

WF-970907--

Title: Calculated Lattice Relaxation in Plutonium-Gallium Alloys

UNCLASSIFIED NOT UCNI

AUG 12 1997  
date

Author(s): John David Becker, CMS  
John M. Wills, T-1  
Larry Cox, NMT-5  
Bernard R. Cooper West Virginia Univ.

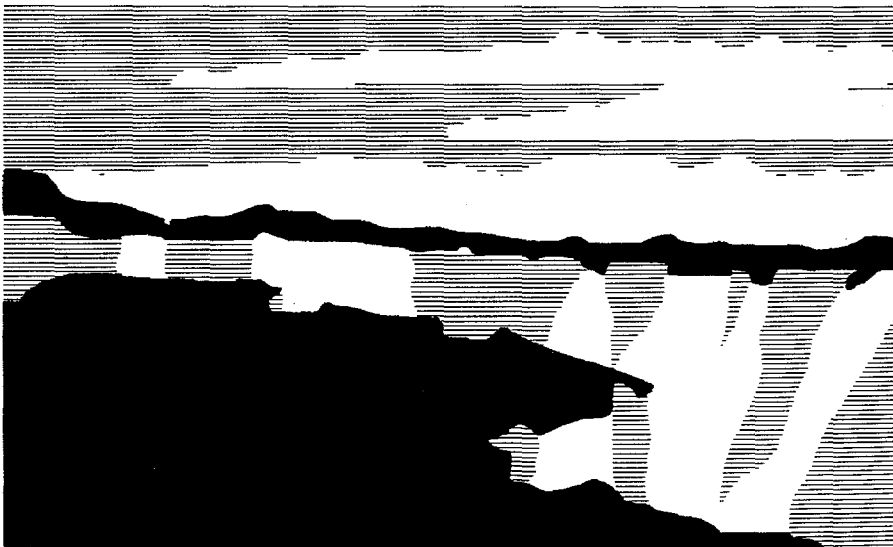
RECEIVED  
DEC 01 1997  
OSTI

Submitted to: To be published in Journal of Alloys and Compounds in conjunction with the Actinides '97 conference

MASTER

Los Alamos

NATIONAL LABORATORY



Los Alamos National Laboratory, an affirmative action/equal opportunity employer, is operated by the University of California for the U.S. Department of Energy under contract W-7405-ENG-36. By acceptance of this article, the publisher recognizes that the U.S. Government retains a nonexclusive, royalty-free license to publish or reproduce the published form of this contribution, or to allow others to do so, for U.S. Government purposes. The Los Alamos National Laboratory requests that the publisher identify this article as work performed under the auspices of the U.S. Department of Energy.

REPRODUCTION OF THIS DOCUMENT IS UNLIMITED

*Handwritten signature*

## **DISCLAIMER**

This report was prepared as an account of work sponsored by an agency of the United States Government. Neither the United States Government nor any agency thereof, nor any of their employees, makes any warranty, express or implied, or assumes any legal liability or responsibility for the accuracy, completeness, or usefulness of any information, apparatus, product, or process disclosed, or represents that its use would not infringe privately owned rights. Reference herein to any specific commercial product, process, or service by trade name, trademark, manufacturer, or otherwise does not necessarily constitute or imply its endorsement, recommendation, or favoring by the United States Government or any agency thereof. The views and opinions of authors expressed herein do not necessarily state or reflect those of the United States Government or any agency thereof.

## **DISCLAIMER**

**Portions of this document may be illegible in electronic image products. Images are produced from the best available original document.**

# Calculated lattice relaxation in Pu-Ga alloys

J. D. Becker, J. M. Wills, and L. Cox

*Center for Materials Science, Theoretical Division, and Nuclear Materials Technology Division*

*MS K765, Los Alamos National Laboratory, New Mexico 87545*

B. R. Cooper

*Department of Physics, West Virginia University, Morgantown, West Virginia 26506-6315*

(today)

## Abstract

Hellman-Feynman forces on atoms surrounding the gallium site in a  $\text{Pu}_{31}\text{Ga}$  supercell are calculated with the full-potential LMTO method in the local density approximation. These forces are minimized by adjusting atomic positions using an iterative Broyden scheme. At equilibrium the nearest-neighbor shell of plutonium atoms relaxes inward by 1.04% of the initial theoretical bond length (2.86 Å). A similar calculation on a  $\text{Pu}_{32}$  supercell shows no relaxation.

