns/atom.

Data decks may be stacked one behind the other. The job terminates normally when it encounters a negative Z.

DEGA-A
(LP-129)

```

PROGRAM DEGAA(INP, OUT, FILM) DEGA 00002
DIMENSION XLAMARY(100), LARY(101), ALFAARY(100), IMAXARY(100) DEGA 00003
1 ,NSUHSHL(28), NSHELL(100) DEGA 00004
COMMON/SCRATCH/SCRATCH(1204) DEGA 00005
DIMENSION AM1S(401), AM2S(401), JMAXS(401) DEGA 00006
EQUIVALENCE (SCRATCH(1), AM1S(1)), (SCRATCH(402), AM2S(1)), DEGA 00007
1 (SCRATCH(803), JMAXS(1)) DEGA 00008
DIMENSION AROOT(2) DEGA 00009
DIMENSION PDUM(2) DEGA 00010
COMMON/CB3/ Z, ZM1, RR2, RR, A0 DEGA 00011
COMMON/AIMAX/ AF(51,402), JMAXF(402), IMAX, DEGA 00012
1 IMAXF, IMAXFP1, IMAXB, IMAXBPI, C(3,400), DEGA 00013
2 CF(3,402), ATOP(401), ATOPF(402) DEGA 00014
DIMENSION AB(51,402), JMAXB(402), CB(3,402), ATOPB(402) DEGA 00015
EQUIVALENCE(AF(1), AB(1)), (JMAXF(1), JMAXB(1)), DEGA 00016
1 (CF(1), CB(1)), (ATOPF(1), ATOPB(1)) DEGA 00017
COMMON/EPS/EPSCONV, FBMAX, EM16, EMATELE, EMDVDD, MAXDIM DEGA 00018
DIMENSION AXLAMB(100) DEGA 00019
DIMENSION XLAMWKB(100), LWKB(101), NWKB(100) DEGA 00020
COMMON/PI/PI, TWOSPI DEGA 00021
COMMON/CB1/ HNUVEC(500), ACOFVEC(500), NOPTS, IHNUMAX, MM(100), DEGA 00022
1 NN(100), MNMAX, I4MIN, I4MAX DEGA 00023
COMMON/METHODS/METHOD, TEMPLAM, CAOF, CAPFP, THETA, THETAP DEGA 00024
PI = 3.1415926535898 S TWOSPI = 2.0/PI DEGA 00025
MAXITER = 100 DEGA 00026
MAXDIM = 100 DEGA 00027
EPSCONV = 1.0E-5 DEGA 00028
FRMAX = 1.0E200 DEGA 00029
EM16 = 1.0E-8 DEGA 00030
EMATELE = 1.0E-5 DEGA 00031
EMDVDD = 1.0E-8 DEGA 00032
RMAXFAC = 25.0 DEGA 00033
EPMI = 1.0E-15 DEGA 00034
DRMIN = 1.0E-8 DEGA 00035
DVMAX = 1.0E-4 DEGA 00036
ATOPFAC = .5 DEGA 00037
DHNUI = .1 DEGA 00038
ZZZFAC = 10.0 DEGA 00039
NODIVNG = 70 DEGA 00040
XLAMFC1 = 3.0 DEGA 00041
XLAMFC2 = .2 DEGA 00042
C MAKE XLAMFC1 .GT. 1.0 AND XLAMFC2 .LT. 1.0 DEGA 00043
CALL ADV(15) DEGA 00044
1 FORMAT(E24.14, 2I5) DEGA 00045
2 FORMAT(BF10.3) DEGA 00046
3 FORMAT(5E25.14) DEGA 00047
7 FORMAT(16I5) DEGA 00048
9 FORMAT(BF10.3) DEGA 00049
997 CONTINUE DEGA 00050
MFAC = 1 DEGA 00051
NOPTS = 500 DEGA 00052
KPHIMAX = 0 DEGA 00053
IFRROR = 0 DEGA 00054
RMIN = 0.0 DEGA 00055
READ 2, Z, RR2, RR DEGA 00056
IF(Z .LT. 0.0) GO TO 998 DEGA 00057
RMAX = RR DEGA 00058
PRINT 3, Z, RR2, RR DEGA 00059
ZM1 = Z - 1.0 DEGA 00060
A0 = .6057*Z**.333333 DEGA 00061
RFAD 7, ISSMAX DEGA 00062
PRINT 7, ISSMAX DEGA 00063

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READ 7, (NSUBSHL(ISS), ISS=1, ISSMAX) DEGA 00064
PRINT 7, (NSUBSHL(ISS), ISS=1, ISSMAX) DEGA 00065
READ 7, KWKB DEGA 00066
PRINT 7, KWKB DEGA 00067
133 FORMAT(F15.5, 2I5) DEGA 00068
DO 132 K=1, KWKB DEGA 00069
READ 133, XLAMWKB(K), LWKB(K), NWKB(K) DEGA 00070
PRINT 1, XLAMWKB(K), LWKB(K), NWKB(K) DEGA 00071
XLAMARY(K) = XLAMWKB(K) DEGA 00072
LARY(K) = LWKB(K) DEGA 00073
132 NSHELL(K) = NWKB(K) DEGA 00074
LARY(KWKB + 1) = -1 DEGA 00075
IF(RR2 .GE. 0.0) SCRATCH(1) = V1(RR2) DEGA 00076
CALL YYY(RMIN,RMAX,DRMIN,DVMAX,ATOPFAC,I2,IERROR, DEGA 00077
1 XLAMWKB, LWKB, KWKB, ZZZFAC) DEGA 00078
IF(IERROR .NE. 0) GO TO 99 DEGA 00079
I2P1 = I2 + 1 DEGA 00080
ISKIP = 3*MAXDIM + 4 DEGA 00081
IECS = 1 - ISKIP DEGA 00082
DO 118 I=1, I2 DEGA 00083
IECS = IECS + ISKIP DEGA 00084
CALL ECWR(ATOP(I+1), IECS, 1, IE) DEGA 00085
118 CALL ECWR(C(1,I), IECS+1, 3, IE) DEGA 00086
PRINT 7, IMAX, I2 DEGA 00087
IMAXP1 = IMAX + 1 DEGA 00088
IF(IMAXP1 .GT. 400) GO TO 109 DEGA 00089
DO 10B I=IMAXP1, 400 DEGA 00090
C(1,I) = 0.0 DEGA 00091
C(2,I) = -1.0 DEGA 00092
108 C(3,I) = 0.0 DEGA 00093
109 ATOP(I) = 0.0 DEGA 00094
DO 10 I=1, IMAX DEGA 00095
10 PRINT 3, C(1,I), C(2,I), C(3,I), ATOP(I+1) DEGA 00096
GO TO 49 DEGA 00097
135 CONTINUE DEGA 00098
CALL ZZZ(XLAMARY, LARY, NSHELL, KPHIMAX, HNUVEC, NOPTS, DEGA 00099
1 IHNUMAX, DHNUI, ZZZFAC) DEGA 00100
136 FORMAT(///) DEGA 00101
PRINT 136 DEGA 00102
DO 137 KPHI=1, KPHIMAX DEGA 00103
137 PRINT 133, XLAMARY(KPHI), LARY(KPHI), NSHELL(KPHI) DEGA 00104
PRINT 136 DEGA 00105
PRINT 3, (HNUVEC(IHNU), THNU=1, IHNUMAX) DEGA 00106
PRINT 136 DEGA 00107
DO 138 IHNU=1, IHNUMAX DEGA 00108
138 ACOFVEC(IHNU) = 0.0 DEGA 00109
KWKBMAX = 0 DEGA 00110
DO 139 KPHI=1, KPHIMAX DEGA 00111
KWKBMAX = KWKBMAX + 1 DEGA 00112
NWKB(KWKBMAX) = NSHELL(KPHI) DEGA 00113
LWKB(KWKBMAX) = 1000*(LARY(KPHI) + 1) + LARY(KPHI) DEGA 00114
XLAMWKB(KWKBMAX) = XLAMARY(KPHI) DEGA 00115
IF(LARY(KPHI) .EQ. 0) GO TO 139 DEGA 00116
KWKBMAX = KWKBMAX + 1 DEGA 00117
NWKB(KWKBMAX) = NSHELL(KPHI) DEGA 00118
LWKB(KWKBMAX) = 1000*(LARY(KPHI) - 1) + LARY(KPHI) DEGA 00119
XLAMWKB(KWKBMAX) = XLAMARY(KPHI) DEGA 00120
139 CONTINUE DEGA 00121
KWKB = 0 DEGA 00122
I4MIN = 1 DEGA 00123
140 KWKB = KWKB + 1 DEGA 00124
XLAMARY(1) = XLAMWKB(KWKB) DEGA 00125

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NSHELL_L(1) = NWKB/KWKB; DEGA 00126
LPOS = LWKB(KWKB)/1000 DEGA 00127
LARY(1) = LWKB(KWKB) - LPOS*1000 DEGA 00128
141 IF(1.0000001*ABS(XLAMARY(1)) .LT. HNUVFC(I4MIN)) GO TO 142 DEGA 00129
I4MIN = I4MIN + 1 DEGA 00130
GO TO 141 DEGA 00131
142 I4MAX = IHNUMAX DEGA 00132
MNMAX = 0 DEGA 00133
DO 143 I4=I4MIN , I4MAX DEGA 00134
MNMAX = MNMAX + 1 DEGA 00135
MNMAXP1 = MNMAX + i DEGA 00136
MM(MNMAX) = i DEGA 00137
NN(MNMAX) = MNMAXP1 DEGA 00138
XLAMARY(MNMAXP1) = HNUVEC(I4) + XLAMARY(1) DEGA 00139
LARY(MNMAXP1) = LPOS DEGA 00140
143 NSHELL_(MNMAXP1) = 0 DEGA 00141
LARY(MNMAXP1 + 1) = -2 DEGA 00142
KPHIMAX = 0 DEGA 00143
49 CONTINUE DEGA 00144
KPHIMP1 = KPHIMAX + 1 DEGA 00145
L = LARY(KPHIMP1) DEGA 00146
IF(L .EQ. -1) GO TO 135 DEGA 00147
IF(L .EQ. -2) GO TO 99 DEGA 00148
METHOD = 2 DEGA 00149
IF(XLAMARY(KPHIMP1) .LT. 0.0) METHOD = 1 DEGA 00150
XL = L DEGA 00151
XLLP1 = L*(L+1) DEGA 00152
XLLM1 = XL*(XL-1.0) DEGA 00153
TWOXL = 2.0*XL DEGA 00154
LM2 = L-2 DEGA 00155
LM1 = L-1 DEGA 00156
LP1 = L+1 DEGA 00157
XLPI = LP1 DEGA 00158
IF (METHOD .EQ. 1) GO TO 107 DEGA 00159
XLAMBDA = XLAMARY(KPHIMP1) DEGA 00160
SMALLK = SQRT(XLAMBDA) DEGA 00161
RMAX = (XLLP1 + 1.0/XLAMBDA - 30.0)*SMALLK DEGA 00162
RTMP = 10.0/XLAMBDA DEGA 00163
IF(RTMP .GT. RMAX) RMAX = RTMP DEGA 00164
IF(ATOP(I2+1) .GT. RMAX) RMAX = 1.05*ATOP(I2+1) DEGA 00165
IF(RMAX .LT. 1.01) RMAX = 1.01 DEGA 00166
GO TO 122 DEGA 00167
146 RMAX = 1.2*RMAX DEGA 00168
IERROR = 0 DEGA 00169
GO TO 110 DEGA 00170
107 AROOT(1) = 0.0 DEGA 00171
AROOT(2) = 0.0 DEGA 00172
IMAX = I2 + 1 DEGA 00173
ATOP(IMAX+1) = 1000.0 DEGA 00174
CALL ROOTDIV(XLAMARY(KPHIMP1), XLLP1, AROOT, ICNTR, ICNTD, ICASE, DEGA 00175
1 IERROR, 1) DEGA 00176
PRIN 3, XLAMARY(KPHIMP1), AROOT(1), AROOT(2) DEGA 00177
IF(IERROR .EQ. 0) GO TO 151 DEGA 00178
PRINT 152, IERROR DEGA 00179
152 FORMAT(15, * RMAX SET TO 1.1*ATOP(I2+1)*)
IERROR = 0 DEGA 00180
RMAX = 1.1*ATOP(I2+1) DEGA 00181
GO TO 122 DEGA 00182
151 RMAX = AROOT(2) DEGA 00183
IF(AROOT(1) .GT. RMAX) RMAX = AROOT(1) DEGA 00185
RMAX = RMAXFAC*RMAX DEGA 00186
IF(RMAX .LT. 1.01*ATOP(I2+1))RMAX = 1.01*ATOP(I2+1) DEGA 00187

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PRINT 153, RMAX
153 FORMAT(* RMAX = *, E20.10) DEGA 00188
122 IMAX = I2 DEGA 00189
110 DR = ATOPFAC*ATOP(IMAX+1) DEGA 00190
RTMP= ATOP(IMAX + 1) DEGA 00191
SMALLK = SQRT(ABS(XLAMARY(KPHIMP1) + (2.0 - XLLP1/RTMP)/RTMP)) DEGA 00192
RTMP = ATOP(IMAX+1) + .5*(ATOP(IMAX+1) - ATOP(IMAX)) DEGA 00193
SMALLK1 = SQRT(ABS(XLAMARY(KPHIMP1) + (2.0 - XLLP1/RTMP)/RTMP)) DEGA 00194
IF(SMALLK1 .GT. SMALLK) SMALLK = SMALLK1 DEGA 00195
IF(SMALLK1 .GT. SMALLK) SMALLK = SMALLK1 DEGA 00196
DEMAX = 6.28/SMALLK DEGA 00197
IF(DR .GT. DMAX) DR = DMAX DEGA 00198
IMAX = IMAX + 1 DEGA 00199
ATOP(IMAX+1) = ATOP(IMAX) + DR DEGA 00200
IF(IMAX .EQ. 400) 124, 123 DEGA 00201
124 PRINT 125 DEGA 00202
125 FORMAT(* 400 INTERVALS WILL NOT SPAN (0,RMAX)*)
GO TO 999 DEGA 00203
123 IF(ATOP(IMAX+1) .GE. RMAX) 111, 110 DEGA 00204
111 ATOP(IMAX+1) = RMAX DEGA 00205
CAPR = RMAX DEGA 00206
DEMAX = ATOP(IMAX + 1) DEGA 00207
ATOP(IMAX+1) = CAPR DEGA 00208
GO TO (68,69), METHOD DEGA 00209
DEGA 00210
68 NODIV = NODIVNG DEGA 00211
NODIVP1 = NODIV + 1 DEGA 00212
AXLAMB(1) = XLAMFC1*XLAMARY(KPHIMP1) DEGA 00213
AXLAMB(NODIVP1) = XLAMFC2*XLAMARY(KPHIMP1) DEGA 00214
DAXLAMB = ABS ALOG(ABS(AXLAMB(1))) DEGA 00215
1 - ALOG(ABS(AXLAMB(NODIVP1)))) / NODIV DEGA 00216
IF(ABS(AXLAMB(1)) .GT. ABS(AXLAMB(NODIVP1))) DAXLAMB = -DAXLAMB DEGA 00217
DO 60 I=2, NODIV DEGA 00218
60 AXLAMB(I) = -EXP(ALOG(ABS(AXLAMB(I-1))) + DAXLAMB) DEGA 00219
XLAMBDA = AXLAMB(1) DEGA 00220
GO TO 70 DEGA 00221
69 TEMPLAM = XLAMBDA DEGA 00222
NODIV = 4 S NODIVP1 = NODIV + 1 DEGA 00223
AXLAMB(1) = 0.0 S DXLAM = PI/4.0 DEGA 00224
DO 71 I=1, NODIV DEGA 00225
71 AXLAMB(I+1) = AXLAMB(I) + DXLAM DEGA 00226
CALL CARSON(XLAMBDA, C(2,IMAX), MFAC, CAPR, XLLP1, DEGA 00227
1 CAPF, CAPFP, THETA, THETAP, IERROR) DEGA 00228
IF(IERROR .EQ. 12) GO TO 146 DEGA 00229
70 CONTINUE DEGA 00230
AROOT(1) = 0.0 S ARROOT(2) = 0.0 DEGA 00231
CALL ROOTDIV(XLAMBDA, XLLP1, ARROOT, ICNTR, ICNTD, ICASE, DEGA 00232
1 IERROR, 0) DEGA 00233
PRINT 3, XLAMBDA, AROOT(1), AROOT(2) DEGA 00234
J25SET = 1 DEGA 00235
80 J25FST = 1 DEGA 00236
J25MIN = J25SET DEGA 00237
J25MAX = NODIVP1 DEGA 00238
GO TO 90 DEGA 00239
81 J25FST = 2 DEGA 00240
J25MIN = NODIVP1+1 DEGA 00241
J25MAX = NODIVP1 + 20 DEGA 00242
D25 = (XLAMSTP - XLAMSTT)/19.0 DEGA 00243
AXLAMB(J25MIN) = XLAMSTT DEGA 00244
AXLAMB(J25MAX) = XLAMSTP DEGA 00245
I79MIN = J25MIN+1 DEGA 00246
I79MAX = J25MAX - 1 DEGA 00247
DO 79 I79=I79MIN, I79MAX DEGA 00248
79 AXLAMB(I79) = AXLAMB(I79 - 1) + D25 DEGA 00249

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90 DO 25 J= J25MIN, J25MAX
  XLAMSTP = XLAMLB(J)
  CALL TAYLORF(XL, XLAMSTP, IERROR, AF, JMAXF, IMAXF, CF, ATOPF)
  IRKW = IMAXFP1 + 1
  CALL TAYLORB(XL, XLAMSTP, IERROR, AB(1, IRKW),
  1 JMAXH(IRKW), IMAXB, CB(1,IRKW), ATOPR(IRKW))
  CALL BOUNDARY(IFCONV, FBSTP)
  TROUBLE MAY ARISE (MISS AN EIGENVALUE) IF FBSTP=0 TWICE
  IN A ROW.