## I. INTRODUCTION

The  $\delta$  (nominally fcc) phase of plutonium is stable from 320°C to 463°C. Addition of small amounts (the solvus lines are not precisely known) of gallium stabilizes the  $\delta$  phase to room temperature – at least the phase is kinetically stable.

No fundamental description of the  $\delta$  phase yet exists. Söderlind *et al*<sup>3</sup> demonstrate the suitability of the application of the local density approximation (LDA) and the related general gradient approximation (GGA) to the ground state of Pu. Due to the high density of states at the Fermi energy of the itinerant  $f$  states the ground state of Pu is determined by the band filling and the tendency to split the band via a Peierls-Jahn-Teller distortion. They obtain excellent agreement for the density of the low-temperature, monoclinic  $\alpha$  phase by treating the  $f$  states as itinerant. This approach leads to large errors in the density calculation (approximately 30%) for  $\delta$ -Pu<sup>4,5</sup> as well as in the Pu<sub>3</sub>X compounds for the  $\delta$  stabilizers X = Al, Ga, In, or Tl<sup>5</sup>. Additionally, the LDA predicts that the Pu<sub>3</sub>X compounds are metastable in calculations treating  $f$  states as itinerant<sup>5</sup>.

X-ray absorption fine-structure spectroscopy (EXAFS) determines the local environment around specific sites whereas x-ray diffraction yields only average properties. Cox *et al*<sup>1</sup> performed EXAFS measurements on 3.3 at. % Ga alloy. They report that the plutonium atoms in the nearest-neighbor shells surrounding gallium atoms relax inward by 3.7 % of the ideal bond length, 4.61 Å. Faure *et al*<sup>2</sup> performed EXAFS analyses on alloys ranging from 3.43 at. % Ga to 10.43 at. %. For the 3.43 at. % alloy they find an inward relaxation of 3.5 %. They also show a minimum in the relaxation (with respect to concentration of gallium) of 1.6 % of the average bond length at a concentration of 7 at. %.

In this study the question as to whether the LDA can reflect the modification of the transition temperature of  $\delta$  Pu from 320°C to near room temperature by small additions of Ga is explored by first-principles calculation of the electronic structure and atomic forces in an ordered 3.125 at. % Ga alloy. The structural disorder around the Ga sites modifies the electronic structure, and this change is examined for implications on the structural stability

of the alloy.

## II. COMPUTATIONAL METHOD

The minimum energy volume of a fcc-based 32 atom supercell ( $\text{Pu}_{31}\text{Ga}$  with the Ga atom in the center) is determined with the full-potential LMTO method<sup>6,7</sup> in the local density approximation [LDA] with the von Barth-Hedin<sup>9</sup> density functional. The calculations are all-electron and scalar relativistic. To keep the force calculation to a reasonable size spin-orbit interaction is excluded.

The basis sets include the  $6s$ ,  $6p$ ,  $7s$ ,  $7p$ ,  $6d$  and  $5f$  partial waves for Pu the  $3d$ ,  $4s$ , and  $4p$  for Ga. Two sets of energy parameters are used for the calculation of the basis within the muffin tin, the lower energy being appropriate for semi-core states and the higher for valence levels. The orbitals are defined within a single energy panel to allow hybridization, i.e., matrix elements connecting basis functions associated with different sets of energy parameters are included in the Hamiltonian and overlap matrix elements.

The sampling over the irreducible wedge of the Brillouin zone is performed with the special k-point method<sup>8</sup>. 10 points per atom in the irreducible wedge of the zone – corresponding to 216 points per atom, or 6912 points in the full Brillouin zone – are used. The convergence is accelerated by associating each eigenvalue with a small Gaussian function of width 10 mRy.

In the 32 atom supercell (see Fig. 1) only the nearest- and third-nearest neighbors are allowed to move under the constraint of cubic symmetry. The nearest neighbors move along the diagonals  $\langle 011 \rangle$  of the  $\{200\}$  planes, and the third nearest neighbors move along the cell-face diagonals  $\langle \bar{1}\bar{1}0 \rangle$  of the  $\{100\}$  planes). The Pu atoms in the 2nd shell surrounding Ga are halfway between Ga atoms in adjacent supercells and are therefore fixed by symmetry.

The forces on the Pu atoms in the nearest-neighbor and third nearest-neighbor shells surrounding the Ga atom are calculated for a self-consistent potential. These forces, constrained to reflect the crystal symmetry, are parallel to the aforementioned degrees of free-

dom. The positions of those atoms are then adjusted to lower the forces by a modified Broyden technique. The force calculation is repeated with subsequent corrections to the lattice configuration until the projected corrections are less than .001% of the initial bond length. This corresponded to magnitudes of the forces of less than  $1 \times 10^{-13}$  Newtons. For this study 6 iterations were required to find the "relaxed" configuration.

### III. RESULTS AND DISCUSSION

A  $\text{Pu}_{32}$  supercell with the same lattice as Fig. 1 is examined for local distortions. The space group is lowered to orthorhombic to allow more complicated distortion modes. The calculated forces on all of the atoms are less than  $1 \times 10^{-8}$  Ry/a.u.

The  $\text{Pu}_{31}\text{Ga}$  supercell minimum energy lattice parameter is 8.096 Å. For the initial perfect fcc - lattice, the forces on the atoms in the nearest and third nearest neighbor shells are -.0055 Ry/a.u. and .004 Ry/a.u. respectively ( $1 \text{ Ry/a.u.} = 4.119 \times 10^{-8}$  Newtons). The negative sign on the nearest-neighbor force indicates a force with a sense acting toward the gallium atom at the center, and the positive sign on the third nearest neighbor force means a force pushing the atom away from the face center - and further from the gallium atom.

In the final configuration the Pu atoms in the nearest-neighbor shell have contracted inward by 1.0414 % of the initial Pu-Ga bond length, 2.86251 Å. The third-nearest neighbor shell has relaxed away from the gallium site by 0.474 % of the original distance of 4.958 Å. The shell surrounding 5th neighbor contracts isotropically by 1.416

The decrease in total energy from the initial to final configuration is 0.0283 mRy/atom. The formation energy of the alloy is + 0.295 Ry/atom. As in the case of the  $\text{Pu}_3\text{X}$  compounds the LDA calculations indicate the "Ga-stabilized" alloys are actually metastable at low temperature. As noted by Adler<sup>10</sup> consideration of thermodynamic measurements in the Pu-rich alloys implies a low-temperature decomposition of the  $\delta$  phase into  $\alpha + \text{Pu}_3\text{X}$ .

Measurements of the average Pu-Ga bond length in alloys and LDA calculations of the atomic volume suggest that the main modification of the electronic structure due to a Ga

impurity is realized with, at most, the addition of 3.3 at% Ga. This is supported by analysis of the bands and densities of states of the compounds and elements. Fig. 2 shows the densities of states projected onto Pu and Ga sites for Pu<sub>3</sub>Ga,  $\delta$  Pu, fcc Ga, and Pu<sub>31</sub>Ga. The hybridization of Ga 4*p* states with Pu 6*d* is apparent in Pu<sub>31</sub>Ga even in the 5th neighbor shells surrounding the Ga atoms. The effect upon the 5*f* states is less pronounced in the 5th neighbors where the *f*-projected DOS is much more like that of pure  $\delta$  Pu, than in those of the nearest neighbor Pu sites where the impurity induced spectra resemble those of the Pu<sub>3</sub>Ga compound. The projected spectra associated with the other 3 crystallographic sites in the supercell show less pronounced trends.