  ***** *****
  HERE, LATER, FIND NEW ROOTS AND CHECK STABILITY CONDITIONS.
  IF(IFCONV .EQ. 1) 73, 74
  73 CAPLAMB = XLAMSTP
  GO TO 75
  74 IF(J .EQ. J25MIN) 26, 27
  27 IF(FBSTP*FBSTP .LE. 0.0) 28, 26
  28 XLAMMID = .5*(XLAMSTP + XLAMSTT)
  CALL TAYLORF(XL, XLAMMID, IERROR, AF, JMAXF, IMAXF, CF, ATOPF)
  IRKW = IMAXFP1 + 1
  CALL TAYLORB(XL, XLAMMID, IERROR, AB(1,IRKW),
  1 JMAXB(IRKW), IMAXB, CB(1,IRKW), ATOPR(IRKW))
  CALL BOUNDARY(IFCONV, FB4ID)
  IF(FB4ID .GT. FBSTP) 29, 30
  29 FBTOP = FBSTP  S  FBBOT = FBSTP  S  GO TO 31
  30 FBTOP = FBSTP  S  FBBOT = FBSTT
  31 IF((FBTOP .GT. FB4ID) .AND. (FB4ID .GT. FBBOT)) 32, 57
  57 PRINT 58
  PRINT 58
  PRINT 59
  PRINT 58
  PRINT 58
  58 FORMAT(* XXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXX*)
  59 FORMAT(* FB4ID IS NOT BETWEEN FBTOP AND FBBOT. MAKE SURE A VALUE
  1 OF LAMBDA WAS NOT MISSED.*)
  GO TO 87
  32 XLAMB0 = XLAMSTT  S  XLAMBI = XLAMSTP
  FR0 = FRSTT  S  FB1 = FBSTP
  C REGULA DOES NOT CHECK STABILITY CONDITIONS.
  CALL REGULA(XLAMB0, XLAMBI, FB0, FR1, CAPLAMB, MAXITER, XL, IERROR)
  C HERE, LATER, FIND NEW ROOTS AND CHECK STABILITY CONDITIONS.
  IF(IERROR .NE. 0) GO TO 87
  IF(XLAMSTT .LT. XLAMSTP) GO TO 105
  XLAMB0 = XLAMSTP
  XLAMBI = XLAMSTT
  GO TO 104
  105 XLAMB0 = XLAMSTT
  XLAMBI = XLAMSTP
  104 IF(XLAMB0 .LE. CAPLAMB .AND. CAPLAMB .LE. XLAMBI) 75, 86
  86 PRINT 58
  PRINT 58
  PRINT 88
  88 FORMAT(* CAPLAMB IS NOT BETWEEN XLAMSTT AND XLAMSTP. XLAMSTT, CA
  1PLAMB, AND XLAMSTP ARE *)
  PRINT 3, XLAMSTT, CAPLAMB, XLAMSTP
  PRINT 58
  PRINT 58
  87 IF(J25FST .EQ. 1) 82, 84
  82 J25SET = J
  PRINT 83
  83 FORMAT(* DIVIDE THIS INTERVAL INTO 19 EQUAL INTERVALS AND TRY AGAIN
  1IN. *)
  PRINT 58

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PRINT 58 DEGA 00312
GO TO 81 DEGA 00313
84 PRINT 85 DEGA 00314
85 FORMAT(* THIS INTERVAL FAILED FOR THE SECOND TIME. FORGET IT AND DEGA 00315
1 GO TO THE NEXT INTERVAL. *)
PRINT 58 DEGA 00316
PRINT 58 DEGA 00317
GO TO 80 DEGA 00318
75 GO TO(65, 66), METHOD DEGA 00319
66 ALPHA = CAPLAMB S CAPLAMB = XLAMBDA DEGA 00320
PRINT 67, ALPHA, CAPLAMB DEGA 00321
67 FORMAT(* ALPHA =*, E24.14, * FOR XLAMBDA =*, E24.14) DEGA 00322
GO TO 127 DEGA 00323
65 CONTINUE DEGA 00324
IV1 = 0 DEGA 00325
D = ATOPF(2) DEGA 00326
DLPI = D*LP1 DEGA 00327
JMAXROT = JMAXF(1) - 1 DEGA 00328
PDUM(1) = AF(1,2)/DLPI DEGA 00329
PDUM(2) = (AF(2,2) - XLPI*AF(1,2)/D)/DLPI DEGA 00330
CALL STURMSQ(AF(2:)), JMAXROT, PDUM, D, IV2, IERROR) DEGA 00331
IV1 = IV1 + IV2 DEGA 00332
IF(IMAXF.EQ. 1) GO TO 98 DEGA 00333
DO 91 IF=2, IMAXF DEGA 00334
D = ATOPF(IF+1) - ATOPF(IF) DEGA 00335
CALL STURMSQ(AF(1,IF), JMAXF(IF), AF(1,IF+1), D, IV2, IERROR) DEGA 00336
91 IV1 = IV1 + IV2 DEGA 00337
98 CONTINUE DEGA 00338
DO 95 IR=1, IMAXB DEGA 00339
IBKW = IMAXFP1 + IB DEGA 00340
D = ATOPB(IBKW + 1) - ATOPB(IBKW) DEGA 00341
CALL STURMSQ(AB(1,IBKW), JMAXB(IBKW), AB(1,IBKW+1), DEGA 00342
1 D, IV2, IERROR) DEGA 00343
95 IV1 = IV1 + IV2 DEGA 00344
PRINT 128, IV1 DEGA 00345
128 FORMAT(* THIS WAVE FUNCTION HAS*, I5, * CROSSINGS.*)
127 IBKW = IMAXFP1 + IMAXBPI DEGA 00346
FAC = AB(1,IBKW)/AF(1,IMAXFP1) DEGA 00347
DO 33 I=1, IMAXF DEGA 00348
JJJ = JMAXF(I) DEGA 00349
DO 33 JF=1, JJJ DEGA 00350
33 AF(JF,I) = FAC*AF(JF,I) DEGA 00351
IF(CAPLAMB .LT. 0.0) CALL NORMPHI(CAPLAMB, L) DEGA 00352
PRINT 3, CAPLAMB DEGA 00353
KPHIMAX = KPHIMAX + 1 DEGA 00354
GO TO(129,130), METHOD DEGA 00355
129 IV1L1 = IV1 + L + 1 DEGA 00356
IF(NSHELL(KPHIMAX) .EQ. IV1L1) GO TO 154 DEGA 00357
IV1 = NSHELL(KPHIMAX) - L - 1 DEGA 00358
KPHIMAX = KPHIMAX - 1 DEGA 00359
PRINT 134, IV1 DEGA 00360
134 FORMAT(* THE PREVIOUS WAVE FUNCTION SHOULD HAVE HAD*, I5,
1 * CROSSINGS,*/* FORGET THE LAST EIGENVALUE AND TRY SOME MORE,*; DEGA 00361
1 GO TO 26 DEGA 00362
154 IRKW = IMAXFP1 + 1 DEGA 00363
PHIMIN9 = ABS(AB(1,IBKW)) DEGA 00364
PHIMAX9 = PHIMIN9 DEGA 00365
IF(IMAXB .EQ. 1) GO TO 155 DEGA 00366
DO 156 IR=2, IMAXB DEGA 00367
IRKW = IMAXFP1 + IR DEGA 00368
PHI9 = ABS(AB(1,IBKW)) DEGA 00369
IF(PHI9 .GT. PHIMAX9) PHIMAX9 = PHI9 DEGA 00370
DEGA 00371
DEGA 00372
DEGA 00373

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156 CONTINUE DEGA 00374
155 DO 157 IF=1, IMAXF DEGA 00375
    PHI9 = ABS(AF(1,IF))
    IF(PHI9 .GT. PHIMAX9) PHIMAX9 = PHI9 DEGA 00376
157 CONTINUE DEGA 00377
    PRINT 158, PHIMAX9, PHIMIN9 DEGA 00378
158 FORMAT(" PHI MAX AND MIN ARE*, 2E20.10")
    IF(PHIMIN9 .LT. PHIMAX9*EPHI) GO TO 131 DEGA 00380
    PRINT 159 DEGA 00381
159 FORMAT(" RMAX IS NOT BIG ENOUGH")
    KPHIMAX = KPHIMAX - 1 DEGA 00382
    GO TO 146 DEGA 00383
160 NSHELL(KPHIMAX) = 0 DEGA 00384
161 IMAXARY(KPHIMAX) = IMAX DEGA 00385
    XLAMARY(KPHIMAX) = CAPLAMB DEGA 00386
    LARY(KPHIMAX) = L DEGA 00387
    IF(CAPLAMB .LT. 0.0) 112, 113 DEGA 00388
112 ALFAARY(KPHIMAX) = 0.0 DEGA 00389
    GO TO 114 DEGA 00390
113 ALFAARY(KPHIMAX) = ALPHA DEGA 00391
114 CONTINUE DEGA 00392
    JMAXS(1) = JMAXF(1)
    DO 115 I=1, IMAXF DEGA 00393
        AM1S(I) = AF(1,I)
    115 AM2S(I) = AF(2,I) DEGA 00394
        IC = IMAXB1
        ID = IMAXF DEGA 00395
        DO 116 I=1, IMAXB DEGA 00396
            IC = IC-1
            ID = ID+1 DEGA 00397
            IBKW = IMAXFP1 + IC
            AM1S(ID) = AB(1,IBKW) DEGA 00398
            AM2S(ID) = AB(2,IBKW) DEGA 00399
116 JMAXS(ID) = JMAXB(IBKW) DEGA 00400
        DO 117 I=2, IMAXFP1 DEGA 00401
117 JMAXS(I) = 0 DEGA 00402
        IMAXBF = IMAXB + IMAXF DEGA 00403
        IFCS = KPHIMAX + 4 DEGA 00404
        IECS1 = IECS + MAXDIM DEGA 00405
        IECS2 = IECS1 + MAXDIM DEGA 00406
        CALL ECWR(JMAXS(1), IECS, 1, IE) DEGA 00407
        CALL ECWR(AM1S(1), IECS1, 1, IE) DEGA 00408
        CALL ECWR(AM2S(1), IECS2, 1, IE) DEGA 00409
        DO 121 I=3, I2P1 DEGA 00410
        IFCS = IECS + ISKIP
        IECS1 = IECS + MAXDIM DEGA 00411
        IECS2 = IECS1 + MAXDIM DEGA 00412
        CALL ECWR(JMAXS(I), IECS, 1, IE) DEGA 00413
        CALL ECWR(AM1S(I), IECS1, 1, IE) DEGA 00414
        CALL ECWR(AM2S(I), IECS2, 1, IE) DEGA 00415
        DO 121 I=3, I2P1 DEGA 00416
        IFCS = IECS + ISKIP
        IECS1 = IECS + MAXDIM DEGA 00417
        IECS2 = IECS1 + MAXDIM DEGA 00418
        CALL ECWR(JMAXS(I), IECS, 1, IE) DEGA 00419
        CALL ECWR(AM1S(I), IECS1, 1, IE) DEGA 00420
        CALL ECWR(AM2S(I), IECS2, 1, IE) DEGA 00421
        IF(IMAX .EQ. I2) GO TO 126 DEGA 00422
        IECSS = 4*(400 - I2)
        IECS = IECS*(KPHIMAX - 1) + 1 DEGA 00423
        IFCS = IECS + I2*ISKIP DEGA 00424
        IJUMP = 400 - I2
        INUM = IMAX - I2 DEGA 00425
        I2P2 = I2+2
        CALL ECWR(ATOP(I2P2), IECS, INUM, IE) DEGA 00426
        IECS = IECS + IJUMP DEGA 00427
        CALL ECWR(JMAXS(I2P2), IECS, INUM, IE) DEGA 00428
        IECS = IECS + IJUMP DEGA 00429
        CALL ECWR(AM1S(I2P2), IECS, INUM, IE) DEGA 00430
        IECS = IECS + IJUMP DEGA 00431
        CALL ECWR(AM2S(I2P2), IECS, INUM, IE) DEGA 00432
        IECS = IECS + IJUMP DEGA 00433
        CALL ECWR(AM1S(I2P2), IECS, INUM, IE) DEGA 00434
        IECS = IECS + IJUMP DEGA 00435

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IECS = IECS + IJUMP
CALL ECWR(AM2S(I2P2), IECS, INUM, IE) DEGA 00436
126 GO TO 61 DEGA 00437
26 XLA4STT = XLA4STP $ FBSTT = FBSTP DEGA 00438
25 CONTINUE DEGA 00439
IF(J25FST .EQ. 2) B0, 998 DEGA 00440
61 ATOP(IMAX+1) = ATOPTMP DEGA 00441
GO TO 49 DEGA 00442
99 IF(KPHIMAX .EQ. 0) GO TO 999 DEGA 00443
DO 120 KPHI = 1, KPHIMAX DEGA 00444
PRINT 7, LARY(KPHI) DEGA 00445
120 PRINT 3, XLA4ARY(KPHI) , ALFAARY(KPHI) DEGA 00446
CALL MATELE(KPHIMAX, XLA4ARY, LARY, ALFAARY, IMAXARY, IZ, DEGA 00447
1 NSUBSHL, ISSMAX, NSHELL) DEGA 00448
999 CONTINUE DEGA 00449
IF(KWKB .LT. KWKBMAX) GO TO 140 DEGA 00450
145 FORMAT(15X, * EV*, 10X, * BARNS/ATOM*) DEGA 00451
PRINT 145 DEGA 00452
YTOP = ALOG10(ACOFVEC(1)) DEGA 00453
YBOT = YTUP DEGA 00454
DO 144 IHNU=1, IHNUMAX DEGA 00455
HNUVEC(IHNU) = 13.605*HNUVEC(IHNU) DEGA 00456
PRINT 3, HNUVEC(IHNU), ACOFVEC(IHNU) DEGA 00457
ACOFVEC(IHNU) = ALOG10(ACOFVEC(IHNU)) DEGA 00458
IF(ACOFVEC(IHNU) .GT. YTOP) YTOP = ACOFVEC(IHNU) DEGA 00459
IF(ACOFVEC(IHNU) .LT. YBOT) YBOT = ACOFVEC(IHNU) DEGA 00460
144 HNUVEC(IHNU) = ALOG10(HNUVEC(IHNU)); DEGA 00461
CALL ADV(2) DEGA 00462
CALL DGA(120, 980, 50, 910, HNUVEC(1), HNUVEC(IHNUMAX), YTOP-YBOT) DEGA 00463
CALL DLGLG DEGA 00464
CALL SBLOG DEGA 00465
CALL SLLOG DEGA 00466
CALL PLOT(IHNUMAX, HNUVEC, 1, ACOFVEC, 1, 42, 1) DEGA 00467
READ 7, IHNUMAX DEGA 00468
PRINT 7, IHNUMAX DEGA 00469
IF(IHNUMAX .EQ. 0) GO TO 997 DEGA 00470
READ 2, (HNUVEC(IHNU), ACOFVEC(IHNU)), IHNU=1, IHNUMAX DEGA 00471
DO 150 IHNU=1, IHNUMAX DEGA 00472
PRINT 3, HNUVEC(IHNU), ACOFVEC(IHNU) DEGA 00473
HNUVEC(IHNU) = ALOG10(HNUVEC(IHNU)) DEGA 00474
150 ACOFVEC(IHNU) = ALOG10(ACOFVEC(IHNU)) DEGA 00475
CALL PLOT(IHNUMAX, HNUVEC, 1, ACOFVEC, 1, 55, 0) DEGA 00476
GO TO 997 DEGA 00477
998 CONTINUE DEGA 00478
CALL ADV(151) DEGA 00479
CALL EMPTY DEGA 00480
END DEGA 00481
SUBROUTINE ROOTDIV(XLAMBDA, XLLP1, AROOT, ICNTR, ICNTD, ICASE, DEGA 00482
1 IERROR, IFSTOP) DEGA 00483
DIMENSION AROOT(2) DEGA 00484
COMMON/AIMAX/ AF(51:402), JMAXF(402), IMAX, DEGA 00485
1 IMAXF, IMAXFP, IMAXB, IMAXBPI, C(3:400), DEGA 00486
2 CF(3:402), ATOP(401), ATOPF(402) DEGA 00487
DIMENSION AB(51:402), JMAXB(402), CB(3:402), ATOPB(402) DEGA 00488
EQUIVALENCE(AF(1), AB(1)), (JMAXF(1), JMAXB(1)), DEGA 00489
1 (CF(1), CB(1)), (ATOPF(1), ATOPB(1)) DEGA 00490
ICNTR = 0 $ ICNTD = 0 $ IERROR = 0 DEGA 00491
DO 10 I=1, IMAX DEGA 00492
II=I DEGA 00493
CALL BINOM (XLAMBDA, XLLP1, II, NOROUTS, ROOT1, ROOT2, NODIV, DIV1) DEGA 00494
NOROUT1 = NOROUTS + 1 DEGA 00495
GO TO(14, 11, 12),NOROUT1 DEGA 00496
DEGA 00497

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11 IF((ATOP(I) .LE. ROOT1) .AND. (ROOT1 .LT. ATOP(I+1)))13,14    DEGA 00498
13 ICNTR = ICNTR + 1          DEGA 00499
  AROOT(ICNTR) = ROOT1      DEGA 00500
  IF(ICNTR .EQ. 2)15, 14     DEGA 00501
12 IF(ROOT1 .LT. ROOT2) 28, 27 DEGA 00502
27 TEMP = ROOT1  S  ROOT1 = ROOT2  S  ROOT2 = TEMP.      DEGA 00503
28 IF((ATOP(I) .LE. ROOT1) .AND.(ROOT1 .LT. ATOP(I+1)))16,17    DEGA 00504
16 ICNTR = ICNTR + 1          DEGA 00505
  AROOT(ICNTR) = ROOT1      DEGA 00506
  IF(ICNTR .EQ. 2)15, 17     DEGA 00507
17 IF((ATOP(I) .LE. ROOT2) .AND. (ROOT2 .LT. ATOP(I+1)))18,14    DEGA 00508
18 ICNTR = ICNTR + 1          DEGA 00509
  AROOT(ICNTR) = ROOT2      DEGA 00510
  IF(ICNTR .EQ. 2)15, 14     DEGA 00511
15 IF(ICNTD .EQ. 1)19, 20     DEGA 00512
20 IF(NUDIV .EQ. 1)21, 19     DEGA 00513
21 IF((ATOP(I).LE. DIV1) .AND. (DIV1 .LT. ATOP(I+1)))22, 19    DEGA 00514
22 ICNTU = 1  S  ADIV = DIV1  S  IDIV = I  S  GO TO 19      DEGA 00515
14 IF(ICNTD .EQ. 1)10, 23     DEGA 00516
23 IF(NUDIV .EQ. 1)24, 10     DEGA 00517
24 IF((ATOP(I).LE. DIV1) .AND. (DIV1 .LT. ATOP(I+1)))25, 10    DEGA 00518
25 ICNTU = 1  S  ADIV = DIV1  S  IDIV = I      DEGA 00519
10 CONTINUE                  DEGA 00520
19 IF((ICNTD .EQ. 1) .AND. (ICNTR .EQ.2))29, 44      DEGA 00521
44 IF((ICNTD .EQ.1).AND. (ICNTR .EQ. 0)) 45, 26      DEGA 00522
45 ICASE = 5  S  GO TO 31      DEGA 00523
29 ICASE = 4                  DEGA 00524
  IF((AROOT(1) .LT. ADIV) .AND. (ADIV .LT. AROOT(2)))31, 30    DEGA 00525
30 IERROR = 2                  DEGA 00526
  PRINT 2                    DEGA 00527
? FORMAT(* IERROR=2, ICASE=4. MAX IS NOT BETWEEN THE TWO ROOTS.*)
  RETURN                      DEGA 00529
26 IF((ICNTD.EQ. 0) .AND. (ICNTR .EQ. 0))34, 35      DEGA 00530
34 ICASE = 1  S  IDIV = IMAX      DEGA 00531
  ADIV = (ATOP(IMAX) + ATOP(IMAX+1))/2.0      DEGA 00532
  GO TO 31                  DEGA 00533
35 IF((ICNTD .EQ. 0) .AND.(ICNTR .EQ. 1))37, 40      DEGA 00534
37 ICASE = 2                  DEGA 00535
  IF(XLLP1 .LT. .25) 47, 46      DEGA 00536
47 IMAXP1 = IMAX + 1          DEGA 00537
  DO 48 I=2, IMAXP1          DEGA 00538
  IF(AROOT(1) .LT. ATOP(I)) 49, 48      DEGA 00539
49 IDIV = I-1                  DEGA 00540
  ADIV = AROOT(1)            DEGA 00541
  GO TO 31                  DEGA 00542
48 CONTINUE                  DEGA 00543
  IDIV = IMAX                DEGA 00544
  GO TO 38                  DEGA 00545
46 IDIV = IMAX                DEGA 00546
  IF(AROOT(1) .LT. ATOP(IMAX))38, 39      DEGA 00547
38 ADIV = (ATOP(IMAX) + ATOP(IMAX+1))/2.0      DEGA 00548
  GO TO 31                  DEGA 00549
39 ADIV = (AROOT(1) + ATOP(IMAX+1))/2.0      DEGA 00550
  GO TO 31                  DEGA 00551
40 IF((ICNTD .EQ. 1) .AND.(ICNTR .EQ. 1))41, 42      DEGA 00552
42 IERROR = 1                  DEGA 00553
  PRINT 1, ICNTD, ICNTR      DEGA 00554
  1 FORMAT(* IERROR=1, ICNTD =#, I2, *, ICNTR =#, I2)
  RETURN                      DEGA 00555
41 ICASE = 3                  DEGA 00557
  IF(AROOT(1) .LT. ADIV) 31, 43      DEGA 00558
43 IERROR = 3                  DEGA 00559

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PRINT 3, AROOT(1), ADIV
3 FORMAT(" IERROR=3, ICASE=3, AROOT(1).GE.ADIV, AROOT(1) =*,E20.10, DEGA 00560
1      *, ADIV =*, E20.10) DEGA 00561
RETURN DEGA 00562
31 IF(IFSTOP .EQ. 1) RETURN DEGA 00563
IMAXF = IDIV   S   IMAXFP1 = IMAXF + 1 DEGA 00564
IMAXB = IMAX + 1 - IDIV   S   IMAXBP1 = IMAXB + 1 DEGA 00565
DO 32 I=1, IMAXF DEGA 00566
ATOPF(I) = ATOP(I) DEGA 00567
CF(1,I) = C(1,I)   S   CF(2,I) = C(2,I) DEGA 00568
32 CF(3,I) = C(3,I) DEGA 00569
ATOPF(IMAXFP1) = ADIV DEGA 00570
II = IMAX + 1   S   III = IMAX + 2 DEGA 00571
DO 33 I=1, IMAXB DEGA 00572
III = III-1 DEGA 00573
IRKW = IMAXFP1 + I DEGA 00574
ATOPB(IBKW) = ATOP(III) DEGA 00575
II = II - 1 DEGA 00576
CR(1,IBKW) = C(1,II)   S   CB(2,IBKW) = C(2,II) DEGA 00577
33 CB(3,IBKW) = C(3,II) DEGA 00578
IRKW = IMAXFP1 + IMAXBPI DEGA 00579
ATOPB(IBKW) = ADIV DEGA 00580
RETURN DEGA 00581
END DEGA 00582
SUBROUTINE BINOM(XLAMBDA, XLLP1, I, NOROTS, ROOT1, ROOT2,
1 NODIV, DIV1) DEGA 00583
COMMON/AIMAX/ AF(51,402), JMAXF(402), IMAX, DEGA 00584
1 IMAXF, IMAXFP1, IMAXB, IMAXBP1, C(3,400) DEGA 00585
2 CF(3,402), ATOP(401), ATOPF(402) DEGA 00586
DIMENSION AB(51,402), JMAXB(402), CB(3,402), ATOPB(402) DEGA 00587
EQUIVALENCE(AF(1), AB(1)), (JMAXF(1), JMAXB(1)) DEGA 00588
1 (CF(1), CB(1)), (ATOPF(1), ATOPB(1)) DEGA 00589
B1 = -(2.0*C(3,I) + XLLP1) DEGA 00590
B2 = -2.0*C(2,I) DEGA 00591
B3 = XLAMBDA - 2.0*C(1,I) DEGA 00592
ARSB1 = ABS(B1) DEGA 00593
IF(ARSB1 .LT. ABS(B2)*1.0E-12) 1, 2 DEGA 00594
2 IF(ARSB1 .LT. ABS(B3)*1.0E-12) 1, 3 DEGA 00595
1 ROOT1 = -B2/B3 DEGA 00596
NOROTS = 1 DEGA 00597
NODIV = 0 DEGA 00598
GO TO 6 DEGA 00599
3 RAD = B2*B2 - 4.0*B1*B3 DEGA 00600
TWOBI = 2.0*B1 DEGA 00601
NODIV = 1 DEGA 00602
DIV1 = -TWOBI/B2 DEGA 00603
IF(RAD .LT. 0.0) 4, 5 DEGA 00604
4 NOROTS = 0 DEGA 00605
GO TO 6 DEGA 00606
5 NOROTS = 2 DEGA 00607
RAD = SQRT(RAD) DEGA 00608
T1 = ARS(TWOBI) DEGA 00609
T2 = ABS(B2 + RAD) DEGA 00610
IF(T2 .LT. T1*1.0E-20) 7, 8 DEGA 00611
9 FORMAT( I5, 3E20.10, * XXXXX*) DEGA 00612
7 I1 = 1 DEGA 00613
PRINT 9, I1, TWOBI, B2, RAD DEGA 00614
ROOT1 = 1.0E100 DEGA 00615
GO TO 10 DEGA 00616
8 CONTINUE DEGA 00617
ROOT1 = -TWOBI/(B2 + RAD) DEGA 00618
10 T1 = ABS(TWOBI) DEGA 00619
DEGA 00620
DEGA 00621

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T2 = ABS(-B2 + RAD) DEGA 00622
IF(T2 .LT. T1*1.0E-20) 11, 12 DEGA 00623
11 I1 = 2 DEGA 00624
PRINT 9, I1, TWOBI, B2, RAD DEGA 00625
ROOT2 = 1.0E100 DEGA 00626
GO TO 6 DEGA 00627
12 CONTINUE DEGA 00628
ROOT2 = TWOBI/(-B2 + RAD) DEGA 00629
6 RETURN DEGA 00630
END DEGA 00631
SUBROUTINE REGULA(XLAMB0,XLAMB1,FB0,FB1,CAPLAMB,MAXITER,XL,IERROR) DEGA 00632
COMMON/AIMAX/ AF(51,402), JMAXF(402), IMAX,
1 IMAXF, IMAXFP1, IMAXB, IMAXBP1, C(3,400), DEGA 00633
2 CF(3,402), ATOP(401), ATOPF(402) DEGA 00634
DIMENSION AB(51,402), JMAXB(402), CB(3,402), ATOPB(402) DEGA 00635
EQUIVALENCE(AF(1,, AB(1,, (JMAXF(1,, JMAXB(1,, DEGA 00636
1 (CF(1,, CB(1,, (ATOPF(1,, ATOPB(1,, DEGA 00637
COMMON/EPS/ EPSCONV, FBMAX DEGA 00638
1 FORMAT(2E24.14, 4E20.10) DEGA 00639
IERROR = 0 DEGA 00640