The discrepancy between the measured and calculated relaxed bond lengths may originate in the treatment of the Pu 5*f* electrons. Perhaps the magnitude of the relaxation is limited primarily by the much lower unit cell volume in the LDA model, or perhaps the over bonding inherent in the LDA restricts the relaxation as well. The very question of the “volume problem” in  $\delta$ -Pu has been explored with *ad hoc* studies. For example, Eriksson *et al*<sup>11</sup> and Pénicaud<sup>12</sup> use constrained Hamiltonians to localize some *f* states resulting in volumes that are very close to the measured values. Méot-Reymond and Fournier<sup>13</sup> hypothesize a Mott-like transition between  $\alpha$ - and  $\delta$ -Pu to a Kondo compensated ground state for  $\delta$ -Pu. These calculations all support the long-held notion that a rigorous, predictive theory for the partial localization of *f*-states is required in order to capture fully the enigmatic properties of Pu.



## REFERENCES

- <sup>1</sup> L. E. Cox, R. Martinez, J. H. Nickel, S. D. Conradson, and P. G. Allen, *Phys. Rev. B* **51**, 751 (1995).
- <sup>2</sup> Ph. Faure, B. Deslandes, D. Bazin, C. Tailland, R. Doukhan, J. M. Fournier, and A. Falanga, *J. Alloys Compounds* **244**, 131 (1996).
- <sup>3</sup> P. Söderlind, J. M. Wills, B. Johansson, and O. Eriksson, *Phys. Rev. B* **55**, 1997 (1997).
- <sup>4</sup> P. Söderlind, O. Eriksson, J. M. Wills, and A. M. Boring, *Phys. Rev. B* **48**, 9306 (1993); B. Johansson and A. Rosengrin, *ibid*, **11**, 2836 (1975); E. A. Kmetko and H. H. Hill, in *Plutonium 1970 and Other Actinides*, ed. W. N. Miner (Metall. Soc. AIME, New York, 1970); Warren E. Pickett, A. J. Freeman and D. D. Koelling, *Phys. Rev. B* **22**, 2695 (1980); H. L. Skriver, O. K. Andersen, and B. Johansson, *Phys. Rev. Lett.*, **41**, 42 (1978); **44**, 1230 (1980); M. S. S. Brooks, B. Johansson, and H. L. Skriver, *Handbook on the Physics and Chemistry of the Actinides*, ed. A. J. Freeman and G. H. Lander (North-Holland, Amsterdam, 1984), Vols. 1-5.
- <sup>5</sup> J. D. Becker, J. M. Wills, L. Cox, and B. R. Cooper, *Phys. Rev. B* **54**, 17265 (1996).
- <sup>6</sup> J. M. Wills, unpublished, J. M. Wills and B. R. Cooper, *Phys. Rev. B* **36**, 3809 (1987), D. L. Price and B. R. Cooper, *ibid*, **39**, 4945 (1989).
- <sup>7</sup> O. K. Anderson, *Phys. Rev. B* **12**, 3060 (1975).
- <sup>8</sup> L. Cunningham, *Phys. Rev. B* **10**, 4988 (1974).
- <sup>9</sup> P. Hohenburg and W. Kohn, *Phys. Rev.* **136**, B864 (1964), W. Kohn and L. Sham, *Phys. Rev.* **140**, A1133 (1965), U. von Barth and L. Hedin, *J. Phys. C* **5**, 1629 (1972).
- <sup>10</sup> P. H. Adler, *Met. Trans. A* **22A**, 2237 (1991).
- <sup>11</sup> O. Eriksson, J. D. Becker, and J. M. Wills *in progress*.
- <sup>12</sup> M. Pénicaud, *J. Phys. Cond. Matter*, **9**, 6341 (1997).

<sup>13</sup>S. Méot-Reymond and J. M. Fournier, *J. of Alloys and Compounds*, **232**, 119 (1996).

## FIGURES

FIG. 1.  $\text{Pu}_{31}\text{Ga}$  supercell. Gallium atom is denoted by filled circle. Typical nearest-neighbor plutonium atom is labeled 1. Third-nearest neighbor is labeled 3. Arrows show relaxation modes.

FIG. 2. Projected densities of states in  $\delta\text{-Pu}$ , fcc Ga, and in the  $\text{Pu}_{31}\text{Ga}$  supercell. The graphs on the left show the  $5f$ -projected DOS, and the  $6d$ ,  $4p$ -projected DOS are on the left. All spectra

Ry.