DO 14 ITER = 1, MAXITER DEGA 00641
IF(FB1 .EQ. FB0) 20, 21 DEGA 00642
20 IRKW = IMAXFP1 + IMAXBP1 DEGA 00643
AFAC = AB(1,IBKW)/AF(1,IMAXFP1)*AF(2,IMAXFP1) DEGA 00644
FROJND = FBOJND/ABS(AFAC) DEGA 00645
CAPLAMR = .5*(XLAMB1 + XLAMB0) DEGA 00646
PRINT 22 DEGA 00647
PRINT 22 DEGA 00648
PRINT 23, FBOUND, EPSCONV DEGA 00649
PRINT 24, CAPLAMB, XLAMB1, XLAMB0 DEGA 00650
PRINT 22 DEGA 00651
PRINT 22 DEGA 00652
PRINT 22 DEGA 00653
RETURN DEGA 00654
22 FORMAT(* XXXXXXXXXXXXXXXXXXXXXXXXXXXXXXX*) DEGA 00655
23 FORMAT(* FB1=FB0, FBOUND = *, E20.10, EPSCONV = *, E20.10) DEGA 00656
24 FORMAT(* CAPLAMB = *, E24.14, 4H = (, E24.14, 2H +, E24.14, 4H )/2) DEGA 00657
21 ONEGAMA = (XLAMB1 - XLAMB0)/(FB1 - FB0) DEGA 00658
XLAMB2 = XLAMB1 - ONEGAMA*FB1 DEGA 00659
IF(XLAMB2.EQ.XLAMB1.OR.XLAMB2.EQ.XLAMB0) GO TO 15 DEGA 00660
CALL TAYLORF(XL, XLAMB2, IERROR, AF, JMAXF, IMAXF, CF, ATOPF) DEGA 00661
IF(IERROR .NE. 0) RETURN DEGA 00662
IRKW = IMAXFP1 + 1 DEGA 00663
CALL TAYLORR(XL, XLAMB2, IERROR, AB(1,IBKW), DEGA 00664
1 JMAXH(IBKW), IMAXB, CB(1,IBKW), ATOPR(IBKW)) DEGA 00665
IF(IERROR .NE. 0) RETURN DEGA 00666
CALL BOUNDARY(IFCONV, FBOUND) DEGA 00667
IF(IFCONV .EQ. 1) 15, 16 DEGA 00668
15 CAPLAMB = XLAMB2 $ RETURN DEGA 00669
16 IF(ABS(FBOUND) .GT. FBMAX) 17, 19 DEGA 00670
17 IERROR = 7 DEGA 00671
PRINT 7 DEGA 00672
7 FORMAT(* IERROR = 7, FBOUND .GT. FBMAX*) DEGA 00673
RETURN DEGA 00674
19 XLAMB0 = XLAMB1 $ XLAMB1 = XLAMB2 DEGA 00675
FB0 = FB1 DEGA 00676
14 FB1 = FBOUND DEGA 00677
IFRROR = 8 DEGA 00678
PRINT 8, MAXITER DEGA 00679
8 FORMAT (* PROBLEM DOES NOT CONVERGE WITHIN*,IS,* ITERATIONS*) DEGA 00680
RETURN DEGA 00681
END DEGA 00682
SUBROUTINE TAYLORF(XL, ALPHLAM, IERROR, A, JMAX, IMAX, C, ATOP) DEGA 00683

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DIMENSION A(51,1), JMAX(1), C(3,1), ATOP(I) DEGA 00684
COMMON/METHODS/METHOD, TEMPLAM, CAPF, CAPFP, THETA, THETAP DEGA 00685
COMMON/EPS/EPSCONV, FBMAX, EM16 DEGA 00686
GO TO (60, 61), METHOD DEGA 00687
60 XLAMBDA = ALPHLAM DEGA 00688
GO TO 62 DEGA 00689
61 ALPHA = ALPHLAM DEGA 00690
XLAMBDA = TEMPLAM DEGA 00691
62 CONTINUE DEGA 00692
DO 30 I=1, IMAX DEGA 00693
30 JMAX(I) = 0 DEGA 00694
IERQR = 0 DEGA 00695
D = ATOP(2) DEGA 00696
C***** LEFT BOUNDARY CONDITIONS. THESE ARE ONLY TRUE FOR DEGA 00697
C PHI(0)=0 WHERE PHI(R) IS THE EIGENFUNCTION. DEGA 00698
C***** DEGA 00699
A(1,1) = 0.0 DEGA 00700
A(2,1) = 1.0 DEGA 00701
C***** DEGA 00702
1 CALL TAYLOR1(A(1,1), JMAX(1), D, xi'AMBDA, DEGA 00703
XL, C(1,1), C(2,1), EM16, IERROR) DEGA 00704
IF(IERROR .EQ. 9) RETURN DEGA 00705
RR = ATOP(2) DEGA 00706
CALL POLY0P(A(1,1), JMAX(1), RR, P) DEGA 00707
A(1,2) = P*RR*XL DEGA 00708
CALL POLY1P(A(1,1), JMAX(1), RR, DERIVP) DEGA 00709
A(2,2) = (DERIVP*RR + P*XL)*RR***(XL-1.0) DEGA 00710
IF(IMAX .EQ. 1) GO TO 37 DEGA 00711
IBOT = 2 DEGA 00712
GO TO 58 DEGA 00713
ENTRY TAYLORB DEGA 00714
DO 54 I=1, IMAX DEGA 00715
54 JMAX(I) = 0 DEGA 00716
GO TO (65, 66), METHOD DEGA 00717
65 XLAMBDA = ALPHLAM DEGA 00718
GO TO 67 DEGA 00719
66 ALPHA = ALPHLAM DEGA 00720
XLAMBDA = TEMPLAM DEGA 00721
67 CONTINUE DEGA 00722
IERROR = 0 DEGA 00723
IPOT = 1 DEGA 00724
C***** RIGHT BOUNDARY ,R.B. CONDITIONS. HERE A(1,1) IS AN DEGA 00725
ARBITRARY CONSTANT. THE MAGNITUDE OF PHI(R.B.). A(2,1) IS DEGA 00726
THE DERIVATIVE OF PHI(R.B.) NORMALIZED TO A(1,1). DEGA 00727
DEGA 00728
DEGA 00729
C***** DEGA 00730
GO TO (63, 64), METHOD DEGA 00731
63 CONTINUE DEGA 00732
A(1,1) = 1.0E-140 DEGA 00733
A(2,1) = -SQRT(ABS(XLAMBDA))*A(1,1) DEGA 00734
GO TO 58 DEGA 00735
64 THETA1 = THETA + ALPHA DEGA 00736
COSTHE1 = COS(THETA1) DEGA 00737
A(1,1) = CAPF*COSTHE1 DEGA 00738
A(2,1) = CAPFP*COSTHE1 - CAPF*THETAP*SIN(THETA1) DEGA 00739
C***** DEGA 00740
58 XLL = XL*(XL+1.0) DEGA 00741
DO 25 I=IBOT, IMAX DEGA 00742
D = ATOP(I+1) - ATOP(I) DEGA 00743
CALL TAYLORS(A(1,I), JMAX(I), ATOP(I), D, XLAMBDA, DEGA 00744
XL, C(1,I), C(2,I), C(3,I), EM16, IERROR) DEGA 00745

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IF(IERROR .EQ. 10) RETURN
CALL POLY0P(A(1,I), JMAX(I), D, A(I,I+1))
CALL POLY1P(A(1,I), JMAX(I), D, A(2,I+1))
25 CONTINUE
37 RETURN
END
SUBROUTINE BOUNDARY(IFCONV, FBOUND)
COMMON/AIMAX/ AF(51,402), JMAXF(402), IMAX,
1 IMAXF, IMAXFP1, IMAXB, IMAXBP1, C(3,400),
2 CF(3,402), ATOP(401), ATOPF(402)
DIMENSION AB(51,402), JMAXB(402), CB(3,402), ATOPB(402)
EQUIVALENCE(AF(1), AB(1)), (JMAXF(1), JMAXB(1)),
1 (CF(1), CB(1)), (ATOPF(1), ATOPB(1))
COMMON/EPS/EPSCONV, F8MAX
C YOU ARE LIVING DANGEROUSLY IF YOU LET IMAXF=1. THIS MAY RESU DEGA 00746
C IN AN UNDETECTED DIVISION BY ZERO OR AN UNDETECTED LOSS OF ACCURAC DEGA 00747
C IF(IMAXF .EQ. 1) 1, 2 DEGA 00748
2 IF(ABS(AF(1,IMAXFP1)) .LT. ABS(AF(1,IMAXF))*1.0E-4) 3, 1 DEGA 00749
1 IRKW = IMAXFP1 + IMAX
IRKWP1 = IBKW + 1
IF(ABS(AB(1+IBKWP1)) .LT. ABS(AB(1+IBKW))*1.0E-4) 3, 5 DEGA 00750
3 PRINT 4
4 FORMAT(*      IN DANGER OF DIVIDING BY ZERO, OR ATLEAST LOOSING ACCU DEGA 00751
1 RACY. *)
5 IBKW = IMAXFP1 + IMAXBP1
FAC = AB(1+IBKW)/AF(1,IMAXFP1)
AFAC = FAC*AF(2,IMAXFP1)
FROUND = AFAC - AB(2,IBKW)
EPSC = ABS(AFAC)*EPSCONV
IF(ABS(FBOUND) .LT. EPSC) 6, 7 DEGA 00752
6 IFCONV = 1  S  GO TO 8 DEGA 00753
7 IFCONV = 0 DEGA 00754
8 RETURN
END
SUBROUTINE STURMSQ(A1, JMAX1, A2, D, IV2, IERROR)
DIMENSION A1(2), A2(2), CPI( 51), CPIPI( 51)
COMMON/SCRATCH/SCRATCH(604)
EQUIVALENCE(SCRATCH(1), CPI(1)), (SCRATCH(52), CPIPI(1))
IERROR = 0
JMAX1 = JMAX1
IF(D .LT. 0.0) 11, 12 DEGA 00755
11 ISIGN = -1
GO TO 13
12 ISIGN = 1
13 IV2 = 0
J1 = JMAX1+1
DO 14 J=1, JMAX1
J1 = J1 - 1
CPI(J) = A1(J1)
14 CPIPI(J) = (J1-1)*CPI(J)
JMAX1PI = JMAX1-1
P0 = CPI(JMAX1)
PD = A2(1)
P10 = CPIPI(JMAX1PI)
P1D = A2(2)
IF(P10 .EQ. 0.0) GO TO 15
IF(P0*P10 .LT. 0.0) 15, 16
15 IV2 = IV2 + 1
16 IF(PD .EQ. 0.0) GO TO 17
IF(P0*PD .LT. 0.0) 17, 18
17 IV2 = IV2 - 1
18 FAC = CPI(1)/CPIPI(1)
DEGA 00756
DEGA 00757
DEGA 00758
DEGA 00759
DEGA 00760
DEGA 00761
DEGA 00762
DEGA 00763
DEGA 00764
DEGA 00765
DEGA 00766
DEGA 00767
DEGA 00768
DEGA 00769
DEGA 00770
DEGA 00771
DEGA 00772
DEGA 00773
DEGA 00774
DEGA 00775
DEGA 00776
DEGA 00777
DEGA 00778
DEGA 00779
DEGA 00780
DEGA 00781
DEGA 00782
DEGA 00783
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DEGA 00788
DEGA 00789
DEGA 00790
DEGA 00791
DEGA 00792
DEGA 00793
DEGA 00794
DEGA 00795
DEGA 00796
DEGA 00797
DEGA 00798
DEGA 00799
DEGA 00800
DEGA 00801
DEGA 00802
DEGA 00803
DEGA 00804
DEGA 00805
DEGA 00806
DEGA 00807

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ZERO = ABS(CPI(1))*1.0E-11
DO 19 J1=2, JMAXIP1
19 CPI(J1) = CPI(J1) - FAC*CPIP1(J1)
NOZERO = 1
DO 20 J=2, JMAXI
IF(ABS(CPI(J)) .LT. ZERO) 20, 21
20 NOZERO = NOZERO + 1
GO TO 99
21 JMAXI = JMAXI - NOZERO
DO 22 J=1, JMAXI
22 CPI(J) = CPI(J+NOZERO)
IF(JMAXI .LT. JMAXIP1) 23, 18
23 JMIN = JMAXI + 1
DO 24 J=JMIN, JMAXIP1
24 CPI(J) = 0.0
DO 25 J=1, JMAXIP1
TEMP = CPI(J)
CPI(J) = CPIP1(J)
25 CPIP1(J) = -TEMP
JTEMP = JMAXI
JMAXI = JMAXIP1
JMAXIP1 = JTEMP
P0 = P10
P0 = P1D
P10 = CPIP1(JMAXIP1)
P1D = CPIP1(1)
IF(JMAXIP1 .EQ. 1) 28, 26
26 DO 27 J1=2, JMAXIP1
27 P1D = P1D*D + CPIP1(J1)
28 IF(P10 .EQ. 0.0) GO TO 29
IF(P0*D .LT. 0.0) 29, 30
29 IV2 = IV2 + 1
30 IF(P1D .EQ. 0.0) GO TO 31
IF(P0*D .LT. 0.0) 31, 35
31 IV2 = IV2 - 1
35 IF(JMAXIP1 .EQ. 1) 99, 18
99 IV2 = ISIGN*IV2
IF(IV2 .LT. 0) 32, 34
32 IERROR = 5
PRINT 33
33 FORMAT(* IV2 IS LESS THAN 0. *)
34 RETURN
END

SUBROUTINE YYY(RMIN, RMAX, DRMIN, DMAX, ATOPFAC, I2, IERROR,
1 XLA4WKB, LWKB, KWKB, ZZZFAC)
DIMENSION XLA4WKB(1), LWKB(1)
COMMON/AIMAX/ AF(51*402), JMAXF(402), IMAX,
1 IMAXF, IMAXFP1, IMAXB, IMAXBPI, C(3*400),
2 CF(3,402), ATOP(401), ATOPF(402)
DIMENSION AB(51*402), JMAXB(402), CB(3*402), ATOPB(402)
EQUIVALENCE(AF(1), AB(1)), (JMAXF(1), JMAXB(1)),
1 (CF(1), CB(1)), (ATOPF(1), ATOPB(1))
DIMENSION A(3, 4)
DIMENSION XLA4DIM(10), XLDIM(10)
COMMON/CB3/ Z, ZM1, RR2, RR, A0
2 FORMAT(////)
IERROR = 0
XLAMMAX = 0.0
LMAX = 0
DO 65 I=1, 10
XLAMUIM(I) = 0.0
65 XLDIM(I) = I*(I-1)
DEGA 00808
DEGA 00809
DEGA 00810
DEGA 00811
DEGA 00812
DEGA 00813
DEGA 00814
DEGA 00815
DEGA 00816
DEGA 00817
DEGA 00818
DEGA 00819
DEGA 00820
DEGA 00821
DEGA 00822
DEGA 00823
DEGA 00824
DEGA 00825
DEGA 00826
DEGA 00827
DEGA 00828
DEGA 00829
DEGA 00830
DEGA 00831
DEGA 00832
DEGA 00833
DEGA 00834
DEGA 00835
DEGA 00836
DEGA 00837
DEGA 00838
DEGA 00839
DEGA 00840
DEGA 00841
DEGA 00842
DEGA 00843
DEGA 00844
DEGA 00845
DEGA 00846
DEGA 00847
DEGA 00848
DEGA 00849
DEGA 00850
DEGA 00851
DEGA 00852
DEGA 00853
DEGA 00854
DEGA 00855
DEGA 00856
DEGA 00857
DEGA 00858
DEGA 00859
DEGA 00860
DEGA 00861
DEGA 00862
DEGA 00863
DEGA 00864
DEGA 00865
DEGA 00866
DEGA 00867
DEGA 00868
DEGA 00869

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DO 66 I=1, KWKB
IF(XLAMWKB(I) .LT. XLAMMAX) XLAMMAX = XLAMWKB(I)
IF(LWKB(I) .GT. LMAX) LMAX = LWKB(I)
J = LWKB(I) + 1
IF(XLAMWKB(I) .LT. XLAMDIM(J)) XLAMDIM(J) = XLAMWKB(I)
66 CONTINUE
LMAXP1 = LMAX + 1
XLDIM(LMAX + 2) = LMAXP1*(LMAX + 2)
LMAX = LMAX + 3
XLAMDIM(LMAX) = ZZZFAC*ABS(XLAMMAX)
XLDIM(LMAX) = 0.0
68 FORMAT(2E20.10)
DO 69 L=1, LMAX
69 PRINT 68, XLAMDIM(L), XLDIM(L)
IF(RR2 .GT. 0.0) GO TO 62
IMAX = 1
DR = ABS(RR2)
ATOP(2) = DR
C(1,1) = 0.0
C(2,1) = -1.0
C(3,1) = 0.0
63 DR = ATOPFAC*ATOP(IMAX+1)
IF(DR .GT. DRMAX) DR = DRMAX
IMAX = IMAX + 1
ATOP(IMAX+1) = ATOP(IMAX) + DR
C(1,IMAX) = 0.0
C(2,IMAX) = -1.0
C(3,IMAX) = 0.0
IF(ATOP(IMAX+1) .GE. RMAX) 64, 63
64 ATOP(IMAX+1) = RMAX
I2 = IMAX
RETURN
62 IMAX = 0
I2 = 0
IREG1 = 2
IREG2 = 1
OPAF = 1.0 + ATOPFAC
RROT = RMIN
IF(RR2 .GE. RMAX) 50, 51
50 RTOP = RMAX
IFINISH = 1
GO TO 37
51 RTOP = RR2
IFINISH = 0
37 DRTB = RTOP - RBOT
R1 = .3*DRTB
R2 = .6*DRTB
CALL DRMAXSB(DRMAX, R1, R2, XLAMDIM, XLDIM, LMAX)
IF(DRTB .LE. DRMAX) GO TO 21
RTOP = RBOT + DRMAX
IFINISH = 0
21 IF(IREG2 .EQ. 3) 60, 59
60 IF(I2 .EQ. 0) I2 = IMAX
IMAX = IMAX + 1
C(1, IMAX) = 0.0
C(2, IMAX) = -1.0
C(3, IMAX) = 0.0
GO TO 61
59 DR = RTOP - RBOT
DDR = DR/9.0
IF(DR .LT. DRMIN) 22, 23
22 PRINT 3
DEGA 00870
DEGA 00871
DEGA 00872
DEGA 00873
DEGA 00874
DEGA 00875
DEGA 00876
DEGA 00877
DEGA 00878
DEGA 00879
DEGA 00880
DEGA 00881
DEGA 00882
DEGA 00883
DEGA 00884
DEGA 00885
DEGA 00886
DEGA 00887
DEGA 00888
DEGA 00889
DEGA 00890
DEGA 00891
DEGA 00892
DEGA 00893
DEGA 00894
DEGA 00895
DEGA 00896
DEGA 00897
DEGA 00898
DEGA 00899
DEGA 00900
DEGA 00901
DEGA 00902
DEGA 00903
DEGA 00904
DEGA 00905
DEGA 00906
DEGA 00907
DEGA 00908
DEGA 00909
DEGA 00910
DEGA 00911
DEGA 00912
DEGA 00913
DEGA 00914
DEGA 00915
DEGA 00916
DEGA 00917
DEGA 00918
DEGA 00919
DEGA 00920
DEGA 00921
DEGA 00922
DEGA 00923
DEGA 00924
DEGA 00925
DEGA 00926
DEGA 00927
DEGA 00928
DEGA 00929
DEGA 00930
DEGA 00931

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3 FORMAT(* AN INTERVAL ALONG THE R-AXIS GOT TOO SMALL.*)
PRINT 4, DR, DRMIN DEGA 00932
4 FORMAT(* DR =*,E20.10,*,*10X,*DRMIN =*,E20.10) DEGA 00933
IFRROR = 21 DEGA 00934
6 FORMAT (* IERROR =*, I5) DEGA 00935
PRINT 6, IERROR DEGA 00936
PRINT 2 DEGA 00937
GO TO 99 DEGA 00938
23 R1 = RBOT $ R3 = RTOP $ R2 = (R1 + R3)/2.0 DEGA 00939
IF(R1 .LT. 1.0E-200) 33, 34 DEGA 00940
33 A(3,4) = 0.0 $ GO TO 35 DEGA 00941
34 A(3,4) = R1*R1*V(R1) DEGA 00942
35 A(2,4) = R2*R2*V(R2) DEGA 00943
A(1,4) = R3*R3*V(R3) DEGA 00944
A(1,1) = R3*R3 $ A(2,1) = R2*R2 $ A(3,1) = R1*R1 DEGA 00945
A(1,2) = R3 $ A(2,2) = R2 $ A(3,2) = 01 DEGA 00946
A(1,3) = 1.0 $ A(2,3) = 1.0 $ A(3,3) = 1.0 DEGA 00947
CALL MATPAC(-1, A, 3, 1, DET, 0.0, IF SING) DEGA 00948
CHAT1 = A(1,4) $ CHAT2 = A(2,4) $ CHAT3 = A(3,4) DEGA 00949
C***** R = V IS NEVER USED. WE WILL ONLY BE WORKING WITH VS DEGA 00950
C WHERE V(R) .NE. 0 FOR R .NE. 0. DEGA 00951
C***** DEGA 00952
C***** DEGA 00953
C***** DEGA 00954
C***** DEGA 00955
R = KBOT DEGA 00956
DO 24 J=1, 8 DEGA 00957
R = R + DDR DEGA 00958
VR = V(R) DEGA 00959
P = CHAT1 + CHAT2/R + CHAT3/(R*R) DEGA 00960
XJ = J DEGA 00961
C 1 FORMAT(4E20.10) DEGA 00962
C PRINT 1, XJ, R, VR, P DEGA 00963
IF(ABS((VR - P)/VR) .LT. DVMAX) 24, 25 DEGA 00964
24 CONTINUE DEGA 00965
C***** DEGA 00966
IREG2 = IREG1 DEGA 00967
IMAX = IMAX + 1 DEGA 00968
C(1,IMAX) = CHAT1 $ C(2,IMAX) = CHAT2 $ C(3,IMAX) = CHAT3 DEGA 00969
61 ATOP(IMAX + 1) = RTOP DEGA 00970
IF (FINISH .EQ. 1) 99, 31 DEGA 00971
31 IF(IMAX .LT. 40) 28, 32 DEGA 00972
32 PRINT 7 DEGA 00973
7 FORMAT(* THE MAXIMUM NUMBER OF INTERVALS WILL NOT SPAN (RMIN, RMAX) DEGA 00974
11,*)
IFRROR = 22 DEGA 00975
PRINT 6, IERROR DEGA 00976
PRINT 2 DEGA 00977
GO TO 99 DEGA 00978
28 RBOT = RTOP DEGA 00979
IF(IREG1 .EQ. 3) 58, 57 DEGA 00980
58 DRTOP = ATOPFAC*RTOP DEGA 00981
R1 = RTOP DEGA 00982
R2 = RTOP + .5*(RTOP - ATOP(IMAX)) DEGA 00983
CALL DRMAXSB(DRMAX, R1, R2, XLAMDIM, XLDIM, LMAX) DEGA 00984
IF(DRTOP .GT. DRMAX) DRTOP = DRMAX DEGA 00985
RTOP = RTOP + DRTOP DEGA 00986
GO TO 52 DEGA 00987
C***** DEGA 00988
C***** DEGA 00989
C THIS CARD DETERMINES MAXIMUM INTERVAL LENGTH. DEGA 00990
C***** DEGA 00991
57 IF(IMAX .EQ. 1) 40, 41 DEGA 00992
DEGA 00993

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40 DR1 = DR          DEGA 00994
DR2 = DR          DEGA 00995
DR3 = DR          DEGA 00996
DR4 = DR          DEGA 00997
DRTMP = DR         DEGA 00998
GO TO 42          DEGA 00999
41 DR5 = DR4        DEGA 01000
DR4 = DR3        DEGA 01001
DR3 = DR2        DEGA 01002
DR2= DR1        DEGA 01003
DR1 = DR          DEGA 01004
DRTMP = (DR1 + DR2 + DR3 + DR4 + DR5)/5.0  DEGA 01005
42 IF(2.0*DRTMP .LT. ATOPFAC*RTOP) 46, 47    DEGA 01006
46 RTOP = RTOP + 2.0*DRTMP        DEGA 01007
GO TO 48          DEGA 01008
47 RTOP = DPAF*RTOP        DEGA 01009
48 R1 = RR0T        DEGA 01010
R2 = RR0T + .5*(RBOT - ATOP(IMAX))        DEGA 01011
CALL DRMAXSB(DRMAX, R1, R2, XLAMDIM, XLDIM, LMAX)  DEGA 01012
IF(RTOP - RBOT .GT. DRMAX) RTOP = RBOT + DRMAX  DEGA 01013
GO TO (54, 53), IREG1  DEGA 01014
54 IF(RTOP .GE. RR2) 55, 52    DEGA 01015
55 RTOP = RR2        DEGA 01016
IREG1 = 2          DEGA 01017
GO TO 52          DEGA 01018
53 IF(RTOP .GE. RR) 56, 52    DEGA 01019
56 RTOP = RR        DEGA 01020
IREG1 = 3          DEGA 01021
C*****          DEGA 01022
52 IF(RMAX .LE. RTOP) 29, 26    DEGA 01023
29 RTOP = RMAX  S  IFINISH = 1  DEGA 01024
GO TO 21          DEGA 01025
25 IREG1 = IREG2        DEGA 01026
IF(IMAX .EQ. 0) 43, 44        DEGA 01027
44 IF( DR .LT. .5*DRTMP) 43, 45  DEGA 01028
43 RTOP = R2          DEGA 01029
GO TO 26          DEGA 01030
45 RTOP = RBOT + .75*DR        DEGA 01031
26 IFINISH = 0        DEGA 01032
GO TO 21          DEGA 01033
99 IF(I2 .EQ. 0) I2 = IMAX    DEGA 01034
RETURN          DEGA 01035
END          DEGA 01036
SUBROUTINE DRMAXSB(DRMAX, R1, R2, XLAMDIM, XLDIM, LMAX)  DEGA 01037
DIMENSION XLAMDIM(1), XLDIM(1)
SMALLK = 0.0        DEGA 01038
R12 = 1.0/R1**2        DEGA 01039
R22 = 1.0/R2**2        DEGA 01040
TVR1 = 2.0*V(R1)        DEGA 01041
TVR2 = 2.0*V(R2)        DEGA 01042
DO 70 L=1, LMAX        DEGA 01043
SK = ABS(XLAMDIM(L) - TVR1 - XLDIM(L)*R12)        DEGA 01044
IF(SK .GT. SMALLK) SMALLK = SK        DEGA 01045
SK = ABS(XLAMDIM(L) - TVR2 - XLDIM(L)*R22)        DEGA 01046
IF(SK .GT. SMALLK) SMALLK = SK        DEGA 01047
70 CONTINUE        DEGA 01048
DRMAX = 6.28/SORT(SMALLK)        DEGA 01049
RETURN          DEGA 01050
END          DEGA 01051
FUNCTION V1(R)
COMMON/CB3/ Z, ZM1, RR2, RR, A0        DEGA 01052
FNZ2 = 1.0/(1.0 + A0*RR2)        DEGA 01053
DEGA 01054
DEGA 01055

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FNZ = FNZZ**2*(2.0*A0*RR2*FNZZ + 1.0)*ZM1
A1 = RR/RR2*(ZM1/FNZ*FNZZ**2 - 1.0) + 1.5
VV = ZM1/RR
A0RR = A0*RR
FNZSRRM = -FNZ/RR
ENTRY V
IF(R .GT. RR) GO TO 3
X1 = R/RR
IF(R .GT. RR2) GO TO 2
V1 = VV/(X1*(1.0 + A0RR*x1)**2)
V1 = -V1 + FNZSRRM*(X1**2/2.0 - A1) - 1.0/R
RETURN
2 V1 = FNZSRRM*(1.0/x1 + X1**2/2.0 - 1.5) - 1.0/R
RETURN
3 V1 = -1.0/R
RETURN
END
SUBROUTINE MATPAC (IJOB, A, N, M, DET, EP, IF SING)
DIMENSION A(3, 4)
IF SING = 0
DET = 1.
NPI = N+1
NPM = N*M
NM1 = N-1
IF(IJOB) 2, 1, 2
1 DO 3 I=1, N
NPI = N+I
A(I,NPI) = 1.
IP1 = I+1
IF(N = IP1) 2, 19, 19
19 DO 3 J=IP1, N
NPJ = N+J
A(I, NPJ) = 0.
3 A(J, NPI) = 0.
2 DO 4 J=1, NM1
C = ABS(A(J,J))
JP1 = J+1
DO 5 I=JP1, N
D = ABS(A(I,J))
IF(C=D) 6, 5, 5
6 DET = -DET
DO 7 K=J, NPM
B = A(I,K)
A(I, K) = A(J, K)
7 A(J, K) = B
C = D
5 CONTINUE
IF( ABS(A(J,J))-EP) 14, 15, 15
14 DET = 0.
IF(IJOB) 16, 16, 17
16 IF SING = 1
17 RETURN
15 DO 4 I= JP1, N
CONST = A(I,J)/A(J,J)
DO 4 K = JP1, NPM
4 A(I,K) = A(I,K) - CONST*A(J,K)
IF( ABS(A(N,N)) - EP) 14, 18, 18
18 DO 11 I=1, N
11 DET = DET*A(I,I)
IF(IJOB) 10, 10, 17
10 DO 12 I=1, N
K = N-I+1
DEGA 01056
DEGA 01057
DEGA 01058
DEGA 01059
DEGA 01060
DEGA 01061
DEGA 01062
DEGA 01063
DEGA 01064
DEGA 01065
DEGA 01066
DEGA 01067
DEGA 01068
DEGA 01069
DEGA 01070
DEGA 01071
DEGA 01072
DEGA 01073
DEGA 01074
DEGA 01075
DEGA 01076
DEGA 01077
DEGA 01078
DEGA 01079
DEGA 01080
DEGA 01081
DEGA 01082
DEGA 01083
DEGA 01084
DEGA 01085
DEGA 01086
DEGA 01087
DEGA 01088
DEGA 01089
DEGA 01090
DEGA 01091
DEGA 01092
DEGA 01093
DEGA 01094
DEGA 01095
DEGA 01096
DEGA 01097
DEGA 01098
DEGA 01099
DEGA 01100
DEGA 01101
DEGA 01102
DEGA 01103
DEGA 01104
DEGA 01105
DEGA 01106
DEGA 01107
DEGA 01108
DEGA 01109
DEGA 01110
DEGA 01111
DEGA 01112
DEGA 01113
DEGA 01114
DEGA 01115
DEGA 01116
DEGA 01117

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KPL = K+1
DO 12 L=NPL, NPM
S= 0.
IF( N - KP1) 12, 20, 20
20 DO 13 J=KP1, N
13 S = S+A(K,J)*A(J,L)
12 A(K,L) = (A(K,L)-S)/A(K,K)
RETURN
END
SUBROUTINE NORMPHI(CAPLAMB, L)
COMMON/AIMAX/ AF(51,402), JMAXF(402), IMAX,
1 IMAXF, IMAXFP1, IMAXB, IMAXBP1, C(3,400),
2 CF(3,402), ATOP(401), ATOPF(402)
DIMENSION AR(51,402), JMAXB(402), CB(3,402), ATOPB(402)
EQUIVALENCE (AF(1), AB(1)), (JMAXF(1), JMAXB(1)),
1 (CF(1), CB(1)), (ATOPF(1), ATOPB(1))
DIMENSION CC(101)
COMMON/SCRATCH/SCRATCH(604)
EQUIVALENCE (SCRATCH(1), CC(1))
SQAB = SQRT(ABS(CAPLAMB))
IBKW = IMAXFP1 + 1
EXPSSQ = EXP(-SQAB*ATOPB(IBKW))
CAPA = AR(1,IBKW)/EXPSSQ
GUNDA2 = (CAPA*EXPSSQ)*2/(2.0*SQAB)
D = ATOPF(2)
CALL POLYMLUL(AF(1:I), JMAXF(I), AF(1:I)+ JMAXF(I), CC, NC)
L2 = 2*I
LD = L2 + NC
SUM = CC(NC)/LD
N = NC
NCM1 = NC - 1
DO 26 NN=1, NCM1
N = N - 1
LD = LD - 1
SUM = SUM*D + CC(N)/LD
26 GUNDA2 = GUNDA2 + SUM*D*(L2 + 1)
IF(IMAXF .EQ. 1) GO TO 27
DO 20 I=2, IMAXF
D = ATOPF(I+1) - ATOPF(I)
CALL POLYMLUL(AF(1:I)+ JMAXF(I), AF(1:I)+ JMAXF(I), CC, NC)
SUM = CC(NC)/NC
N = NC
NCM1 = NC - 1
DO 21 NN=1, NCM1
N = N - 1
21 SUM = SUM*D + CC(N)/N
20 GUNDA2 = GUNDA2 + SUM*D
27 DO 22 I=1, IMAXB
IRKW = IMAXFP1 + I
D = ATOPB(IBKW + 1) - ATOPB(IBKW)
CALL POLYMLUL(AB(1,IBKW), JMAXB(IBKW),
1 AB(1:IBKW), JMAXB(IBKW), CC, NC)
S1,M = -CC(NC)/NC
N = NC
NCM1 = NC - 1
DO 23 NN=1, NCM1
N = N - 1
23 SUM = SUM*D - CC(N)/N
22 GUNDA2 = GUNDA2 + SUM*D
GUNDA = SQRT(GUNDA2)
DO 24 I=1, IMAXF
JJJ = JMAXF(I)
DEGA 01118
DEGA 01119
DEGA 01120
DEGA 01121
DEGA 01122
DEGA 01123
DEGA 01124
DEGA 01125
DEGA 01126
DEGA 01127
DEGA 01128
DEGA 01129
DEGA 01130
DEGA 01131
DEGA 01132
DEGA 01133
DEGA 01134
DEGA 01135
DEGA 01136
DEGA 01137
DEGA 01138
DEGA 01139
DEGA 01140
DEGA 01141
DEGA 01142
DEGA 01143
DEGA 01144
DEGA 01145
DEGA 01146
DEGA 01147
DEGA 01148
DEGA 01149
DEGA 01150
DEGA 01151
DEGA 01152
DEGA 01153
DEGA 01154
DEGA 01155
DEGA 01156
DEGA 01157
DEGA 01158
DEGA 01159
DEGA 01160
DEGA 01161
DEGA 01162
DEGA 01163
DEGA 01164
DEGA 01165
DEGA 01166
DEGA 01167
DEGA 01168
DEGA 01169
DEGA 01170
DEGA 01171
DEGA 01172
DEGA 01173
DEGA 01174
DEGA 01175
DEGA 01176
DEGA 01177
DEGA 01178
DEGA 01179

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DO 24 J=1, JJJ
24 AF(J,I) = AF(J,I)/GUNDA
DO 25 I=1, IMAXB
IRKW = IM, XFP1 + I
JJJ = JMAXB(IRKW)
DO 25 J=1, JJJ
25 AR(J,IRKW) = AB(J,IRKW)/GUNDA
RRETURN
END
SUBROUTINE POLYMUL (A, LM, B, LN, C, LL)
DIMENSION A(1), B(1), C(1)
LL = LM + LN - 1
MMIN = 1
DO 1 L=1 ,LL
IF(L .GT. LM) 3, 2
2 MMAX = L
3 IF(L .GT. LN) 5, 4
4 NMAXP1 = L + 1
GO TO 6
5 MMIN = MMIN + 1
6 C(L) = 0.0
N = NMAXP1
DO 1 M= MMIN , MMAX
N = N - 1
1 C(L) = C(L) + A(M)*B(N)
RRETURN
END
SUBROUTINE MATELE(KPHIMAX, XLAMARY, LARY, ALFAARY, IMAXARY, IZ)
1 NSUBSHL, ISSMAX, NSHELL)
DIMENSION JMAX(400), AM1S(400), AM2S(400)
EQUIVALENCE (SCRATCH(1), ATOP1P1), (SCRATCH(2), C1),
1 (SCRATCH(3), C2), (SCRATCH(4), C3), (SCRATCH(5), JMAX(1)),
2 (SCRATCH(405), AM1S(1)), (SCRATCH(405), AM2S(1))
DIMENSION XLAMARY(1), LARY(1), ALFAARY(1), IMAXARY(1)
1 ,NSUHSHL(1), NSHELL(1)
COMMON/AIMAX/ A(51,100), CAPO(100), IFSTOP(100),
1 XLLP1(100), S1(300), S2(300), DVPOLY(70), SCRATCH(1204)
2 , AM1(400), AM2(400), AMT(51), AMS(51)
3 , A1N(400), A2N(400), ANT(51), ANS(51)
4 , ATOPP1M(400), ATOPP1N(400), JMAXM(400), JMAXN(400)
COMMON/CB1/ HNUVEC(500), ACOFVEC(500), NOPTS, IHNUMAX, MM(100),
1 NN(100), MNMAX, I4MIN, I4MAX
COMMON/EPS/EPSCONV, FBMAX, EM16, EMATELE, EMDVDD, MAXDIM
1 FORMAT(16I5)
2 FORMAT(25I5)
3 FORMAT(5E25.14)
4 FORMAT(2E25.14, I5)
5 FORMAT(/)
6 FORMAT(4E25.14, 2I5)
PRINT1, MNMAX
PRINT 1, (MM(MN), NN(MN), MN=1, MNMAX)
KPHIM4 = KPHIMAX + 4
MAXDIM4 = MAXDIM + 4
ISKIP = 3*MAXDIM + 4
IECS = 1
IECS1 = IECS + MAXDIM4
IECS2 = IECS1 + MAXDIM
CALL ECRD(SCRATCH(1), IECS, KPHIM4, IE)
CALL ECRD(SCRATCH(405), IECS1, KPHIMAX, IE)
CALL ECRD(SCRATCH(805), IECS2, KPHIMAX, IE)
DO 31 KPHI=1, KPHIMAX
A(1,KPHI) = AM1S(KPHI)
DEGA 01180
DEGA 01181
DEGA 01182
DEGA 01183
DEGA 01184
DEGA 01185
DEGA 01186
DEGA 01187
DEGA 01188
DEGA 01189
DEGA 01190
DEGA 01191
DEGA 01192
DEGA 01193
DEGA 01194
DEGA 01195
DEGA 01196
DEGA 01197
DEGA 01198
DEGA 01199
DEGA 01200
DEGA 01201
DEGA 01202
DEGA 01203
DEGA 01204
DEGA 01205
DEGA 01206
DEGA 01207
DEGA 01208
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DEGA 01230
DEGA 01231
DEGA 01232
DEGA 01233
DEGA 01234
DEGA 01235
DEGA 01236
DEGA 01237
DEGA 01238
DEGA 01239
DEGA 01240
DEGA 01241

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```

31 A(2,KPHI) = A42S(KPHI) DEGA 01242
DO 21 KPHI=1, KPHIMAX DEGA 01243
XL = LARY(KPHI) DEGA 01244
IERROR = 0 DEGA 01245
CALL TAYLOR1 (A(1,KPHI), JMAX(KPHI), ATOPIP1,
1 XLAMARY(KPHI), XL, C1, C2, EM16, IERROR) DEGA 01246
JMAXKP = JMAX(KPHI) DEGA 01247
21 XLLP1(KPHI) = XL*(XL + 1.0) DEGA 01248
DO 20 MN=1, MNMAX DEGA 01249
M = MM(MN) DEGA 01250
N = NN(MN) DEGA 01251
LNLM1 = LARY(N) + LARY(M) + 1 DEGA 01252
DEOM = LNLM1 - 1 DEGA 01253
CALL POLYMUL (A(2+M), JMAX(M)-1, A(2+N), JMAX(N)-1, S2, IS2) DEGA 01254
DO 30 J=1, IS2 DEGA 01255
DEOM = DEOM + 1.0 DEGA 01256
30 S2(J) = S2(J)/DEOM DEGA 01257
CALL POLYOP (S2, IS2, ATOPIP1, P) DEGA 01258
20 CAPO(MN) = -C2*P*ATOPIP1**LNLM1 DEGA 01259
DO 36 MN=1, MNMAX DEGA 01260
36 IFSTOP(MN) = 0 DEGA 01261
DO 24 I=2, I2 DEGA 01262
ATOP1 = ATOPIP1 DEGA 01263
IFCS = IECS + ISKIP DEGA 01264
IECS1 = IECS + MAXDIM DEGA 01265
IECS2 = IECS1 + MAXDIM DEGA 01266
CALL ECRD (SCRATCH(1), IECS, KPHIM4, IE) DEGA 01267
CALL ECRD (SCRATCH(405), IECS1, KPHIMAX, IE) DEGA 01268
CALL ECRD (SCRATCH(805), IECS2, KPHIMAX, IE) DEGA 01269
DO 25 KPHI=1, KPHIMAX DEGA 01270
A(1, KPHI) = AM1S(KPHI) DEGA 01271
25 A(2, KPHI) = AM2S(KPHI) DEGA 01272
D = ATOP1 - ATOPIP1 DEGA 01273
DO 27 KPHI=1, KPHIMAX DEGA 01274
IERROR = 0 DEGA 01275
27 CALL TAYLORS(A(1,KPHI), JMAX(KPHI), ATOPIP1,
1 D, XLAMARY(KPHI), XLLP1(KPHI), C1, C2, C3, EM16, IERROR) DEGA 01276
CALL DVDD(ATOPIP1, D, C2, C3, DVPOLY, IDVDD, EMDVDD) DEGA 01277
MLAST = 0 DEGA 01278
DO 28 MN=1, MNMAX DEGA 01279
IF(IFSTOP(MN) .EQ. 5) GO TO 28 DEGA 01280
M= MM(MN) DEGA 01281
N=NN(MN) DEGA 01282
IF(M .EQ. MLAST) GO TO 33 DEGA 01283
MLAST = M DEGA 01284
CALL POLYMUL(A(1,M), JMAX(M), DVPOLY, IDVDD, S1, IS1) DEGA 01285
33 CALL POLYMUL(A(1,N), JMAX(N), S1, IS1, S2, IS2) DEGA 01286
CALL POLYINT(S2, IS2, D, P) DEGA 01287
CAPO(MN) = CAPO(MN) - P DEGA 01288
IF(ABS(P) .LT. ABS(CAPO(MN))*.EMATELE) 34, 35 DEGA 01289
34 IFSTOP(MN) = IFSTOP(MN) + 1 DEGA 01290
GO TO 28 DEGA 01291
35 IFSTOP(MN) = 0 DEGA 01292
28 CONTINUE DEGA 01293
24 CONTINUE DEGA 01294
ATOP12 = ATOPIP1 DEGA 01295
ISKIP = 3*MAXDIM + 4 DEGA 01296
IJUMP = 400 - I2 DEGA 01297
MLAST = 0 DEGA 01298
NLAST = 0 DEGA 01299
DO 40 MN=1, MNMAX DEGA 01300
IF(IFSTOP(MN) .EQ. 5) GO TO 40 DEGA 01301
DEGA 01302
DEGA 01303

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M = MM(MN)
N = NN(MN)
IF(M .EQ. MLAST) 42, 41
41 MLAST = M
IMMAX = IMAXARY(M) - I2
IF(IMMAX .EQ. 0) GO TO 60
IECS = 4*(400 - I2)
IECS = IECS*(M - 1) + 1
IECS = IECS + I2*ISKIP
CALL ECRD(ATOPP1M(1), IECS, IMMAX, IE)
IECS = IECS + IJUMP
CALL ECRD(JMAXM(1), IECS, IMMAX, IE)
IECS = IECS + IJIMP
CALL ECRD(A1M(1), IECS, IMMAX, IE)
IECS = IECS + IJUMP
CALL ECRD(A2M(1), IECS, IMMAX, IE)
60 CONTINUE
42 IF(N .EQ. NLAST) 45, 44
44 NLAST = N
INMAX = IMAXARY(N) - I2
IFIINMAX .EQ. 0) GO TO 61
IECS = 4*(400 - I2)
IECS = IECS*(N - 1) + 1
IECS = IECS + I2*ISKIP
CALL ECRD(ATOPP1N(1), IECS, INMAX, IE)
IECS = IECS + IJUMP
CALL ECRD(JMAXN(1), IECS, INMAX, IE)
IECS = IECS + IJUMP
CALL ECRD(A1N(1), IECS, INMAX, IE)
IECS = IECS + IJUMP
CALL ECRD(A2N(1), IECS, INMAX, IE)
61 CONTINUE
45 IM = 1
IN = 1
ATOPIP1 = ATOPI2
ALASTM = ATOPI2
ALASTN = ATOPI2
IMFIRST = 0
INFIRST = 0
CALL FINDATP(IM, IMMAX, XLLP1(M), ALASTM, ATOPP1M,
1 XLAMARY(4), IERROR)
IF(IERROR .EQ. 14) GO TO 100
CALL FINDATP(IN, INMAX, XLLP1(N), ALASTN, ATOPP1N,
1 XLAMARY(4), IERROR)
IF(IERROR .EQ. 14) GO TO 100
47 CONTINUE
ATOPI = ATOPIP1
IF(ABS(ALASTM-ALASTN) .LT. (ALASTM+ALASTN)*.5E-12) 48, 49
48 INFIRST = 0
IMFIRST = 0
ATOPIP1 = .5*(ALASTM + ALASTN)
CALL FINDA12(IM, IMMAX, XLAMARY(M), ALFAARY(M), XLLP1(M),
1 ATOPIP1, A1M, A2M, JMAXM, AMS, JNSMAX, IERROR)
IF(IERROR .EQ. 12) GO TO 100
CALL FINDA12(IN, INMAX, XLAMARY(N), ALFAARY(N), XLLP1(N),
1 ATOPIP1, A1N, A2N, JMAXN, ANS, JNSMAX, IERROR)
IF(IERROR .EQ. 12) GO TO 100
IM = IM + 1
IN = IN + 1
CALL FINDATP(IM, IMMAX, XLLP1(M), ALASTM, ATOPP1M,
1 XLAMARY(4), IERROR)
IF(IERROR .EQ. 14) GO TO 100
DEGA 01304
DEGA 01305
DEGA 01306
DEGA 01307
DEGA 01308
DEGA 01309
DEGA 01310
DEGA 01311
DEGA 01312
DEGA 01313
DEGA 01314
DEGA 01315
DEGA 01316
DEGA 01317
DEGA 01318
DEGA 01319
DEGA 01320
DEGA 01321
DEGA 01322
DEGA 01323
DEGA 01324
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DEGA 01326
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DEGA 01341
DEGA 01342
DEGA 01343
DEGA 01344
DEGA 01345
DEGA 01346
DEGA 01347
DEGA 01348
DEGA 01349
DEGA 01350
DEGA 01351
DEGA 01352
DEGA 01353
DEGA 01354
DEGA 01355
DEGA 01356
DEGA 01357
DEGA 01358
DEGA 01359
DEGA 01360
DEGA 01361
DEGA 01362
DEGA 01363
DEGA 01364
DEGA 01365

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CALL FINDATP(IN, INMAX, XLLP1(N), ALASTN, ATOPPIN, DEGA 01366
1 XLAMARY(N), IERROR) DEGA 01367
IF(IERROR .EQ. 14) 100, 50 DEGA 01368
49 IF(ALASTM .GT. ALASTN) 51, 52 DEGA 01369
51 INFIRST = 0 DEGA 01370
IMFIRST = IMFIRST + 1 DEGA 01371
ATOPIP1 = ALASTN DEGA 01372
DM = ATOPIP1 - ALASTM DEGA 01373
IF(IMFIRST .EQ. 1) 53, 54 DEGA 01374
53 CALL FINDA12(IM, IMMAX, XLAMARY(M), ALFAARY(M), DEGA 01375
1 XLLP1(M), ALASTM, A1M, A2M, JMAXM, AMT, JMTMAX, IERROR) DEGA 01376
IF(IERROR .EQ. 12) GO TO 100 DEGA 01377
IERROR = 0 DEGA 01378
CALL TAYLORS(AMT, JMTMAX, ALASTM, DM, XLAMARY(M), DEGA 01379
1 XLLP1(M), 0.0, -1.0, 0.0, EM16, IERROR) DEGA 01380
IF(IERROR .EQ. 10) 100, 54 DEGA 01381
54 CALL POLYOP(AMT, JMTMAX, DM, AMS(1)) DEGA 01382
CALL POLY1P(AMT, JMTMAX, DM, AMS(2)) DEGA 01383
JMSMAX = 0 DEGA 01384
CALL FINDA12(IN, INMAX, XLAMARY(N), ALFAARY(N), XLLP1(N), DEGA 01385
1 ATOPIP1, A1N, A2N, JMAXN, ANS, JNSMAX, IERROR) DEGA 01386
IF(IERROR .EQ. 12) GO TO 100 DEGA 01387
IN = IN + 1 DEGA 01388
CALL FINDATP(IN, INMAX, XLLP1(N), ALASTN, ATOPPIN, DEGA 01389
1 XLAMARY(N), IERROR) DEGA 01390
IF(IERROR .EQ. 14) 100, 50 DEGA 01391
52 IMFIRST = 0 DEGA 01392
INFIRST = INFIRST + 1 DEGA 01393
ATOPIP1 = ALASTM DEGA 01394
DN = ATOPIP1 - ALASTN DEGA 01395
IF(INFIRST .EQ. 1) 55, 56 DEGA 01396
55 CALL FINDA12(IN, INMAX, XLAMARY(N), ALFAARY(N), DEGA 01397
1 XLLP1(N), ALASTN, A1N, A2N, JMAXN, ANT, JNTMAX, IERROR) DEGA 01398
IF(IERROR .EQ. 12) GO TO 100 DEGA 01399
IERROR = 0 DEGA 01400
CALL TAYLORS(ANT, JNTMAX, ALASTN, DN, XLAMARY(N), DEGA 01401
1 XLLP1(N), 0.0, -1.0, 0.0, EM16, IERROR) DEGA 01402
IF(IERROR .EQ. 10) 100, 56 DEGA 01403
56 CALL POLYOP(ANT, JNTMAX, DN, ANS(1)) DEGA 01404
CALL POLY1P(ANT, JNTMAX, DN, ANS(2)) DEGA 01405
JNSMAX = 0 DEGA 01406
CALL FINDA12(IM, IMMAX, XLAMARY(M), ALFAARY(M), XLLP1(M), DEGA 01407
1 ATOPIP1, A1M, A2M, JMAXM, AMS, JMSMAX, IERROR) DEGA 01408
IF(IERROR .EQ. 12) GO TO 100 DEGA 01409
IM = IM + 1 DEGA 01410
CALL FINDATP(IM, IMMAX, XLLP1(M), ALASTM, DEGA 01411
1 ATOPPIN, XLAMARY(M), IERROR) DEGA 01412
IF(IERROR .EQ. 14) 100, 50 DEGA 01413
50 D = ATOP1 - ATOPIP1 DEGA 01414
IERROR = 0 DEGA 01415
CALL TAYLORS(AMS, JMSMAX, ATOPIP1, D, XLAMARY(M), DEGA 01416
1 XLLP1(M), 0.0, -1.0, 0.0, EM16, IERROR) DEGA 01417
IF(IERROR .EQ. 10) GO TO 100 DEGA 01418
CALL TAYLORS(ANS, JNSMAX, ATOPIP1, D, XLAMARY(N), DEGA 01419
1 XLLP1(N), 0.0, -1.0, 0.0, EM16, IERROR) DEGA 01420
IF(IERROR .EQ. 10) GO TO 100 DEGA 01421
CALL DVDD(ATOPIP1, D, -1.0, 0.0, DVPOLY, IDVDD, EMDVDD) DEGA 01422
CALL POLYMUL(AMS, JMSMAX, DVPOLY, IDVDD, S1, IS1) DEGA 01423
CALL POLYMUL(ANS, JNSMAX, S1, IS1, S2, IS2) DEGA 01424
CALL POLYINT(S2, IS2, D, P) DEGA 01425
CAPO(MN) = CAPO(MN) - P DEGA 01426
IF(Abs(P) .LT. Abs(CAPO(MN))*EMATELE) 58, 57 DEGA 01427

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PRIN! 7: ISSMAX

DEGA UUUDS

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58 IFSTOP(MN) = IFSTOP(MN) + 1
      IF(IFSTOP(MN) .EQ. 5) 40 47
57 IFSTOP(MN) = 0
      GO TO 47
100 PRINT 101
101 FORMAT(*     ERROR IN REGION 3*)
40 CONTINUE
      DO 29 MN=1, MNMAX
      CAPO(MN) = 2.0*CAPO(MN)
29 PRINT 3, CAPO(MN)
64 FORMAT(E24.14, * EV*, I5, E24.14, * EV*, I5,
1       E24.14, * EV*, E24.14, * BARNS/ATOM*)
65 FORMAT(E24.14, * BARNS/ATOM*)
66 FORMAT(/)
      DO 62 MN=1, MNMAX
      M = MM(MN)
      N = NN(MN)
      DE = ABS(XLAMARY(M) - XLAMARY(N))
      HNUI = DE*13.605
      DE3 = DE*3
      LMAX = LARY(M)
      IF(LARY(N) .GT. LMAX) LMAX = LARY(N)
THE GA AND NOE ARE ONLY GOOD HERE FOR THE BOUND-FREE CASE.
      MNSS = N
      IF(XLAMARY(M) .LT. 0.0) MNSS = M
      ISS = NSHELL(MNSS)*NSHELL(MNSS) - 1)/2 + LARY(MNSS) + 1
      NOE = NSUHSHL(ISS)
      GA = 2*(2*LARY(MNSS) + 1)
      DSIGMA = 10.756E+6*NOE*LMAX*CAPO(MN)**2/(DE3*GA)
      I4 = I4MIN + MN - 1
      ACOFVEC(I4) = ACOFVEC(I4) + DSIGMA
      EM = XLAMARY(M)*13.605
      EN = XLAMARY(N)*13.605
62 CONTINUE
      RETURN
END
SUBROUTINE ZZZ(XLAMWKB, LWKB, NWKB, KWKB, HNUVEC,
1   NOPTS, IHNUMAX, DHNUI, ZZZFAC)
COMMON/SCRATCH/SCRATCH(1204)
DIMENSION XLAMWKB(1), LWKB(1), NWKB(1), HNUVEC(1)
FAC = ALOG(10.0)
DHNU = DHNUI
DO 6 K=1, KWKB
6 XLAMWKB(K) = ABS(XLAMWKB(K))
CALL SORT1(KWKB, 2, XLAMWKB, SCRATCH, LWKB, NWKB)
XLAMWKB(KWKB+1) = ZZZFAC*XLAMWKB(KWKB)
3 IHNUMAX = 0
DO 1 I=1, KWKB
1 EPS = .01
XNUM = ALOG10(ABS(XLAMWKB(I+1))) - ALOG10(ABS(XLAMWKB(I) + EPS))
NOINT = XNUM/DHNU
IF(NOINT .EQ. 0) NOINT = 1
NOINT = NOINT + 1
DHNU = XNUM/NOINT
IHNUMAX = IHNUMAX + 1
IF(IHNUMAX .GT. NOPTS) 4, 5
4 DHNU = 1.2*DHN
GO TO 3
5 HNUVEC(IHNUMAX) = XLAMWKB(I) + EPS
NOINTM1 = NOINT - 1
DO 2 INT=1, NOINTM1
IHNUMAX = IHNUMAX + 1

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IF(IHNUMAX .GT. NOPTS) GO TO 4
XNUM = FAC*(ALOG10(ABS(XLAMWKB(I)) + EPS)) + INT*SDHNÜ
DEGA 01490
DEGA 01491
DEGA 01492
DEGA 01493
DEGA 01494
DEGA 01495
DEGA 01496
DEGA 01497
DEGA 01498
DEGA 01499
DEGA 01500
DEGA 01501
DEGA 01502
DEGA 01503
DEGA 01504
DEGA 01505
DEGA 01506
DEGA 01507
DEGA 01508
DEGA 01509
DEGA 01510
DEGA 01511
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DEGA 01534
DEGA 01535
DEGA 01536
DEGA 01537
DEGA 01538
DEGA 01539
DEGA 01540
DEGA 01541
DEGA 01542
DEGA 01543
DEGA 01544
DEGA 01545
DEGA 01546
DEGA 01547
DEGA 01548
DEGA 01549
DEGA 01550
DEGA 01551

1 HNUVEC(IHNUMAX) = EXP(XNUM)
IHNUMAX = IHNUMAX + 1
IF(IHNUMAX .GT. NOPTS) GO TO 4
1 HNUVEC(IHNUMAX) = XLAMWKB(I+1)
DO 7 K=1, KWKB
7 XLAMWKB(K) = -XLAMWKB(K)
RETURN
END
SUBROUTINE CARSON(XLAMBDA, C2, MFAC, CAPR, XLLP1,
1 CAPF, CAPFP, THETA, THETAP, IERROR)
COMMON/PI/PI, TWOSPI
IERROR = 0
SMALLC = ABS(C2)
SMALLK = SQRT(XLAMBDA)
CAPM = SORT(TWOSPI/SMALLK)
CAPM = MFAC*CAPM
AN = CAPM S BN = 0.0
CSK = SMALLC/SMALLK S CSK2 = CSK*CSK
ACON = XLLP1 + CSK2 S BCON = -(CSK2 + XLLP1)
DEOM = 1.0 S TOK = 2.0*SMALLK
CAPA = AN S CAPB = BN S CAPAP = 0.0 S CAPBP = 0.0
DO 63 NP1 = 1, 15
DEOM = DEOM*CAPR
N = NP1 - 1
XNP1 = NP1
XNNP1 = N*XNP1
TWONP1 = (2.0*N + 1.0)*CSK
XDEOM = TWOK*XNP1
ANP1 = (ACON - XNNP1)*BN - TWONP1*AN)/XDEOM
BNP1 = ((XNNP1 + BCON)*AN - TWONP1*AN)/XDEOM
AADD = ANP1/DEOM S BADD = BNP1/DEOM
APADD = XNP1*AADD S BPADD = XNP1*BADD
CAPA = CAPA + AADD S CAPB = CAPB + BADD
CAPAP = CAPAP + APADD S CAPBP = CAPBP + BPADD
CAPAB = ABS(CAPA) + ABS(CAPB)
CAPABP = ABS(CAPAP) + ABS(CAPBP)
IF( ABS(AADD) .LT. CAPAB*1.0E-4 .AND.
1 ABS(BADD) .LT. CAPAB*1.0E-4 .AND.
2 ABS(APADD) .LT. CAPABP*1.0E-4 .AND.
3 ABS(BPADD) .LT. CAPABP*1.0E-4; GO TO 62
AN = ANP1
63 BN = BNP1
PRINT 64
64 FORMAT(* CAPA, CAPB, CAPAP, AND CAPBP DO NOT CONVERGE.*)
IERROR = 12
RETURN
***** RUN THIS CODE FOR CAPR .GT. 1.0 *****
***** RUN THIS CODE FOR CAPR .GT. 1.0 *****
62 CAPAP = -CAPA/CAPR
CAPBP = -CAPBP/CAPR
CAPF2 = CAPA*CAPA + CAPB*CAPB
CAPF = SQRT(CAPF2)
CAPFP = (CAPA*CAPAP + CAPB*CAPBP)/CAPF
THETA = SMALLK*CAPR + CSK* ALOG(CAPR) + ATAN2(CAPA, CAPB)
THETAP = SMALLK + CSK/CAPR + (CAPAP*CAPB - CAPBP*CAPA)/CAPF2
RETURN
END
SUBROUTINE TAYLOR1(A, JMAX, D, XLAMBDA, XL, C1, C2, EM16, IERROR)
DIMENSION A(1)

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PRIN! 7: ISSMAX

VLOM VVVVV

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IERROR = 0
DEOM = 0.0
DDEOM = 2.0*XL
B1 = 2.0*C1 - XLAMBDA
B2 = 2.0*C2
IF(JMAX .GT. 2) GO TO 40
IFCONV = 0
FAC = 1.0
AMAX = A(2)
AMAXM16 = AMAX*EM16
DO 20 J=3, 50
DDEOM = DDEOM + 2.0
DEOM = DEOM + DDEOM
JM1 = J-1
A(J) = (B1*A(J-2) + B2*A(JM1))/DEOM
FAC = FAC*D
ARSA = JM1*ABS(A(J))*FAC
IF(ARSA .GT. AMAX) 30, 31
30 AMAX = ABSA
AMAXM16 = AMAX*EM16
GO TO 32
31 IF(ARSA .LT. AMAXM16) 33, 32
32 IFCONV = 0
GO TO 20
33 IF(IFCONV .EQ. 1) 35, 34
35 JMAX = J
RETURN
34 IFCONV = 1
20 CONTINUE
IERROR = 9
PRINT 9, IERROR
9 FORMAT (15,* TAYLOR SERIES DOES NOT CONVERGE IN SUBROUTINE TAYLOR1
1. DO-LOOP 20.*)
RETURN
40 DO 41 J=3, JMAX
DDEOM = DDEOM + 2.0
DEOM = DEOM + DDEOM
JM1 = J-1
41 A(J) = (B1*A(J-2) + B2*A(JM1))/DEOM
RETURN
END
SUBROUTINE TAYLORS(A, JMAX, RR, D, XLAMBDA)
1     XLLP1, C1, C2, C3, EM16, IERROR)
DIMENSION A(1)
IFRROR = 0
RR2 = RR*RR
TWORR = 2.0*RR
SR1 = XLAMBDA - 2.0*C1
SR2 = -2.0*C2
SR3 = -(2.0*C3 + XLLP1)
B1 = SR1*RR2 + SR2*RR + SR3
B2 = SR1*TWORR + SR2
B3 = SR1
A(3) = -B1*A(1) / (2.0*RR2)
A(4) = -(B2*A(1) + B1*A(2) + 2.0*TWORR*A(3)) / (6.0*RR2)
IF(JMAX .GT. 5) GO TO 60
ABSD = ABS(D)
FAC = 1.0
AMAX = ABS(A(2))
AMAXM16 = AMAX*EM16
FAC = FAC*ABSD
ABS3 = 2.0*ABS(A(3))*FAC
DEGA 01552
DEGA 01553
DEGA 01554
DEGA 01555
DEGA 01556
DEGA 01557
DEGA 01558
DEGA 01559
DEGA 01560
DEGA 01561
DEGA 01562
DEGA 01563
DEGA 01564
DEGA 01565
DEGA 01566
DEGA 01567
DEGA 01568
DEGA 01569
DEGA 01570
DEGA 01571
DEGA 01572
DEGA 01573
DEGA 01574
DEGA 01575
DEGA 01576
DEGA 01577
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DEGA 01594
DEGA 01595
DEGA 01596
DEGA 01597
DEGA 01598
DEGA 01599
DEGA 01600
DEGA 01601
DEGA 01602
DEGA 01603
DEGA 01604
DEGA 01605
DEGA 01606
DEGA 01607
DEGA 01608
DEGA 01609
DEGA 01610
DEGA 01611
DEGA 01612
DEGA 01613

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IF(ABS3 .GT. AMAX) 54, 55          DEGA 01614
54 AMAX = ABS3                      DEGA 01615
AMAXM16 = AMAX*EM16                DEGA 01616
55 FAC = FAC*ABSD                 DEGA 01617
ARS4 = 3.0*ABS(A(4))*FAC          DEGA 01618
IF(ABS4 .GT. AMAX) 56, 57          DEGA 01619
56 AMAX = ABS4                      DEGA 01620
AMAXM16 = AMAX*EM16                DEGA 01621
57 DO 26 J=6, 50, 2                DEGA 01622
JM1=J-1   S   JM2 = J-2   S   JM3 = J-3          DEGA 01623
JM4 = J-4   S   JM5 = J-5          DEGA 01624
DEOM = JM3*JM2*RR2                DEGA 01625
A(JM1) = -(B3*A(JM5) + B2*A(JM4) +(B1+JM5*JM4)*A(JM3))          DEGA 01626
1      +JM4*JM3*TWORR*A(JM2) )/DEOM          DEGA 01627
DEOM = JM2*JM1*RR2                DEGA 01628
A(J) = -(B3*A(JM4) + B2*A(JM3) +(B1+JM4*JM3)*A(JM2))          DEGA 01629
1      +JM3*JM2*TWORR*A(JM1) )/DEOM          DEGA 01630
FAC = FAC*ABSD                  DEGA 01631
ARSA1 = JM2*ABS(A(JM1))*FAC        DEGA 01632
FAC = FAC*ABSD                  DEGA 01633
ARSA = JM1*ABS(A(J))*FAC          DEGA 01634
IF(ARSA .GT. AMAX) 45, 44          DEGA 01635
45 AMAX = ABSA                      DEGA 01636
AMAXM16 = AMAX*EM16                DEGA 01637
IF(ARSA1 .GT. AMAX) 46, 26          DEGA 01638
46 AMAX = ABSA1   S   AMAXM16 = AMAX*EM16   S   GO TO 26          DEGA 01639
44 IF(ARSA1 .GT. AMAX) 46, 47          DEGA 01640
47 IF(ARSA .LT. AMAXM16) 48, 26          DEGA 01641
48 IF(ARSA1 .LT. AMAXM16) 49, 26          DEGA 01642
49 JMAX = J                      DEGA 01643
      RRETURN
26 CONTINUE
IERROR = 10                      DEGA 01644
PRINT 10, IERROR, 1                DEGA 01645
10 FORMAT(2I5,* TAYLOR SERIES DOES NOT CONVERGE IN SUBROUTINE TAYLOR          DEGA 01646
1S. DO-LOOP 26 IN LOOP 25.*)
JMAX = 50                      DEGA 01647
IERROR = 0                      DEGA 01648
1 FORMAT(4E24.14)
PRINT 1, AMAX, AMAXM16, ABSA, ABSA1          DEGA 01649
RETURN                           DEGA 01650
60 DO 27 J=6, JMAX, 2                DEGA 01651
JM1=J-1   S   JM2 = J-2   S   JM3 = J-3          DEGA 01652
JM4 = J-4   S   JM5 = J-5          DEGA 01653
DEOM = JM3*JM2*RR2                DEGA 01654
A(JM1) = -(B3*A(JM5) + B2*A(JM4) +(B1+JM5*JM4)*A(JM3))          DEGA 01655
1      +JM4*JM3*TWORR*A(JM2) )/DEOM          DEGA 01656
DEOM = JM2*JM1*RR2                DEGA 01657
27 A(J) = -(B3*A(JM4) + B2*A(JM3) +(B1+JM4*JM3)*A(JM2))          DEGA 01658
1      +JM3*JM2*TWORR*A(JM1) )/DEOM          DEGA 01659
      RETURN
END
SUBROUTINE POLY0P( A, JMAX, D, P)
DIMENSION A(I)
M = JMAX
P = A(M)
JUP = M - 1
IF(JUP .LT. 1) RETURN
DO 1 J=1, JUP
M = M- 1
1 P = P*D + A(M)
      RETURN

PRINT 7, ISSMAX                      DEGA 01660

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ENTRY POLYIP
M = JMAX
P = (M-1)*A(M)
JUP = M-2
IF(JUP .LT. 1) RETURN
DO 2 J=1, JUP
M = M-1
2 P = P*D + (M-1)*A(M)
RETURN
ENTRY POLYINT
M = JMAX
P = A(M)/M
J1,P = M-1
IF(JUP .LT. 1) GO TO 4
DO 3 J=1, JUP
M = M-1
3 P = P*D + A(M)/M
4 P = P*D
RETURN
END
SUBROUTINE DVDD( ATOP1, D, C2, C3, DVPOLY, IDVDD, EMDVDD)
COMMON/SCRATCH/SCRATCH(604)
DIMENSION DVPOLY(1)
OATOP1 = -1.0/ATOP1
DN = 1.0
IF(C3 .EQ. 0.0) 10, 20
10 IDVDD = 1
DVPOLY(1) = -C2/ATOP1**2
EPSILON = ABS(DVPOLY(1))*EMDVDD
TERMLST = DVPOLY(1)
30 IDVDD = IDVDD + 1
TERMLST = TERMLST*OATOP1
DN = DN*D
DVPOLY(IDVDD) = IDVDD*TERMLST
IF(Abs(DVPOLY(IDVDD)*DN) .LT. EPSILON) 40, 30
20 ISCH = 1
ICNT1 = 1
ICNT2 = 1
SCRATCH(1) = -1.0/ATOP1**3
EPSILON = ABS(SCRATCH(1))*EMDVDD
TERMLST = SCRATCH(1)
50 ISCH = ISCH + 1
ICNT2 = ICNT2 + 1
ICNT1 = ICNT1 + ICNT2
TERMLST = TERMLST*OATOP1
DN = DN*D
SCRATCH(ISCH) = ICNT1*TERMLST
IF(Abs(SCRATCH(ISCH)*DN) .LT. EPSILON) 60, 50
60 SCRATCH(499) = C2*ATOP1 + 2.0*C3
SCRATCH(500) = C2
CALL POLYMUL(SCRATCH(1), ISCH, SCRATCH(499), 2, DVPOLY, IDVDD,
40 RETURN
END
SUBROUTINE FINDA12(I, IMAX, XLAM, ALFA, XLLP1, ATOP1P1,
1      A1, A2, JMAX, AS, JSMAX, TERROR)
DIMENSION A1(1), A2(1), JMAX(1), AS(2)
TERROR = 0
IF(I .GT. IMAX) 2, 1
1 AS(1) = A1(I)
AS(2) = A2(I)
JSMAX = JMAX(I)
RETURN

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DEGA 01676
DEGA 01677
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DEGA 01737

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2 CALL CARSON(XLAM, -1.0, 1, ATOPPI1, XLLP1, ----- DEGA 01738
1   CAPF, CAPFP, THETA, THETAP, IERROR) DEGA 01739
IF(IERROR .EQ. 12) RETURN DEGA 01740
THETA1 = THETA + ALFA DEGA 01741
COSTHE1 = COS(THETA1) DEGA 01742
AS(1) = CAPF*COSTHE1 DEGA 01743
AS(2) = CAPFP*COSTHE1 - CAPF*THETAP*SIN(THETA1) DEGA 01744
JSMAX = 0 DEGA 01745
RETURN DEGA 01746
END DEGA 01747
SUBROUTINE FINDATP(IM, IMAX, XLLP1, ALAST, ATOPP1, XLAMB, IERROR) DEGA 01748
DIMENSION ATOPP1(1) DEGA 01749
IERROR = 0 DEGA 01750
IF(IM .GT. IMAX) 2, 1 DEGA 01751
1 ALAST = ATOPP1(IM) DEGA 01752
RETURN DEGA 01753
2 IF(XLAMB .GT. 0.0) 4, 3 DEGA 01754
3 IERROR = 14 DEGA 01755
RETURN DEGA 01756
4 DR = .2*ALAST DEGA 01757
R1 = 1.05*ALAST DEGA 01758
CALL DRMAXSB(DRMAX, ALAST, R1, XLAMB, XLLP1, 1) DEGA 01759
IF(DR .GT. DRMAX) DR = DRMAX DEGA 01760
ALAST = ALAST + DR DEGA 01761
RETURN DEGA 01762
END DEGA 01763

```

PRINT 7, ISSMAX

DEGA 00003

01/09/73 +LASL MCH1 .16 01/09/73 MACH. I ECS ON
18.56.54.J15WM2W 01/09/73
18.56.54.SJOB(NAME=J15WM, AC=J15D, USF=DEGAA, TL=
18.56.54.1 SC=156000, PL=200, MX=66,
18.56.54.S1 CL=U, PR=6, CAT=6, UA=87)5C131)
18.56.55.ASSIGNMT, OLDPL(PLB+LF223L00,SHB)
18.56.55.65 ASSIGNED
18.56.55.LF223L00
18.56.55.ASSIGNMT, NEWPL(NLB+,SHB)
18.56.56.66 ASSIGNED
18.56.56.LD274L00
18.56.56.UPDATE(F,S)
18.57.07. DECK STRUCTURE CHANGED
18.57.07. DECK STRUCTURE CHANGED
18.57.14. UPDATING FINISHED
18.57.15.REWIND(SOURCE)
18.57.16.UPDATE(N,I=SOURCE)
18.57.38. UPDATING FINISHED
18.57.38.COPYSBF(COMPILE,OUTPUT)
18.57.43.CP 00005.336 SEC.
18.57.43.PP 00057.626 SEC.
18.57.43.SS 00127.002 SEC.
18.57.43.
18.57.43.
18.57.43.
18.57.43.

2W

2W

2W